



DEPARTMENT OF AEROSPACE ENGINEERING  
INDIAN INSTITUTE OF TECHNOLOGY MADRAS  
CHENNAI – 600036

# Development of a Vision Guided Aerially Launched Short Range Missile



*A Thesis*

*Submitted by*

**APPILI VAMSI KRISHNA**

*For the award of the degree*

*Of*

**MASTER OF TECHNOLOGY**

May 2022





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*There's power in your purpose!*

**– Joe Braxton**



*I dedicate this thesis to my parents, teachers for inspiring me,  
guiding me, thus, shaping a beautiful life to me*



# THESIS CERTIFICATE

This is to undertake that the Thesis titled **DEVELOPMENT OF A VISION GUIDED AERIALY LAUNCHED SHORT RANGE MISSILE**, submitted by me to the Indian Institute of Technology Madras, for the award of **Master of Technology**, is a bona fide record of the research work done by me under the supervision of **Dr. S R Chakravarthy**. The contents of this Thesis, in full or in parts, have not been submitted to any other Institute or University for the award of any degree or diploma.

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# ABSTRACT

When the knowledge of Aerospace engineering proved its use in possibilities of enhancement in defense and security, providing supremacy for a nation in the global community, with ensuring land safety and country sovereignty had lead to the interest over years in development of weapons like UCAVs, Missiles.

Now a days, there is high tension in every country if a country announces their advanced defense capabilities in terms of missile technology, namely nuclear missiles, ICBMs, Interceptor systems. Missiles are highly used in today war (or) to prove strength, so other countries respects our interests by treating their equals.

India is exporting Brahmos missiles to Vietnam, Philippines, these missiles have unit cost in order of Millions of USD. Since each missile is so costly, we cant afford to lose it due to interception by enemy during operation, Thus missile wont be used until it is an inevitable situation

The Idea of the thesis is to develop a low cost air to ground missile which is capable of attacking target that is 2 km far, when launched via an aerial platform (fixed wing UCAV or Hexarotor UCAV) from an altitude of 500 to 1000 meters from mean sea level. Aim is to launch a swarm of missiles over a target autonomously, So, we need not worry about any interceptors in mid-way. Also, we can save many of our valuable soldier lives, since we use autonomous, human-pilot-less systems, thus reducing majority of the possible collateral damage during attack initiation. This technology is need of the hour since India received potential suside bomber threats from Al-Qaeda in the Subcontinent (AQIS) on June 6, 2022. This missile is portable and is capable of launch from the hand launcher.

This thesis details the design of rocket motor and 4 versions of missile with their archetecture, subsystem standards and specifications and overall development of Precision Guided Munition (PGM) Missile 5 kg



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## ABBREVIATIONS

<b>AC</b>	Aerodynamic Centre.
<b>Al</b>	Aluminium.
<b>AOA</b>	Angle of attack.
<b>AP</b>	Ammonium perchlorate.
<b>ASCII</b>	American Standard Code For Information Exchange.
<b>ASI</b>	Aircraft Stores Interface.
<b>BC</b>	Bus Controller.
<b>BEM</b>	Balastic Evaluation Motor.
<b>BIT</b>	Built-in-Test.
<b>BLOSOA</b>	Backup-Line-of-sight-Obstacle-Avoidance-Trajectory.
<b>CEA</b>	Chemical Equilibrium Analysis.
<b>CEP</b>	Circular Error Probability.
<b>COTS</b>	Commercially Off the Shelf.
<b>CPU</b>	Central Processing Unit.
<b>DARPA</b>	Defense Advanced Research Projects Agency.
<b>DOA</b>	Dioctyl adipate.
<b>DOF</b>	Degree of Freedom.
<b>FCC</b>	Flight Control Computer.
<b>FCS</b>	Flight Control System.
<b>FPS</b>	Frame Per Second.
<b>GPS</b>	Global Positioning System.

<b>HTPB</b>	Hydroxyl-Terminated PolyButadiene.
<b>I2C</b>	Inter Integrated Circuit.
<b>IITM</b>	Indian Institute of Technology, Madras.
<b>IMU</b>	Inertial Measurement Init.
<b>IPDI</b>	Isophorone diisocyanate.
<b>Lat-Long</b>	Latitude and Longitude.
<b>LOS-OA</b>	Line of Sight Obstacle Avoidance.
<b>LOS-OA-G</b>	Line of Sight Obstacle Avoidance Guided.
<b>MC</b>	Mission Computer.
<b>NCCRD</b>	National Centre for Combustion Research and Development.
<b>ORB</b>	Oriented FAST and Rotated BRIEF.
<b>PCB</b>	Printed Circuit Board.
<b>RAM</b>	Random Access Memory.
<b>ROM</b>	Read Only Memory.
<b>RT</b>	Remote Terminal.
<b>SCADA</b>	Supervisory Control and Data Acquisition.
<b>SCB</b>	The Single Board Computer.
<b>SIFT</b>	Scale-invariant feature transform.
<b>SMP</b>	Stores Management Processor.
<b>SMS</b>	Stores Management System.
<b>SRM</b>	Solid Rocket Motor.
<b>TCP/IP</b>	transmission Control Protocol / Internet protocol.
<b>TTL</b>	Transistor Transistor Logic.
<b>UAV</b>	Unmanned aerial Vehicle.

**UCAV** Unmanned Combat Aerial Vehicle.

**VTOL** Vertical Take-Off and Landing.

**WP** Warhead Payload.



# NOTATION

$V$	Free stream Velocity
$g$	Acceleration due to gravity
$\phi$	Roll angle
$\theta$	Pitch angle
$C^*$	Propellant Characteristics Velocity
$C_D$	Coefficient of Drag
$I_{sp}$	Specific Impulse
$\alpha$	Angle of attack
$\beta$	Side slip angle
$\gamma$	Flight path angle
$\psi$	Yaw angle
$\rho$	density of substance
$C_L$	Coefficient of Lift
$I_{xx}$	Mass moment of inertia
$t_b$	Propellant burnout time
$C_M$	Coefficient of pitching moment
$r_0$	Propellant burn rate
$L$	Rolling moment
$M$	Pitching moment

N Yaw moment

P Pressure

p Roll rate

q Pitch rate

r Yaw rate

# CHAPTER 1

## INTRODUCTION

Defense Advanced Research Projects Agency (DARPA) is working on utilising Unmanned Combat Aerial Vehicles (UCAV)s for front-line defense where there is high chance of collateral damage, Refer [1]. The target application of these missions was to attack the enemy location without loss of our own soldiers. DARPA's X-45 program produced a UAV with tactical aircraft performance, which demonstrated formation flight, manned/unmanned teaming, and a coordinated strike against simulated radars and missile launchers. X-45 could be seen as the proof-of-concept vehicle for the unmanned combat air vehicle (UCAV) concept. These systems developed by DARPA is quite expensive, but efficient in their operation. There is need of indigenous development of classified payloads, for the specific UCAVs that can be developed indigeniously. This idea has been originated in 2019, by Squadron Leader Ravi Raj SR, and began the development of project with the core idea of cost-effective, lessen collateral damage, equipment that is fully indigenous designed & developed.

### 1.1 PROBLEM STATEMENT

Design a missile of Vision Guided Aerially Launched (from altitude of 500 meter to 1000 meter) Short Range Missile (with range of 2 km) with overall structural mass of 5 kg, which includes the payload, propellant, ignition system, battery, electrical equipment, gimbal system, structural components. Also, Design the accessory systems ie., ground launcher, hand launcher, weapon release system.

## **1.2 AIM**

To indigenously develop, cost effective, 5 kg short range missile with payload of minimum 2 kg, which can be attached to UCAV such as indigenously developed VTOL drone or Hexa-rotar UAV to carry out tactical attack operations in hazardous area, and reduce collateral damage.

## **1.3 OBJECTIVE**

1. To Design the architecture of possible version of missile, with input-output pair of execution of mission
2. To Design and Develop optimised Solid-Rocket Engine with on-par sub-systems of missile
3. To Design and analyse accessory systems of missile launch
4. Stability and Trajectory analysis, with a study of further improvement on accuracy using data obtained from launches using deep learning and machine learning models

## **1.4 PREVIOUS WORK**

- \* Squadron leader Ravi Raj during 2019-20 : Solid Rocket motor for the range of 1500 m with  $\Delta\theta < 18$  deg with thrust of 1476 N for 1.5 s burnout is designed with propellant composition shown in table 1.1, It is referred as Solid Rocket Motor (SRM) Version 1.0. It uses 68 mm Rocket Warhead manufactured by Indian Ordnance Factory, It is referred in the project as Weapon Payload (WP) version 1.0. This SRM V1.0 is attached to WP V1.0 and launched aurally from UCAV from altitude of 1000 m. [3]
- \* Niharika during 2020-21 : Literature Review on missile guidance system is studied, using OpenCV tracking implementation algorithms like BOOSTING, MIL, KCF, CSRT, MedianFlow, TLD, MOSSE. [4]
- \* Squadron leader Piyush Raj during 2019-20 : Integration of guided weapon on indigenously developed UAV is carried out, with design of Stores Management System (SMS), Avionic Bus Architecture Design with RS-485 Bus using MODBUS ASCII Protocol, with finalisation on Safty Critical system system integration. [2]

Ingredient	function	Wt%
HTPB	Fuel, Binder	10%
DOA	Plasticizer	3%
Ambilink	Cross-linking agent to ↑ tensile property	0.12%
PBNA	Improves aging characteristics	0.1%
TDI	Curing agent	0.73%
Al <sub>2</sub> O <sub>3</sub>	Fuel, Catalyst	0.1%
AP( course )	Oxidizer	51.5%
AP( Fine )	Oxidizer	34.4%
ACR	Modify Burn Rate	0.05%

Table 1.1: SRP Version 1.0 : Composite Propellant Composition

## 1.5 CURRENT RESEARCH AND WORKFLOW

1. Design of Solid Rocket motor V2.0 for the range of 2000 m with  $\Delta\theta < 45$  deg with thrust of 1000 N for 2.5 s burnout
2. 2500 gram Warhead payload profile, named as WP V2.0 and 2100 gram Warhead payload profile, named as WP V3.0
3. Optimising structural weight without compromising on performance : Carbon composite material selected for Missile frame, to provide same strength as that of aluminum alloy, with 50 percent less weight than aluminum alloy
4. Hydrotest for the material selected to validate the maximum pressure Rocket Motor case can handle
5. Selection of battery and rocket motor igniter
6. Trust calculation using the Pressure data obtained in firing of propellant using BEM
7. Canard Design
8. Canard mechanism design

9. Design of custom 2 axis gimbal for missile
10. Stability analysis of Missile
11. Design of Ground Launcher, Hand Launcher, Weapon Release System A and Weapon Release System B
12. Study on FPGA Architecture
13. Study on Sensors, Single Board Computers (SBC), csrt tracking with pan-tilt servo configuration
14. Trajectory Simulation and Prediction

The target of this project is to develop Vision Guided Aerially Launched Short Range Missile. Since the target missile development have many key variables which are to be in validated certainly to ensure precision, safety in its operation. The version control methodology is adopted, which in each stage gives conclusive data on the key variables tested in the version. Also, each version can be developed as a product with the limitation of version targeted capabilities, after certain iterations in design from the live-field data obtained during validation of certain version missile.

# CHAPTER 2

## ARCHITECTURE & DESIGN OF SYSTEM

### 2.1 DEVELOPMENT PROCESS

The missile development needs validation of various key variables, which is possible when we develop the final version through stages[9] (named versions), and achieving each version validates a major key variable that determines the trajectory of final version. [7]

In this chapter, Aerial platform refers to UCAV which is hosting the missile for launch from known lat-long, altitude, attitude.

### 2.2 VERSION 1

#### 2.2.1 Input

1. Target Latitude - Longitude
2. Latitude, Longitude, Attitude, Altitude of Aerial Launcher

#### 2.2.2 Logic

As we know the initial position and final position of the required trajectory, using Thrust vs Time data, considering drag, gravity,[5] we can calculate the required depression angle, with which the missile is to launched so as to follow the LOS trajectory. This is analogous to the propelled bullet, fired targeting the aim.

### 2.2.3 Details

S.No	Component	Calculated Mass (in gram)
1	Ignitor, CD Nozzle, Insulation	386
2	Electronics	152
3	Propellant	1200
4	Payload	2500
5	Carbonfiber Frame	519
6	Gimbal Shape	47
Total		4804

Table 2.1: Version 1 : Mass Distribution

1. No Gimbal, No Camera
2. Canards are fixed at zero angle of attack, act like stablisers. (These are placed so as the trajectory, field data collected during testing can be used for validation, and used in development of upcoming versions)
3. This has payload mass of 2500 gram and propellant mass of 1200 gram
4. It has battery and electronics necessary for the ignition, thus, the electronics mass calculated to be 152 gram
5. This Missile Version use SRM Version 2.0, and WP Version 2.0
6. Weapon Release System A (WRS-A) is used here which is estimated about 2.4 kg, thus, altogether mass of missile and WRS-A is about 7.2 kg
7. This is perfect to launch from hexarotor drone (UCAV) with minimum payload capacity of 8 kg

### 2.2.4 Validated Key Variable

1. This Launch validates Thrust Vs Time graph
2. This Launch validates our trajectory calculation, and the live data collected in each launch can be used for refining & validating our angle of depression required

at launch for the targeted range, using deep learning, thus having developing the trajectory prediction machine learning code

3. Validates Weapon Release System used
4. Validates UCAV Stability during operation of Launch

### 2.2.5 Output & Expected Trajectory

1. Fire and Forget
2. Target Lock before Launch
3. Launched at required angle of depression, for the targeted range via LOS trajectory

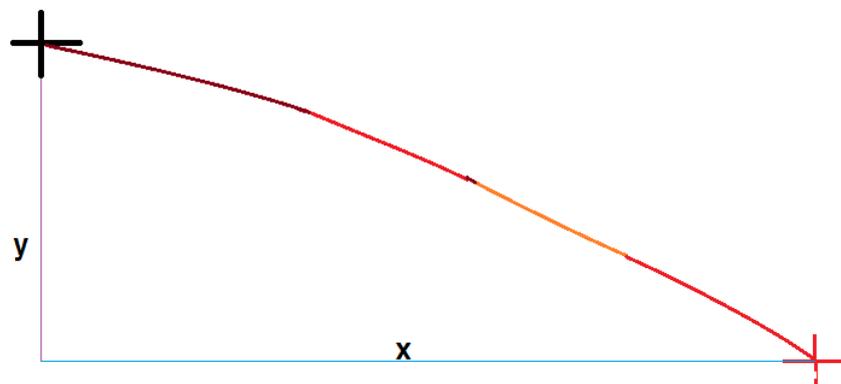


Figure 2.1: Expected LOS Trajectory

## 2.2.6 Architecture

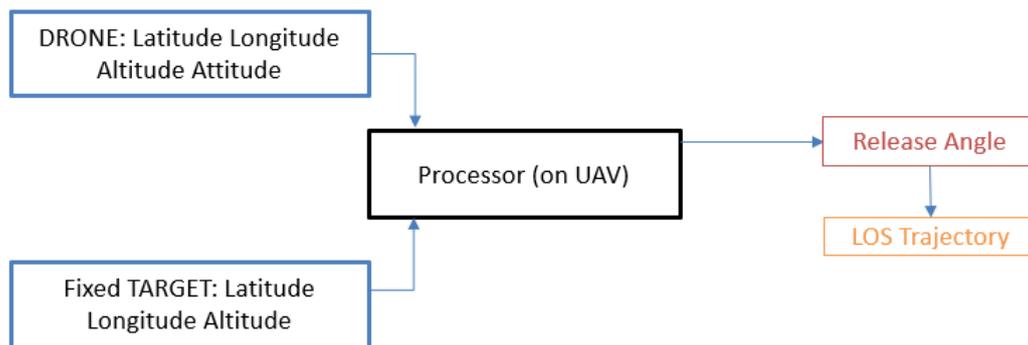


Figure 2.2: Architecture : Version 1

## 2.3 VERSION 2

### 2.3.1 Input

1. Target Latitude - Longitude
2. Latitude, Longitude, Attitude, Altitude of Aerial Launcher
3. Obstacle Latitude - Longitude, Height, Trajectory safe height required from obstacle height, Radius of obstacle, Safe Radial distance needed from obstacle

### 2.3.2 Logic

We know the initial position, final position and the obstacle location on the way, with its height, and respective required safe distances. Thus, with our precise Thrust vs Time data (obtained by cleaning the data using machine learning using live-field data obtained in testing of version 1), considering gravity, drag, canard control force and moment, we can calculate deflection angle required for canard during canard operation for duration of 0.5 second pre and post obstacle, so as to pitch up missile and pitch down missile, so as to escape the obstacle. The initial angle of depression of launch from aerial platform( Hexarotar UAV or fixed wing - VTOL) will be determined such a way that, missile reach the safe distance height coordinates of obstacle and can be able to perform turn maneuver.

Here, our trajectory is determined and pre-set before launch.[6] Thus, the PWM signals needed for the canard over duration of flight is determined before launch, and the data is fed to missile processor. Hence it is a open-loop control system. The trajectory path is said as Line of Sight - Obstacle Avoidance (LOS-OA) Trajectory

### 2.3.3 Details

S.No	Component	Calculated Mass (in gram)
1	Ignitor, CD Nozzle, Insulation	386
2	Electronics	191
3	Propellant	1200
4	Payload	2500
5	Carbonfiber Frame	519
6	Gimbal Shape	47
7	Servo Mechanism	148
Total		4991

Table 2.2: Version 2 : Mass Distribution

1. No Gimbal, No Camera
2. Servo mechanism attached to canards, and they take precise angle of attack, with accuracy of 0.1 degree by pairing it with our PWM servo controller
3. This has payload mass of 2500 gram and propellant mass of 1200 gram
4. The electronics constitutes of battery, servo controller, raspberry pi constitutes mass of 191 gram
5. This Missile Version use SRM Version 2.0, and WP Version 2.0
6. Weapon Release System A (WRS-A) is used here which is estimated about 2.4 kg, thus, altogether mass of missile and WRS-A is about 7.4 kg
7. This is perfect to launch from hexarotor drone (UCAV) with minimum payload capacity of 8 kg

### 2.3.4 Validated Key Variable

1. This launch validates the simulated values of aerodynamic properties of canard ( $C_L$  vs  $\alpha$  &  $C_D$  vs  $\alpha$ ) and helps to re-calibrate using machine learning the data obtained in field tests. This helps to accurately control the trajectory using canards, thus enabling us to go for closed loop feedback control in the next version of missile
2. With the validation of our calculations with real-time data obtained in this version, we can program to extend this version to be able to avoid multiple obstacles in its path.

### 2.3.5 Output & Expected Trajectory

1. Fire and Forget
2. Target Lock before Launch
3. Launched at required angle of depression, with a pre-set path for the targeted range, by travelling above obstacles via LOS-OA trajectory

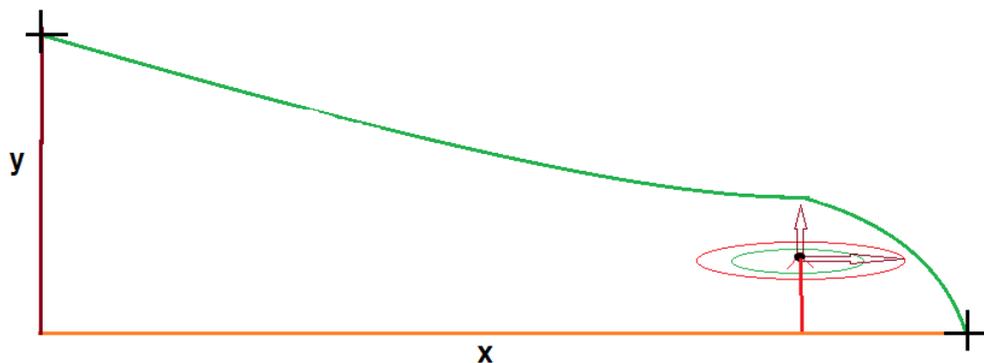


Figure 2.3: Expected LOS-OA Trajectory

## 2.3.6 Architecture

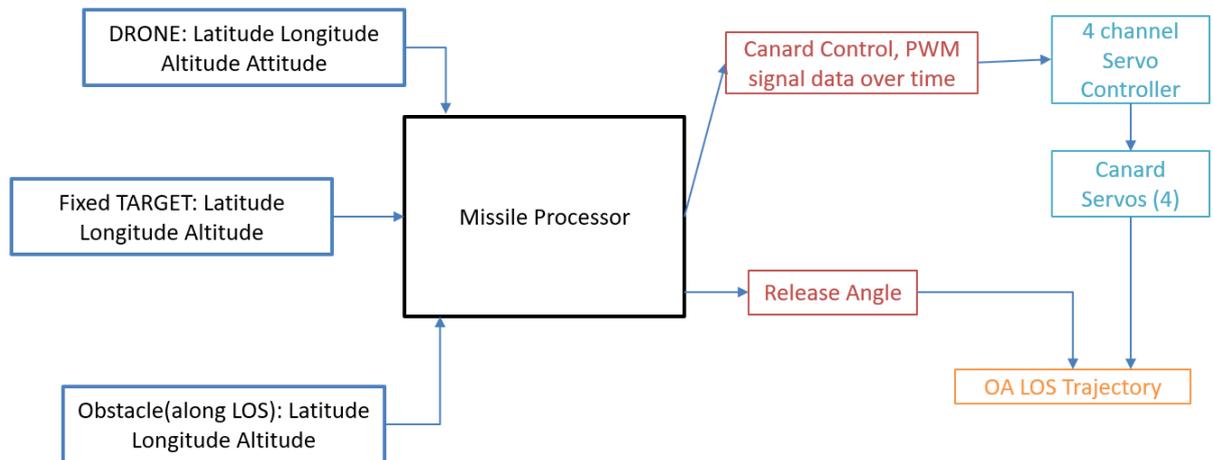


Figure 2.4: Architecture : Version 2

## 2.4 VERSION 3

### 2.4.1 Input

1. Latitude, Longitude, Attitude, Altitude of Aerial Launcher
2. Obstacles Latitude - Longitude, Height, Trajectory safe height required from obstacle height, Radius of obstacle, Safe Radial distance needed from obstacle
3. Exact location(Lat-Long) of **stationary target** at the time of firing or launch is needed

### 2.4.2 Logic

We know the stationary target, lat-long, and obstacles in the mid way, we can now provide software with minimum "y" above which missile path has to be planned. Here, we consider the refined precise data of instantaneous thrust, drag component, gravity effect, with possible disturbances in freestream wind, we can calculate best feasible trajectory and provide flight-path angle over time required to reach the target to missile processor on-board. This trajectory that is generated is called as Backup-Line-of-sight-Obstacle-Avoidance-Trajectory (BLOSOA Trajectory). [10] The missile is launched with calculated initial angle of depression in the intent to travel in BLOSOA path, however we

have a feedback system, an IMU attached to a stabilised gimbal (locked in the attitude of target, before launch). The instantaneous IMU signal and instantaneous PWM signal is fed to Trajectory Processor.[8] This feedback system, validates the current path with intended path, and send PWM signals to canard control surfaces, to achieve closed loop processing of real-time trajectory correction to approach the known stationary target with minimal miss-distance. Thus with use of the closed feedback system, to deal with real-time disturbances, we get into more realistic trajectory called as Line of sight Obstacle Avoidance Guided (LOS-OA-G) Trajectory.

### 2.4.3 Details

S.No	Component	Calculated Mass (in gram)
1	Ignitor, CD Nozzle, Insulation	386
2	Electronics	468
3	Propellant	1200
4	Payload	2100
5	Carbonfiber Frame	519
6	Gimbal + IMU	66
7	Servo Mechanism	148
Total		4887

Table 2.3: Version 3 : Mass Distribution

1. Gimbal is present, with IMU, without camera module
2. Servo mechanism attached to canards, and they take precise angle of attack, with accuracy of 0.1 degree by pairing it with our PWM servo controller
3. This has payload mass of 2100 gram and propellant mass of 1200 gram
4. The electronics constitutes of battery, servo controller, raspberry pi constitutes mass of 191 gram, and the servo mechanism system adds up to 148 grams

5. This Missile Version use SRM Version 2.0, and WP Version 3.0
6. Weapon Release System A (WRS-A) is used here which is estimated about 2.4 kg, thus, altogether mass of missile and WRS-A is about 7.4 kg
7. This is perfect to launch from hexarotor drone (UCAV) with minimum payload capacity of 8 kg

#### **2.4.4 Validated Key Variable**

1. Validation of Trajectory Processor, & efficiency of canards has to be validated
2. Closed feedback loop of Gimbal Stabilization board has to be tested and results are validated
3. Launch with angle of elevation has to be tested with validation
4. The switching from LOS-OA-G Trajectory to BLOSOA Trajectory in the emergency scenario (sensor blackout or) of sensor errors, has to be tested & validated

#### **2.4.5 Output & Expected Trajectory**

1. Fire and Forget
2. Target Lock before Launch
3. Launched at required angle of depression, for the targeted range via LOS-OA-G trajectory
4. Since it is closed loop guided, for a stationary target, we can have launch with angle of elevation attack a target at extended range, This will use LOS-OA-G trajectory system in descend phase of trajectory
5. This Version aims at stationary lat-long of target at the time of firing or launch, and also achieves less miss distance compared to previous versions

#### **2.4.6 Architecture**

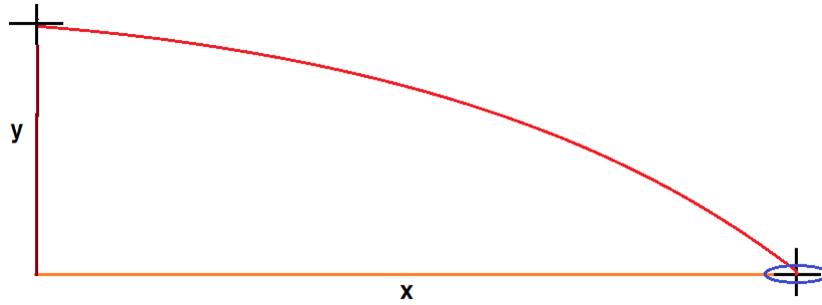


Figure 2.5: Expected LOS-OA-G Trajectory (launched with known angle of depression)

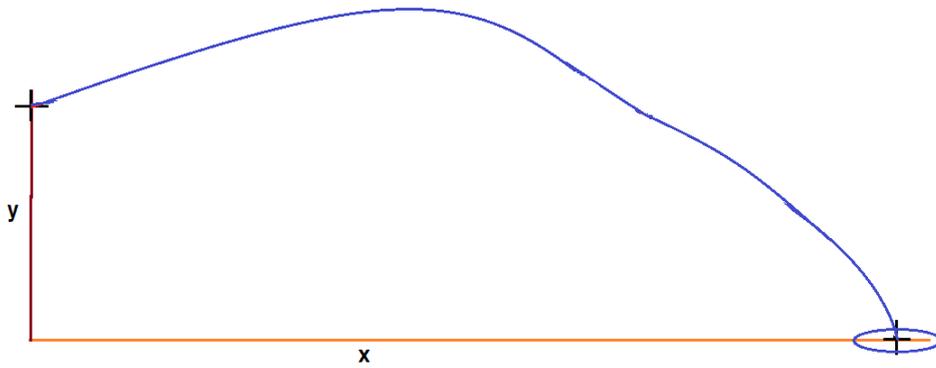


Figure 2.6: Expected LOS-OA-G Trajectory (launched with known angle of elevation)

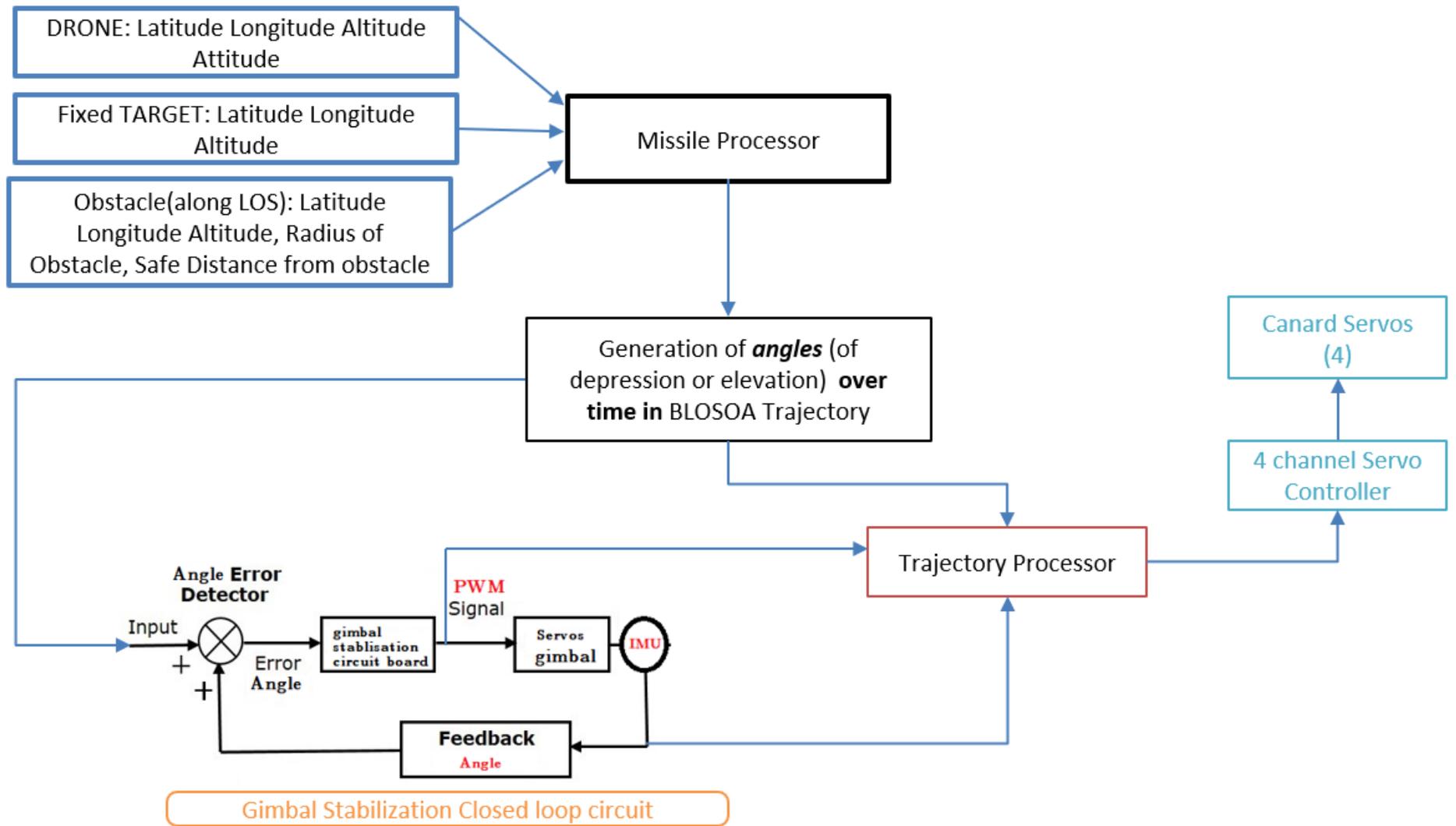


Figure 2.7: Architecture : Version 3

## 2.5 VERSION 4

This Version works for both stationary and moving targets.

### 2.5.1 Input

1. Latitude, Longitude, Attitude, Altitude of Aerial Launcher
2. Obstacle Latitude - Longitude, Height, Trajectory safe height required from obstacle height, Radius of obstacle, Safe Radial distance needed from obstacle
3. To Lock the Target, we need to select target image pixels in the camera view. Also we need to provide exact location(lat-long) of the target at the time of firing

### 2.5.2 Logic

We know the Initial Lat-long of the target, and its image pixels. We aim the missile camera towards the target during target lock, i.e., before firing the missile.

The Missile Camera which is mounted on 2 axis gimbal, will form a closed loop tracking system with the help of tracking processor and gimbal stabiliser processor. The working principle of this tracking is, the PWM signal is sent to gimbal servos, such a way that, position of the target is centered in the frame view of the camera. This is achieved[12] by dividing the frame in to 4 quadrants, and with the use of openCV csrt algorithm, we can get the object coordinates (x,y), and tracking[13] processor communicates (x,y) data to gimbal stabiliser (which has servo controller in it) processes and give correction PWM signal to servo 1 (pitch, yaw), servo 2 (roll), such that (x,y) tend to (0,0). This Feedback loop between camera, and gimbal servos is a closed loop (say CL-1) independent other systems of missile.

Thus, camera always aligned, and pointed towards the target, thus giving us orientation parameter, ie., the vector of the target, to which the missile has to align to. If we try to get this orientation data via gimbal tracking system, there is lag in this communication to

trajectory processor. Thus, we are getting this data signal (say "A") from IMU (say IMU-1) attached physically to camera, this way, we get data much faster speed[14], so the trajectory processor, compares the data signal (say "B"), with body fixed IMU (say, IMU-2), and calculates the PWM signal needed to send to canards, so as to reduce this error between IMU-1 and IMU-2. This Feedback loop between IMU-1, IMU-2, to make  $(A - B) \rightarrow 0$ , forms a independent closed loop system (say CL-2).

The criteria for convergence of this control system is, In a operation cycle(in order of 0.01 second or lower), The orientation signal (delta angle change) of IMU-1 has **to be higher** than the the same of IMU-2. It implies that the system has functional response, which is greater than the required response, [11]in missile orientation change during the operation. This system alters the missile path, and guides in such a way that the miss distance is least, compared to previous versions of missile, Thus we get Optical Guided Precision (OGP) Trajectory

If there is a camera signal blackout or the target is not detected in the image frames captured by camera, then, The missile[15] follows the BLOSOA Trajectory, so as to hit the area near to target, having a considerable miss distance.[16]

### 2.5.3 Details

S.No	Component	Calculated Mass (in gram)
1	Ignitor, CD Nozzle, Insulation	386
2	Electronics	534
3	Propellant	1200
4	Payload	2100
5	Carbonfiber Frame	519
6	Gimbal + IMU + Camera	97
7	Servo Mechanism	148
Total		4984

Table 2.4: Version 4 : Mass Distribution

1. Gimbal is present, with IMU and camera module. IMU is physically fixed behind camera.
2. Servo mechanism attached to canards, and they take precise angle of attack, with accuracy of 0.1 degree by pairing it with our PWM servo controller
3. This has payload mass of 2100 gram and propellant mass of 1200 gram
4. The electronics constitutes of battery, servo controller, raspberry pi constitutes mass of 191 gram, and the servo mechanism system adds up to 148 grams
5. This Missile Version use SRM Version 2.0, and WP Version 3.0
6. Weapon Release System A (WRS-A) is used here which is estimated about 2.4 kg, thus, altogether mass of missile and WRS-A is about 7.4 kg
7. This is perfect to launch from hexarotor drone (UCAV) with minimum payload capacity of 8 kg

### 2.5.4 Validated Key Variable

1. Tracking speed is validated in real time operation
2. Real time closed loop control system convergence is tested & validated

3. Miss distance is obtained and is verified with previous versions, to validate the least miss distance achievable.
4. This also validates our BLOSOA Trajectory effectiveness as it is entirely based on machine learning models of missile theoretical data, and field data. Also, The trend of value miss distance should decrease in each version after consecutive tests as our machine learning model evolves efficient over time, as we provide it with many instance field data.

### **2.5.5 Output & Expected Trajectory**

1. Fire and Forget
2. Target Lock before Launch
3. Launched at required angle of depression, for the targeted range via LOS trajectory

### **2.5.6 Architecture**

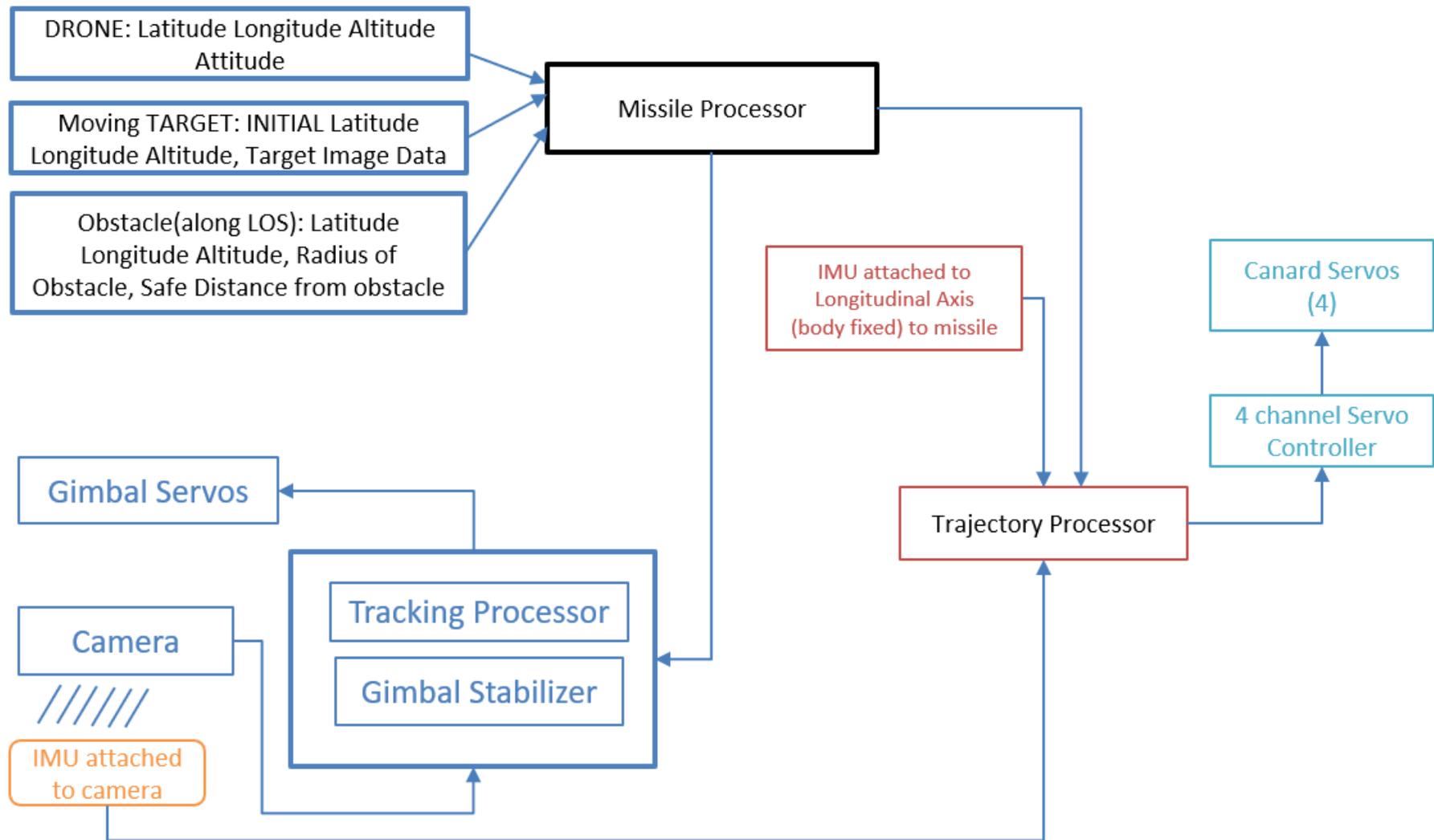


Figure 2.8: Architecture : Version 4

## 2.6 FRAME MATERIAL SELECTION

### Constraints Options

- \* **Nose** : Material at the Nose need to strong enough to sustain in the duration of flight path. Nose need to break when impulse hit to ground, i.e., Nose should not absorb greater impulse of sock at hit with ground or target. Thus we can choose 3D printing method, of most general material which suits the requirement, i.e., ABS plastic.[17]
- \* **Frame** : Missile frame need to be light weight with higher strength compared with any alloy of metal. Thus, we can use Epoxy Carbon Composite with manufacturing process suiting the needs. [18] [19] [20]
- \* **Rocket Engine** : Rocket Motor is a pressure vessel, should withstand high temperature of combustion chamber, of course with insulation, for a time of 15 seconds atleast, Also should be able to withstand pressure of 45 bar atleast. Thus, we can use Phenolic Carbon Composite. [21] [22]
- \* **CD Nozzle** : Graphite can be used in initial tests and validation. Once the design is proved, CD Nozzle can be made from Phenolic Carbon Composite, as we get same properties with light weight. [23] [24]



# CHAPTER 3

## DESIGN AND ANALYSIS OF MISSILE

### 3.1 ENGINE OF MISSILE (SOLID ROCKET DESIGN)

A solid rocket motor is a rocket engine that use solid as a propellant (fuel/oxidiser). Since solid-fuel rockets can remain in storage for a long time without much propellant degradation, and the fact that they almost always launch reliably, they have been frequently [25] used in military applications

The design parameters are interdependent, choice of propellant is dependent on thrust required, and thrust required is dependent [26] on range requirement. The structural mass is dependent on propellant mass, chamber pressure ( $p_c$ ) and temperature ( $t_c$ ). Thrust available depends on exit gas velocity ( $V_e$ ),  $V_e$  is dependent on nozzle design, nozzle design is dependent on choice of propellant. [27] [28]

To design the solid rocket motor, the following steps are followed :

1. Calculate Required Thrust and Burn-time for the requirement of mission. Also, Fix the targeted mass of propellant
2. Fix a propellant composition
3. Fix a chamber pressure and nozzle area ratio
4. Putting all these design criteria in CEA software we get values of various parameters for both Equilibrium flow and Frozen Flow (if applicable)
5. Since the flow in the nozzle is neither equilibrium nor frozen therefore we take the average of all the required quantities obtained from CEA. ( $C_F, P_e, T_c, C^*, \gamma$ )
6. Using all these values find out different parameters like  $U_e, T, A_t, A_e$  etc.,
7. Choose a type of nozzle and calculate its geometric properties

8. Calculate length of convergent portion
9. Then find out mass flow requirements for the given of solid rocket motor thrust for both fuel and oxidizer
10. Estimate mass flow rate, density, burn rate, burn surface area and all other relevant parameters
11. Choose a grain geometry for your motor and calculate the required parameters
12. Select suitable Material for chamber casing and calculate Wall thickness, volume of casing, mass of the motor, length, diameter etc
13. Select the Thermal insulation material and design for nozzle throat insulation / cooling [29] [30]

### 3.1.1 Composition of Propellant

In this iterative process, after referring database of the various propellant composition combinations in the in-house propellants developed by National Centre for Combustion Research and Development (NCCRD), the following propellant ingredients is finally considered optimally for the range of 2000 m with Launch depression angle less than 45 deg with thrust of 1000 N for 2.5 s burnout time. The propellant selected is a Composite Propellant because of its higher densities,[31] specific impulses, and a wider range of burn rates properties.[32]

Ingredient	function	Wt%
HTPB	Fuel,Binder	10%
DOA	Plasticizer	3%
Ambilink	Cross-linking agent to ↑ tensile property	0.28%
IPDI	Curing agent	0.72%
Al	Fuel	18%
AP( coarse )	Oxidizer	40.8%
AP( Fine )	Oxidizer	27.2%

Table 3.1: SRP Version 2.0 : Composite Propellant Composition

SRM Version 2.0 is the Ammonium perchlorate composite propellant (APCP). The composition of APCP can vary significantly depending on the application, intended burn characteristics, and constraints such as nozzle thermal limitations or specific impulse ( $I_{sp}$ ). The composition of APCP chosen is 68 % Ammonium Perchlorate (AP), 14 % Hydroxyl Terminated Polybutadiene (HTPB) ( which includes plasticizer, cross-linking agent, curing agent) and 18 % Aluminium by mass. AP acts as the oxidizer, Al as the fuel and HTPB as a binder and fuel.

### **3.1.2 CEA Analysis**

The chamber pressure is equal to 40 bar and Design Mach number of CD Nozzle is 3, thus nozzle area ratio ( $A_e/A_t$ ) is 4.23.

THEORETICAL ROCKET PERFORMANCE ASSUMING EQUILIBRIUM  
COMPOSITION DURING EXPANSION FROM INFINITE AREA COMBUSTOR

Pin = 580.2 PSIA  
CASE =

	REACTANT	WT FRACTION (SEE NOTE)	ENERGY KJ/KG-MOL	TEMP K
OXIDANT	NH4CL04(I)	1.0000000	-295529.716	300.000
FUEL	AL(cr)	0.5625000	44.802	300.000
FUEL	HTPB	0.4375000	-51800.000	300.000

O/F= 2.12500 %FUEL= 32.000000 R,EQ.RATIO= 1.921799 PHI,EQ.RATIO= 2.659239

	CHAMBER	THROAT	EXIT
Pinf/P	1.0000	1.7338	21.811
P, BAR	40.000	23.070	1.8339
T, K	3284.23	3098.36	2327.00
RHO, KG/CU M	4.0063 0	2.4678 0	2.6622-1
H, KJ/KG	-1844.23	-2376.08	-4398.41
U, KJ/KG	-2842.66	-3310.95	-5087.28
G, KJ/KG	-33642.5	-32374.7	-26928.6
S, KJ/(KG)(K)	9.6821	9.6821	9.6821
M, (1/n)	27.350	27.556	28.086
MW, MOL WT	25.268	25.365	25.685
(dLV/dLP)t	-1.01518	-1.01146	-1.00179
(dLV/dLT)p	1.2853	1.2247	0.0000
Cp, KJ/(KG)(K)	3.7669	3.4131	0.0000
GAMMA <sub>s</sub>	1.1340	1.1378	0.9982
SON VEL,M/SEC	1064.0	1031.4	829.2
MACH NUMBER	0.000	1.000	2.726

PERFORMANCE PARAMETERS

Ae/At	1.0000	4.2300
CSTAR, M/SEC	1571.6	1571.6
CF	0.6562	1.4381
Ivac, M/SEC	1937.8	2565.0
Isp, M/SEC	1031.4	2260.2

Figure 3.1: CEA Analysis

The performance analysis assuming frozen flow is not shown here. It is due to the fact that addition of Aluminium to the propellant makes it a two phase problem due to presence of Aluminium in gases and so the above parameters cannot be obtained by Chemical Equilibrium Analysis software assuming frozen flow. Hence the further analysis is being done assuming equilibrium flow in the nozzle, though in reality the flow is neither equilibrium nor frozen.

Thrust required is  $F = 1000N$  for the trajectory of 2000 m

$$\mathbf{F} = \eta \cdot \lambda \cdot P_c A_t C_F \quad (3.1)$$

Where  $\eta$ -efficiency factor (0.95),

$\lambda$  - divergence loss factor,

$$\lambda = \frac{1 + \cos \alpha}{2} = 0.9531$$

(for  $\alpha = 25$  deg)

Since,

$$C_F = 1.43$$

$$P_c = 4 \text{ MPa}$$

Throat Area,

$$A_t = \frac{F}{\eta \cdot \lambda \cdot P_c \cdot C_F} = 0.00019 \text{ m}^2$$

Throat diameter,

$$d_t = \sqrt{\frac{A_t}{\pi/4}} = 0.0156 \text{ m} = 1.56 \text{ cm}$$

Since

$$\frac{A_e}{A_t} = 4.23$$

Exit Area,

$$A_e = 0.00082 \text{ m}^2$$

Exit diameter,

$$d_e = \sqrt{\frac{A_e}{\pi/4}} = 0.0322 \text{ m} = 3.22 \text{ cm}$$

Mass flow rate,

$$\dot{m} = \frac{P_c A_t}{c^*} = 0.4914 \text{ kg/s}$$

Thrust equation gives

$$\mathbf{F} = \eta * \lambda * (\dot{m}U_e + \mathbf{A}_e (\mathbf{P}_e - \mathbf{P}_a))$$

Exhaust velocity,

$$U_e = I_{sp} - \frac{A_e}{\dot{m}} (P_e - P_a) = 2124.4 \text{ m/s}$$

Vacuum  $I_{sp}$ ,

$$I_{vac} = 2565 \text{ Ns/kg}$$

Vacuum thrust,

$$F_{vac} = \eta \cdot \lambda \cdot (\dot{m} \cdot I_{vac}) = 1141 \text{ N}$$

### 3.1.3 Method of Characteristics

Design of CD Nozzle diverging portion is done using method of characteristics.

$$\text{Pressure Ratio} = \frac{\text{Outside Pressure}}{\text{Chamber Pressure}}$$

$$\text{Temp Ratio} = (\text{Pressure Ratio})^{\frac{\gamma - 1}{\gamma}}$$

$$\text{Critical (Throat) Temp} = \frac{(2 \cdot \gamma \cdot R \cdot \text{Chamber\_Temp})}{\gamma - 1}$$

$$\text{Critical (Throat) Pressure} = \left( \left( \frac{2}{\gamma + 1} \right)^{\frac{\gamma}{\gamma - 1}} \right) \cdot \text{Chamber\_Pressure}$$

$$\text{Critical (Throat) Velocity} = \sqrt{\frac{(2 \cdot \gamma \cdot R \cdot \text{Chamber\_Temp})}{\gamma + 1}}$$

$$\text{Exit Velocity} = \sqrt{\text{Throat Temp} (1 - \text{Temp Ratio})}$$

$$\text{Exit Temp} = (\text{Chamber } T) \cdot \left( \frac{P_{\text{exit}}}{P_{\text{chamber}}} \right)^{\frac{\gamma - 1}{\gamma}}$$

$$\text{Exit Sound Speed} = \sqrt{\gamma \cdot R \cdot \text{Exit Temp}}$$

$$\text{Exit Mach} = \frac{\text{Exit Velocity}}{\text{Exit Sound Speed}}$$

$$PM = \sqrt{\frac{\gamma + 1}{\gamma - 1}} \cdot \text{atan} \sqrt{\frac{\gamma - 1}{\gamma + 1} \cdot (M^2 - 1)} - \text{atan} \sqrt{M^2 - 1}$$

$$\text{Max Angle} = \frac{1}{2} \cdot \{PM(\text{Exit Mach})\}$$

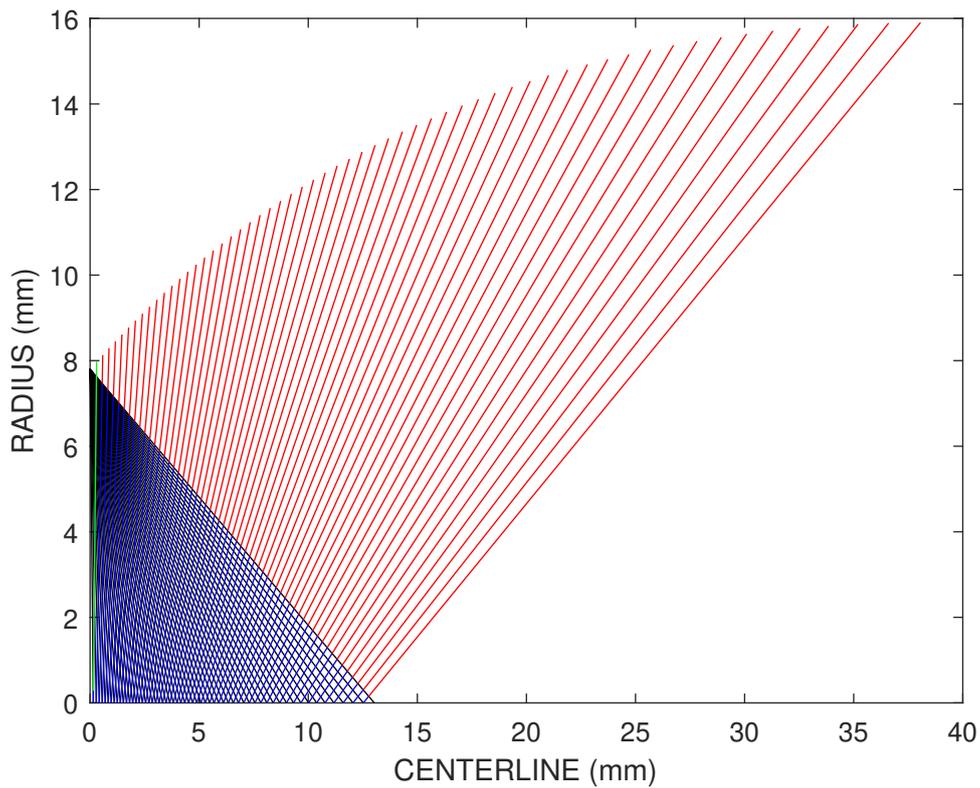


Figure 3.2: CD Nozzle : Diverging portion

$$\text{Angle Increment} = 2 \cdot ((90 - \text{Max Angle}) - \text{fix}(90 - \text{Max Angle}))$$

Matlab code is attached in Appendix B.1

### 3.1.4 Characteristics of Propellant

Density of propellant

$$\rho_p = \frac{1}{\frac{f_a}{\rho_a} + \frac{f_b}{\rho_b} + \frac{f_c}{\rho_c}} \quad (3.2)$$

Where a, b and c represents the AP, HTPB and Al respectively

Propellant constituent	Ammonium Perchlorate	HTPB	Aluminium (crystalline)
Density ( <b>kg/m<sup>3</sup></b> )	1950	920	2700
Mass fraction	0.68	0.14	0.18

Table 3.2: Density and mass fraction of oxidizer and fuel

$$\rho_p = 1761.932 \text{ kg/m}^3$$

Mixture ratio (O/F ratio) obtained from CEA is equal to 2.125

$$\dot{m}_{\text{ox}}/\dot{m}_{\text{f}} = 2.125$$

$$\dot{m} = \dot{m}_{\text{ox}} + \dot{m}_{\text{f}} = 0.4914 \text{ kg/s}$$

Solving above equations, we get

$$\dot{m}_{\text{f}} = 0.157 \text{ kg/s}$$

$$\dot{m}_{\text{ox}} = 0.334 \text{ kg/s}$$

where,  $\dot{m}_{\text{ox}}$  – mass flow rate of oxidizer

$\dot{m}_{\text{f}}$  – mass flow rate of fuel

Burn rate is given by, [32]

$$\dot{r} = aP_c^n$$

The values of a and n are obtained as 6.7 mm/s(atm)<sup>n</sup> and 0.42 respectively.

The a and n values obtained are calculated at 70 bar critical pressure and so the above relation modifies to the following form [32]

$$\dot{r} = a_{70} \left( \frac{P_c}{70} \right)^n = 5.29 \text{ mm/s}$$

Burn area is calculated from the following relation

$$A_b = \frac{\dot{m}}{\rho_p \dot{r}} = 0.0526 \text{ m}^2$$

### 3.1.5 Grain Design

Neutral burning propellant configuration would be a preferred configuration since the pressure-time variation shows a constant pressure. Hence a star configuration has been selected to achieve neutral burning of the propellant.

No. of star points = 6

Angle between two star arms,  $\theta = \theta_{n, \text{neutral}} = 67^\circ$

Area of port,

$$A_p = nl^2 * \frac{1}{\frac{1}{\tan(\frac{\pi}{n})} + \frac{1}{\tan(-\frac{\pi}{n} + \frac{\theta}{2})}} \quad (3.3)$$

$$A_p = 0.3318l^2$$

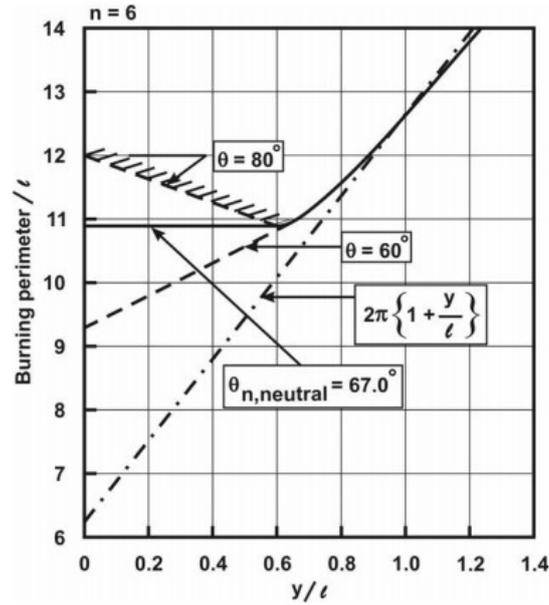


Figure 3.3: The normalized perimeter with burning distance for  $n = 6$  [32]

The extent upto which neutral burning can be achieved is given by the relation

$$\frac{y}{l} = 0.6$$

Where,  $l$  is the length of the star point from the centre of star grain geometry

$y$  is the web thickness (minimum thickness of grain between port and wall)

If the ratio goes more than 0.6, progressive burning comes into action replacing neutral burning.

From the above plot, at  $y/l = 0.6$ ,

burning perimeter( $P$ ) /  $l = 10.9$

$P = 10.9l$

Length of grain,

$$L = \frac{A_b}{P} = \frac{0.00483}{l}$$

Diameter of grain,

$$D = 2 \cdot (y + l) = 3.2l$$

Mass of propellant

$$m_p = \dot{m} \cdot t_b = 1.2285 \text{ kg}$$

Assuming 6% sliver loss (as star configuration has sliver loss of 4-8%),

$$m_p = 1.06 \cdot 1.2285 = 1.3 \text{ kg}$$

Volume of Propellant,

$$V_p = \frac{m_p}{\rho_p} = 0.000739$$

The material selected is carbon composite with 110 MPa yield stress, which is fabricated using compression mould process.

Thickness of wall can be calculated from circumferential stress relation

$$t = \frac{pd_i}{2\sigma} \quad (3.4)$$

Here factor of safety used is equal to 1.4 and so permissible stress,  $\sigma = \frac{\sigma_y}{1.4}$

Diameter of Grain,

$$D = 64.5 \text{ mm}$$

Length of grain,

$$L = \text{length of grain} = 243.46 \text{ mm}$$

thickness,

$$t = \frac{40 \cdot 100000 \cdot 64.5 \cdot 10^{-3}}{2 \cdot \frac{110 \cdot 10^6}{1.4}}$$

$$t = 0.00164 \text{ m} = 1.64 \text{ mm} \quad (3.5)$$

## **Liner**

Liner serves an important function to ensure good bond interface between the propellant and insulation at wall. It also inhibits burning so that propellant only burns at the unlined surfaces. In general, the liner material is the bonding matrix or fuel material in the propellant. This insures a good propellant to liner bond.

The liner material which can be used is HTPB binder cured with Isophorone Diisocyanate (IPDI). In general, thinner liners produce greater bond strengths and increase the propellant loading fractions. So, the thickness of thin liner we use is around (0.127 mm).

## **Stress Release Boots**

Propellant grains are cast at elevated temperatures and allowed to cool and polymerize. The resultant shrinkage develops residual stresses in the propellant charge that are

not relieved by plastic deformation. These stresses can result in bond failure between propellant and liner or case to liner. If liner or the bond is having high strength, the propellant charge will probably fail by cracking down the base of the star point. The result can be a catastrophic failure due to the increased burning surface area.

A technique to overcome this weakness is called the "stress release boot". The boot is fabricated as two individual items and bonded out at the maximum diameter area. Each piece is made from a rubbery flexible material.

### **3.1.6 Propellant mixing**

A plastic beaker of 250 ml is taken and placed on a weighing balance. The balance is then reset to zero. HTPB is poured slowly into the beaker up to the required weight. The weighing balance is again reset to zero with beaker still on the balance tray. Then DOA is poured drop by drop using a dropper and followed by TDI using a glass stirrer rod. The ingredients are well mixed with hands by means of a spatula. The beaker is again kept on the weighing balance with the wetted spatula and the balance is again set to zero. Ambilink and Nonax-D are added to the mixture followed by the addition of coarse and fine AP powder as per the formulations above. The mixture is again hand mixed for 15 minutes and then poured into the propellant mixer. The mixer, shown in figure 3.4, is developed by IIT madras and has a capacity of 200 grams. An evacuation pump is connected to the mixer and the propellant is mixed for an hour within the mixer. Then the propellant is appeared as smooth and glossy, which indicates complete wetting of all the solid surfaces by the binder.

### **3.1.7 Propellant casting**

The propellant slurry is taken out from the mixer and poured into the Teflon casting cup. A cylindrical shaped[36] casting cup (figure 3.7) with one end closed and having a mandrel in the centre is used. Before the propellant is poured to the casting cup, very thin layer of silicon oil is applied on the inner surface of the casting cup and mandrel so



Figure 3.4: Propellant Mixer

that when the cast grain needs to be removed, it would come out easily. The casting cup is then inserted into the casting chamber. The schematic drawing of the casting chamber along with the actual casting chamber is shown in figure 3.5 and 3.6 respectively. The outside diameter of the casting cup is the same as of the internal diameter of the casting chamber. A vacuum pump is connected to the casting chamber in order to remove the air trapped in the propellant. Hot water at 50 °C is circulated in the annular region of the casting chamber to decrease the viscosity[34] of the propellant during casting. An air-tight piston connected to the plunger is inserted into the chamber and the top cap is screwed to the chamber at the top end. The hot water circulation in a jacket surrounding the chamber and vacuum in the chamber are maintained for about 30 minutes. After half an hour of evacuation, the plunger is pressed and the propellant slurry is compressed. A mass of 2-3 kgs is kept on the top of the plunger for one day. After one day, the bottom plate is removed and the cast propellant along with the casting cup is taken out.[35] This is cured in an oven at a temperature of 60 °C for 7 days. After 7 days, the propellant grain is taken out of the casting cup. the propellant grain and its dimensions are shown in figure 3.8 and 3.9 respectively.[37]

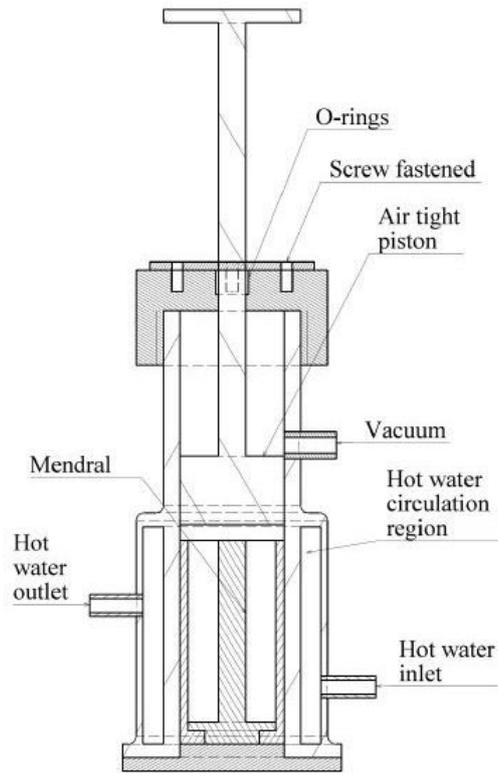


Figure 3.5: schematic drawing of casting chamber



Figure 3.6: casting chamber



Figure 3.7: propellant in casting cup

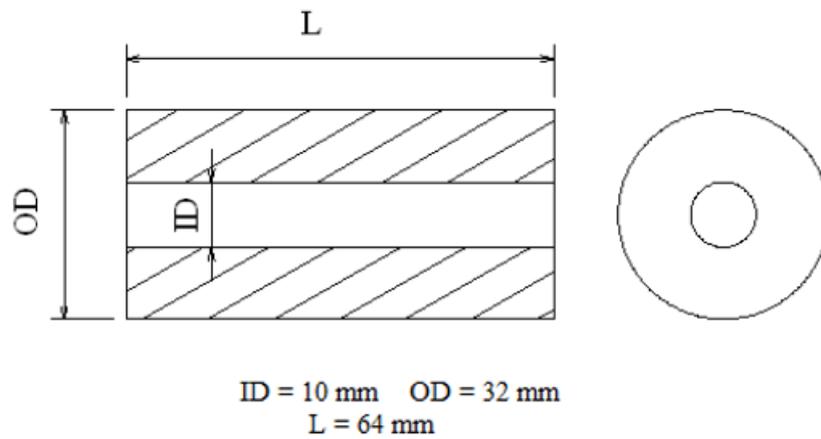


Figure 3.8: propellant dimensions



Figure 3.9: Propellant Grain

### 3.1.8 Ballistic evaluation motor (BEM)

The ballistic evaluation motor (BEM) test is to measure the motor performance parameters under actual operating conditions. The complete assembly drawing of the motor is shown in figure 3.10 below.

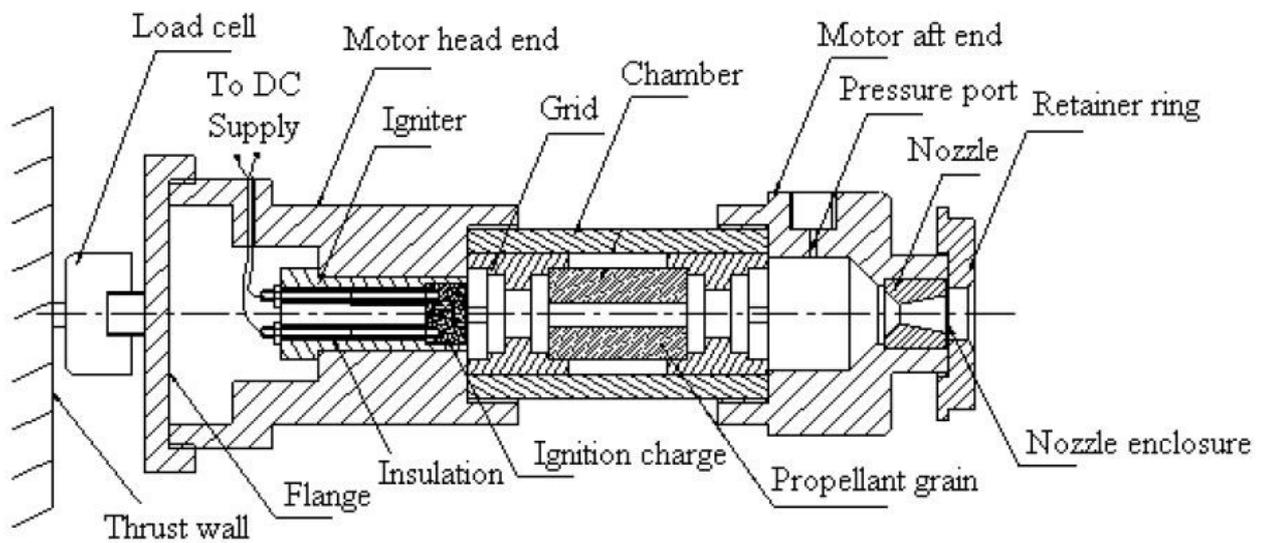


Figure 3.10: Ballistic evaluation motor assembly drawing

The main motor parts and their functions are tabulated in table 3.3

S. No.	Motor part	Function
1	Load cell	Thrust measurement
2	Motor head end	Holds igniter, connection between combustion chamber and load cell
3	Combustion chamber	Holds propellant, provides space for combustion
4	Grid	Holds the propellant in horizontal axis in combustion chamber
5	Motor aft end	Provides space for pressure port and nozzle
6	Nozzle	Expansion of combustion products
7	Retainer ring	Secures nozzle

Table 3.3: Motor parts and their functions

### 3.1.9 Ignition system

The igniter consists of a metallic body through which two tungsten electrodes passed inside covered with hylum insulation. Gunpowder is used as the ignition charge. This is a mixture of potassium nitrate, sulphur and carbon in the ratio of 80:15:5 by mass. Ignition charge is placed in a small paper packet and nichrome wire is passed through it.[38] The ends of the nichrome wire are connected to the electrodes of the igniter. The other end of the igniter is connected to a 24V DC power supply. When the power is supplied to the igniter, the nichrome wire gets heated and thus the ignition charge is fired. Figure 3.11 shows the igniter used in BEM.

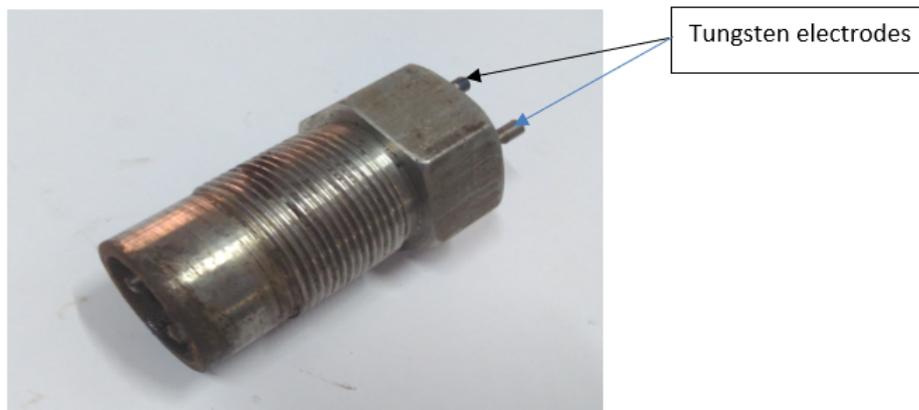


Figure 3.11: Igniter for BEM

### 3.1.10 Testing of BEM

Once the motor is ignited, the flame and hot gas are produced due to the firing of the igniter charge. This flame spreads on the propellant surface, ignites the propellant in close proximity and propellant combustion is commenced. A piezo-resistive transducer connected to the aft end of the motor measures the pressure rise during the combustion. The thrust developed is recorded by the load cell, which gets compressive load in between the thrust wall and motor aft end [39] during firing. Initial port diameter of the propellant and nozzle throat diameter are 10 mm and 9 mm respectively, so the area ratio 1.24. The transducer, load cell and other accessories are connected to the system through data acquisition system. The assembled BEM is shown in Figure 3.12



Figure 3.12: Assembled BEM

### 3.1.11 BEM Chamber design

The motor chamber is a hollow cylinder made up of stainless steel grade 316. The inner diameter of the chamber is 50 mm and the wall thickness provided is 10 mm. Assuming the maximum motor pressure to be 200 bar, the minimum chamber thickness is calculated as follows: [39]

The hoop stress formula a thin walled pressure vessel is given as,

$$\sigma_{\theta} = \frac{P_c \times D_c}{2 \times t_{\text{wall}}} \quad (3.6)$$

where

$P_c$  = chamber pressure,

$D_c$  = diameter of the chamber,

$t_{\text{wall}}$  = wall thickness.

The yield strength of steel is 200 MPa and the minimum wall thickness for a 20 MPa, 50 mm inner diameter of the chamber with a factor of safety of 3 is calculated as,

$$t_{\text{wall}} = \frac{(200 \times 10^6) \times (50 \times 10^{-3})}{2 \times 300 \times 10^6} \times 3 = 5 \times 10^{-3} \text{ m} \quad (3.7)$$

Since the provided wall thickness is 10 mm, which is more than the required thickness, the design is safe.

### 3.1.12 BEM Thread Calculation

External threads of 14 turns per inch (tpi) are provided at both ends of the chamber, and these threaded joints connect the motor head end and aft end. They are made up of mild steel of yield strength 200 MPa, and the force exerted by chamber pressure on these threads is found as

$$F_p = \frac{\pi}{4} \times D_c^2 \times P_c \quad (3.8)$$

The shear force that the threads can withstand is,

$$F_{\text{shear}} = \pi \times d \times m \times \frac{P}{2} \times \sigma_{\text{shear}} \quad (3.9)$$

where,

$d$  = pitch circle diameter of thread

$m$  = number of threads

$$\sigma_{\text{shear}} = \frac{\sigma_{\theta}}{2} \quad (3.10)$$

Equating the pressure force and shear force, we get  $F_p = F_{\text{shear}}$

$$m = \frac{P_c \times D_c^2}{4 \times d \times \frac{p}{2} \times \sigma_{\text{shear}}} \quad (3.11)$$

$$m = \frac{200 \times 10^6 \times (50 \times 10^{-3})^2}{4 \times 68.8218 \times \left(\frac{1.814}{2} \times 10^{-3}\right) \times 33.33 \times 10^2} = 6.002 \quad (3.12)$$

That is, there should be approximately 6 threads, and since the chamber is provided with 11 threads, the design is safe.

### 3.1.13 Burn rate calculation

Let the propellant burn by a distance  $y$  from all the exposed surfaces in time  $t$ . The burnt volume of propellant grain is indicated by the shaded area in Figure 3.13.

$OD$  = outer diameter of the propellant grain,

$ID$  = inner diameter of the propellant grain

$L$  = length of the propellant grain.

Then, the present exposed area is calculated as follows. The end surface area is given by,

$$Ab(y) \text{ end} = 2 \left(\frac{\pi}{4}\right) [(OD - 2y)^2 - (ID + 2y)^2] \quad (3.13)$$

$$Ab(y) \text{ lateral} = \pi(L - 2y)[(OD - 2y) + (ID + 2y)] \quad (3.14)$$

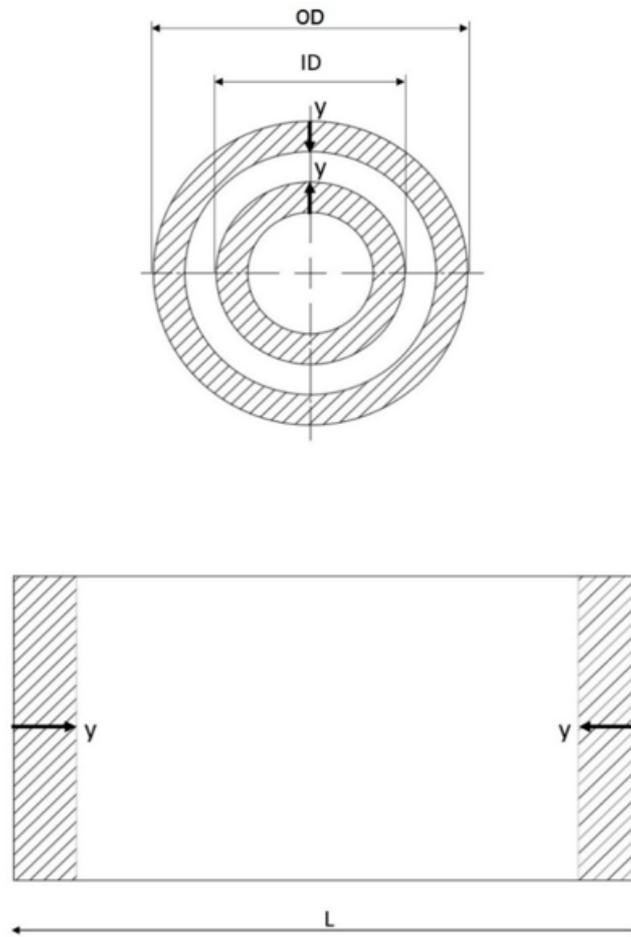


Figure 3.13: Propellant grain burning profile

$$Ab(y) = 2 \left( \frac{\pi}{4} \right) [(OD - 2y)^2 - (ID + 2y)^2] + \pi(L - 2y)[(OD - 2y) + (ID + 2y)] \quad (3.15)$$

$$= \left( \frac{\pi}{2} \right) (OD + ID)(OD - ID + 2L - 8y)$$

The remaining volume of the propellant with respect to burnt distance  $y$  is given by

$$\begin{aligned}
V_p(y) &= \left(\frac{\pi}{4}\right) [(OD - 2y)^2 - (ID + 2y)^2] (L - 2y) \\
&= \left(\frac{\pi}{4}\right) (OD + ID)(OD - ID - 4y)(L - 2y)
\end{aligned}$$

The volume of the propellant consumed up to time t is given by

$$\Delta V_p = \frac{\int_0^t (P_c \times A_t \times dt)}{\rho_p \times C^*} \quad (3.16)$$

$A_t$  = nozzle throat area,

$\rho_p$  = propellant density,

$C^*$  = characteristic velocity,

$$C^* = \frac{\int_0^{t_b} (P_c \times A_t \times dt)}{m_p} \quad (3.17)$$

Where  $t_b$  = total burning time.

The total volume of the propellant at any time = volume consumed + volume remaining

$$V = \Delta V_p + V_p(y) \quad (3.18)$$

Consider the mass balance equation

$$\rho_p \times A_b \times r_0 = P_c \times \frac{A_t}{C^*} + \frac{d}{dt} (\rho_0 V_0) \quad (3.19)$$

For steady state



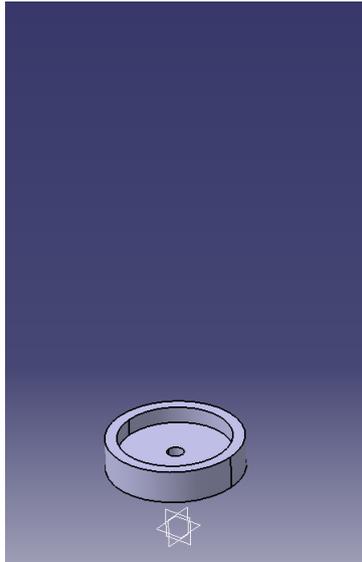


Figure 3.15: Full Scale Mandrel : Base Plate

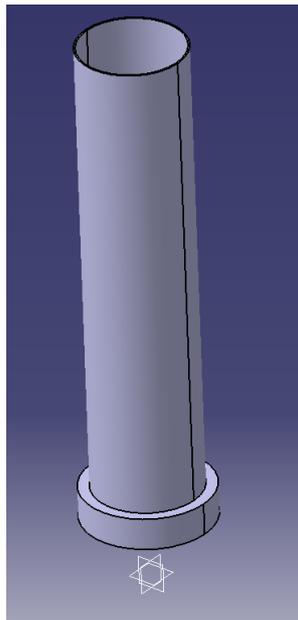


Figure 3.16: Mandrel Assembly

### 3.1.15 Nozzle design for BEM to test SRP V3

The nozzle is designed using Chemical Equilibrium Analysis (CEA) software, in order to expand the propellant combustion gas isentropically from a chamber pressure of 20 bar to atmosphere. The amounts of fuel and oxidizer and pressure ratio are fed in as input for

the analysis. The input and output files of CEA analysis are attached as appendix. The important parameters obtained is tabulated in table 3.4 and the fabricated graphite nozzle is shown in fig.5. The nozzle throat is calculated from equation (3.22) as the propellant burning rate is known from window bomb analysis.

Parameter	Chamber	Throat	Exit
Temperature T(K)	3253.85	3071.25	2327.00
Pressure P(bar)	20.000	11.529	1.0000
Mach number	0.000	1.000	2.687
Area ratio $A_e/A_t$	-	1.0000	3.9467

Table 3.4: BEM Nozzle Dimensions

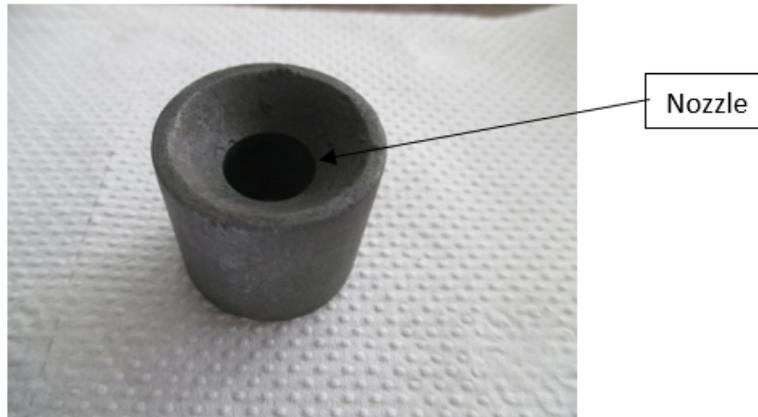


Figure 3.17: Graphite Nozzle

### 3.1.16 Grain Dimensions

Two different grain geometry are used in the present study. Their dimensions are given by table 3.5. Grain 1 is a cylindrical grain without inhibition. The burning unrestricted and the profile is regressive. Whereas the grain 2 is a bigger grain and the outer surface and end surfaces are inhibited. Thus the burning is inside out only and the profile is a progressive one. A mixture of HTPB, TDI and carbon black in the ratio 71.43:7.14:21.43

respectively is used as the inhibitor. The mixture is applied on propellant surface about 1.5 mm thick and cured for one day. An aluminized and non-aluminized grain of geometry 1 is shown in fig.3.18 and an inhibited grain 2 inside the motor chamber is shown in fig. 3.19

Dimensions	Grain
ID (mm)	10
OD (mm)	32
Length (mm)	64
Weight (g)	80

Table 3.5: Grain Dimensions



Figure 3.18: Non-aluminized (left) and aluminized (right) propellant grain 1

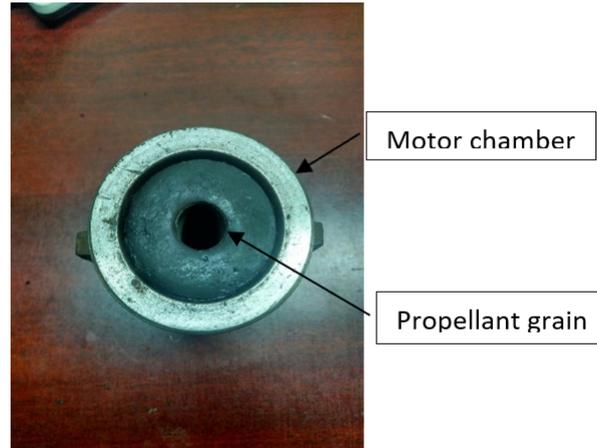


Figure 3.19: Inhibited propellant grain 2

### 3.1.17 Firing & P vs t graph

The composition of Solid Rocket Propellant V 3.0 chosen is 70 % Ammonium Perchlorate (AP), 15 % Hydroxyl Terminated Polybutadiene (HTPB) ( which includes plasticizer, cross-linking agent, curing agent) and 15 % Aluminium by mass. AP acts as the oxidizer, Al as the fuel and HTPB as a binder and fuel.

Ingredient	function	Wt%
HTPB	Fuel,Binder	11%
DOA	Plasticizer	2.8%
Ambilink	Cross-linking agent to ↑ tensile property	0.38%
IPDI	Curing agent	0.82%
Al	Fuel	15%
AP( course )	Oxidizer	41.3%
AP( Fine )	Oxidizer	28.7%

Table 3.6: SRP Version 3.0 : Composite Propellant Composition

BEM firing was performed for propellant combination shown in the table 3.6. The Result

data is shown below in figure 3.20

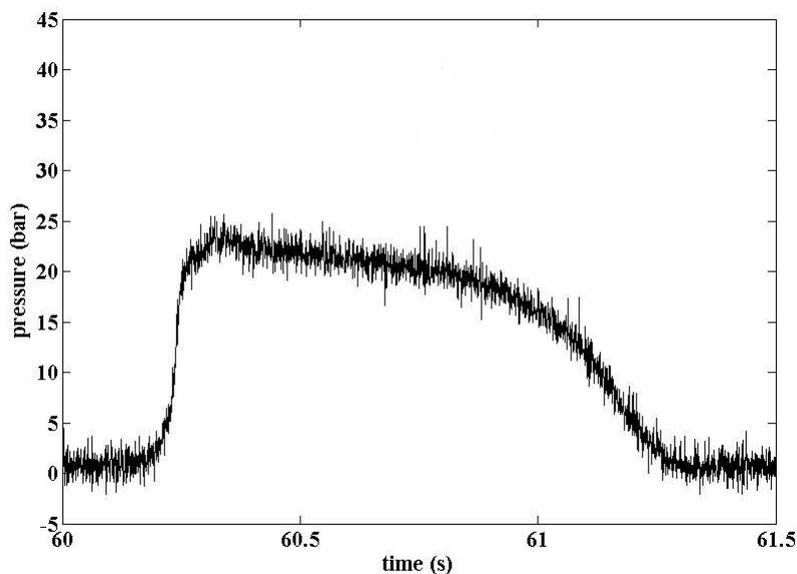


Figure 3.20: P vs T graph

### 3.1.18 Thrust Calculation

We can calculate Thrust vs time graph, provided with Pressure vs time graph.

From P vs t graph, we can get chamber pressure at a time step, we know the back pressure is always equal to atmospheric pressure i.e., 101325 Pa. We also know the CD Nozzle Area ratio i.e.,  $A/A_{star}$  through which the flow passing through.

Thus, For a given Pressure Ratio ( Chamber Pressure / Back Pressure ), and Area Ratio ( Exit Area / Throat Area ), (having known the temperature at chamber, nozzle exit) . There is only one possible flow. This flow can be calculated at each time step, using a Matlab code, for the calculation of thrust at each time step, code is given in appendix

Working of Thrust Calculator code

1. For the given Area Ratio, Code calculates subsonic mach number, supersonic mach number. These Mach number gives pressure ratio, as both cases are isentropic.

When Input the back pressure, we get the range of chamber pressures, below which we get subsonic flow, above which we get under-expanded flow

2. The intermediate chamber pressure, that forms NS at exit plane is calculated, using normal shock at exit plane case
3. Thus we have pressure divisions as follows in table 3.7. Using which each case, we find exit mach number and exit pressure using gas dynamics

ID	Range of Chamber Pressure	Case
1	0 to P01	Subsonic
	P01	Chocking point
2	P01 to P0i	Normal Shock in Diverging portion
	P0i	Normal Shock at diverging portion of CD Nozzle
3	P0i to P02	Oblique Shock, Over Expanded, ( $P_e < P_b$ )
	P02	Perfectly expanded, Design Mach number case (exit mach number = design super sonic mach number)
4	P02 to infinity	Under expanded ( $P_e > P_b$ )

Table 3.7: Pressure Calculation

From CEA analysis of the propellant composition, we can know the temperature at exit, chamber temperature, molecular weight (which can be used to calculate gas constant). Applying these data at each instant in the Thrust Formula, we get Thrust at an instant.

Example Pressure vs Time graph obtained from Propulsion Lab shown in figure 3.21, to find Thrust vs Time graph. The Matlab code runs, once data is fed, and we get Thrust vs Time graph as shown in figure 3.22

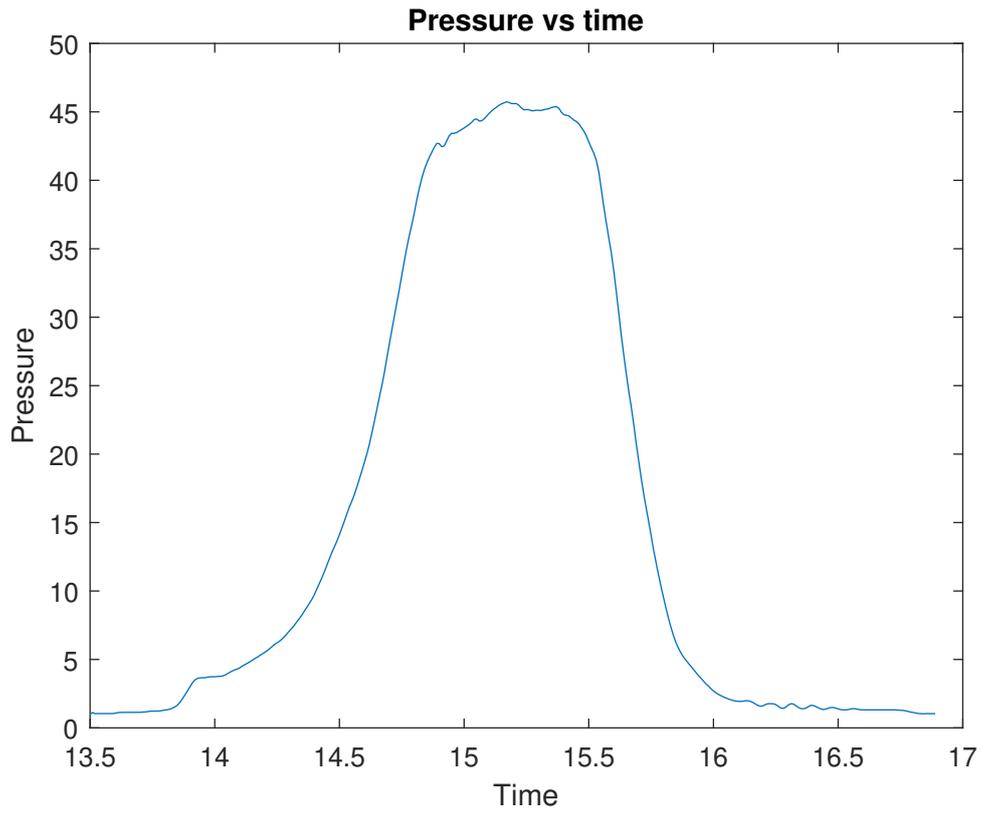


Figure 3.21: Input : Pressure Vs Time

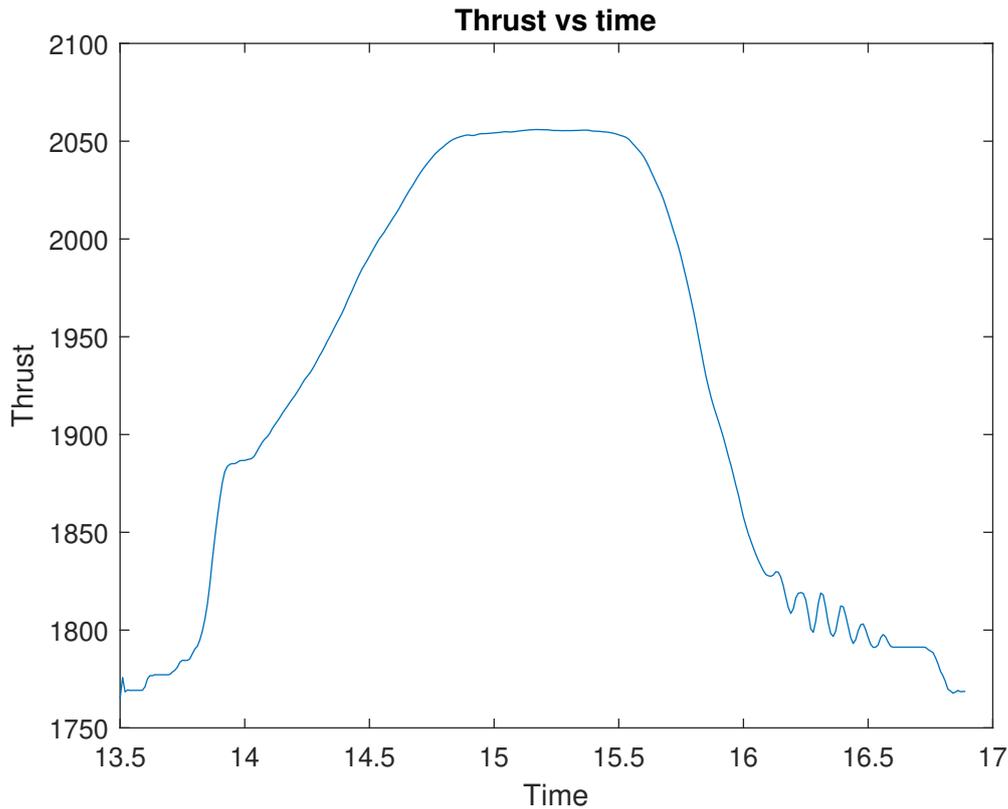


Figure 3.22: Output : Thrust Vs Time

### 3.1.19 Pyrotechnic Igniter & Battery

The solid rocket which[41] we made is of having 1.2 kg propellant and is small rocket motor. Pyrotechnic Igniters are best for small rocket motors. The propulsive force of a solid propellant motor is derived from the combustion of solid propellant at high temperature and pressure. The igniter induces the combustion reaction in a controlled and predictable manner by generating heat flux in the form of hot, dense[40] gases that rapidly ignite the propellant surface. The igniter also contributes towards the generation of a certain minimum pressure inside the motor that is adequate for stable and sustained combustion of the propellant.[42]

#### General requirements of an Igniter are:

1. The temperature of the propellant surface should be raised above its autoignition

temperature

2. Motor chamber pressure should be raised above a threshold pressure requirement for stable burning of a propellant
3. Ignition delay (time delay from application of an electrical pulse to the point when 10 per cent of motor peak pressure is achieved), should be within specified limits
4. The rate of pressure rise,  $dp/dt$ , in the motor chamber during ignition transient should not be unduly high leading to undesirable peaks or shock loads. On the other hand, it should not be too low to cause instability, hang-fires, etc.,
5. The igniter should satisfy the functional, environmental and shelf-life/storage requirements

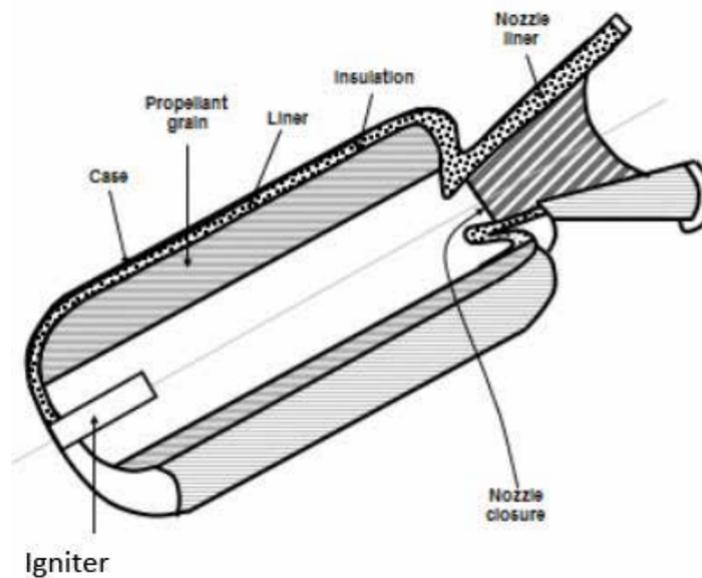


Figure 3.23: General Igniter Function

Pyrotechnic igniters are defined as igniters using pyrotechnic composition or energetic propellant like chemical formulations (usually in granule and/or small pellet form to give large burning surface area and short burn time) as a heat producing material.[43]

The constituents of igniter charge are : fuel, oxidizer, binder mainly and curing agent and other additives in some cases. Powdered Al, B, Mg are used as fuel.  $KNO_3$ ,  $KClO_3$ ,  $KClO_4$ ,  $NH_4ClO_4$ ,  $NH_4NO_3$  are generally used as oxidizers.

Plastizedethyl cellulose is used as a binder which reduces sensitivity.

In ignition of solid rocket motors, a series of events takes place in a tightly timed sequence starting with:

1. Application of an electric pulse
2. Initiation of first fire element (squib or pyro-cartridge)
3. Generation of flash/flamelet
4. Amplification of flash by primer
5. Build up of flash to a strong flame by main igniter charge

### **Nozzle Throat Igniter**

Throat-based igniters are also useful for compact rocket motors where space at nozzle divergent end cannot be used for configuring nozzle cap-based igniter due to length or diameter constraint, and therefore igniter is mounted on the throat of the motor. The material of construction is chosen to give appropriate ejection pressure and ensure smooth ejection of igniter through the throat without damaging it.[44][45][46]

1. Igniter is of ejectable type
2. Igniter hardware ensures sealing of gases at the throat using a seal
3. Charge mass consists of gunpowder,  $\text{BKNO}_3$  granules and pellets, each one for its different purpose
4. O-Ring seating at the neck of the igniter provides sealing at the throat



Figure 3.24: Throat-based igniter with nozzle



Figure 3.25: Throat-based igniter fitted inside nozzle (Throat view Divergent view)

### Operational Features

Throat-based igniter is squib-based ignition system. The squib wires are taken out from the back of the igniter and is held tight at the divergent using a tapered disc butting the divergen to nozzle end. Electrically initiated squib ignites the granules, gunpowder and the pellets. Due to the pressure effect of gunpowder, burning pellets are discharged from the canister into the main combustion chamber. This ignites the propellant surface initiating sustainable ignition. Once adequate pressure is developed inside the chamber, the igniter is ejected from the throat by deforming the collar at which it was held at the throat. To ensure smooth ejection of igniter through the throat, soft material like aluminium is selected as a material of construction for igniter canister.

Throat-based igniters of this composition become very essential in high L/D motors where simultaneous ignition at the head end and nozzle end has to be assured. Similar to nozzle cap based type, this configuration also helps in increased propellant loading and simplified interfaces at the head end. These igniters are generally useful for solid propellant motors of long length.

### 3.1.20 Hydrotest

Hydro test or Hydrostatic test is a type of pressure test performed on piping and pressure vessels to check system integrity under pressure conditions. A hydrostatic test is performed by using water as the test medium. This test is conducted in Propulsion lab, The model design, experimental setup, results are as follows.,

Based on calculation, refer (3.5), The hydrotest setup is designed and fabricated

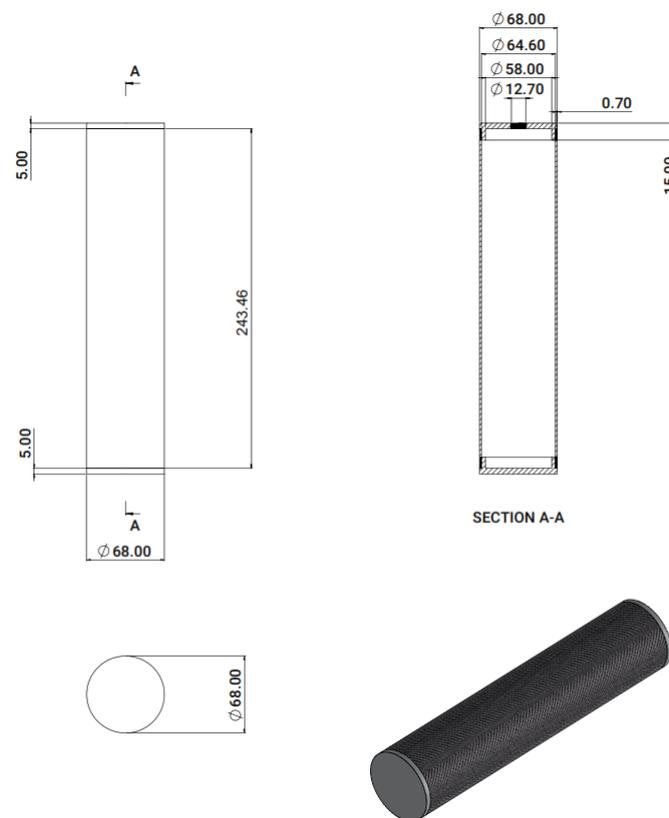


Figure 3.26: Rocket Motor Design

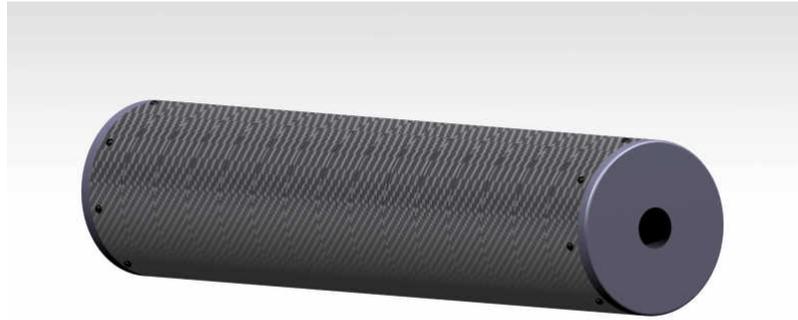
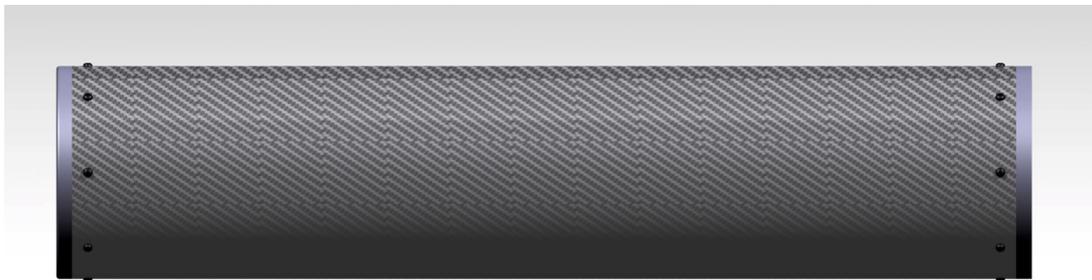


Figure 3.27: Rocket Motor CAD



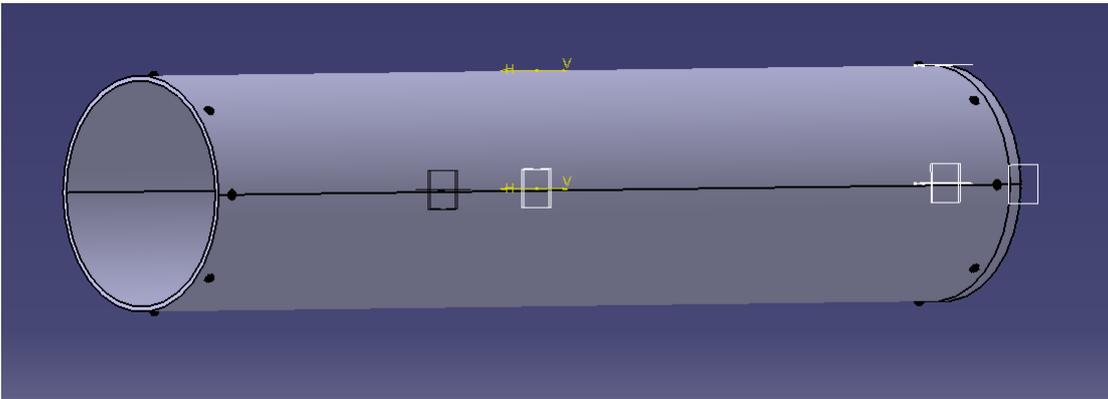
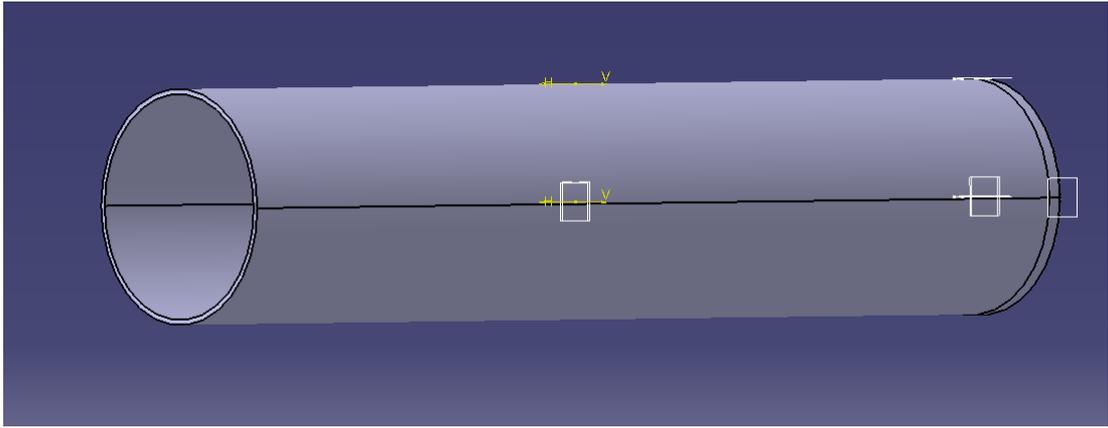




Figure 3.28: Hydrotest Setup



Figure 3.29: Result

Thus, the fabricated Rocket Motor successfully able to handle 50 bar pressure.

## 3.2 SUB-SYSTEMS OF MISSILE

### 3.2.1 Canard Design

The Canard Design, and Canard Data is obtained from reference of previous work of this project, done by Niharika through her dual degree thesis developing a guidance system for a low cost missile, and the same are summarized below.

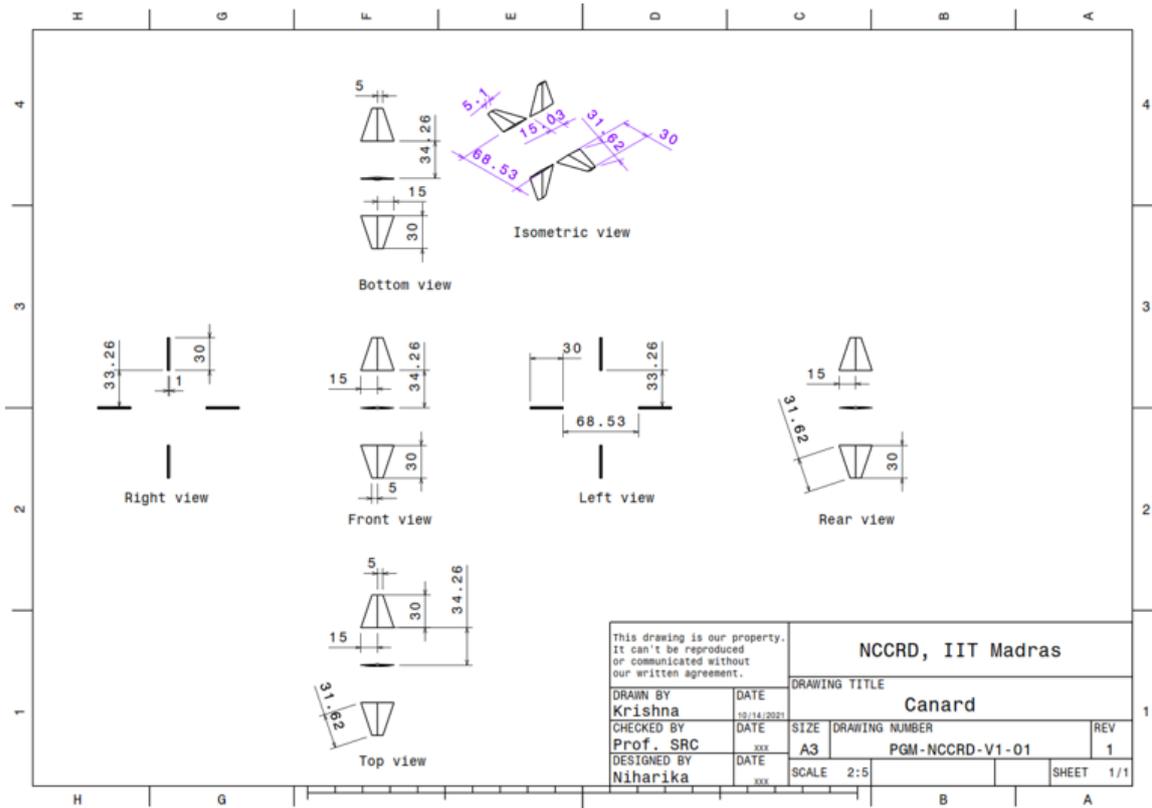


Figure 3.30: Canard Design

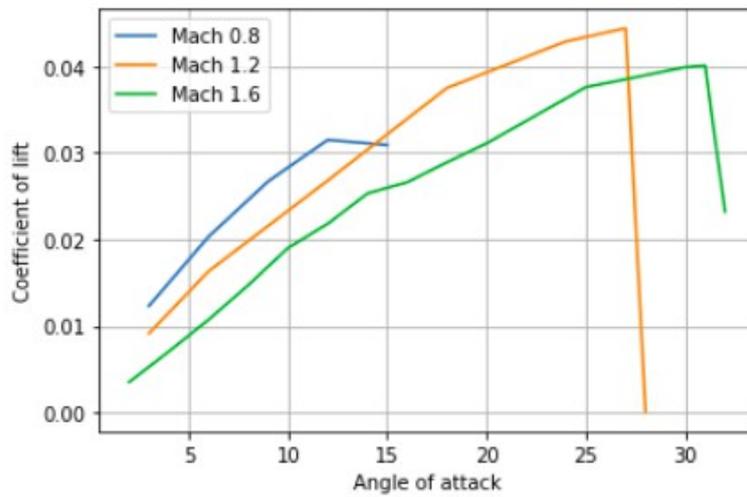


Figure 3.31:  $C_l$  vs AOA

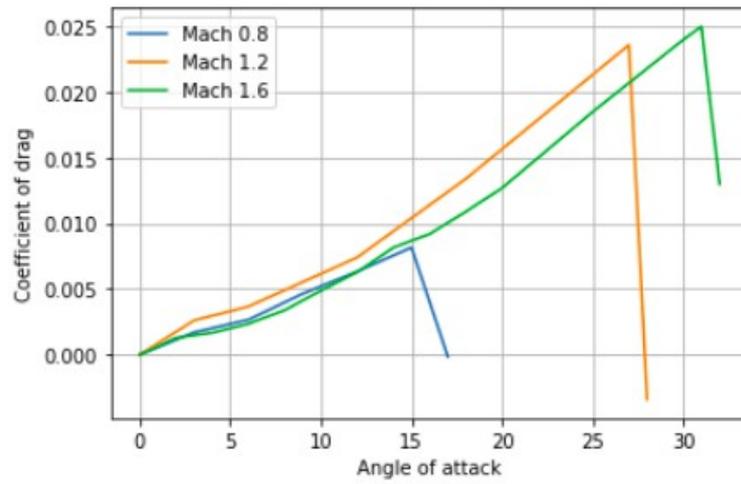


Figure 3.32:  $C_d$  vs AOA

### 3.2.2 Canard Mechanism

For Design of Canard Mechanism, we have taken reference of the following images from T minus arduino.

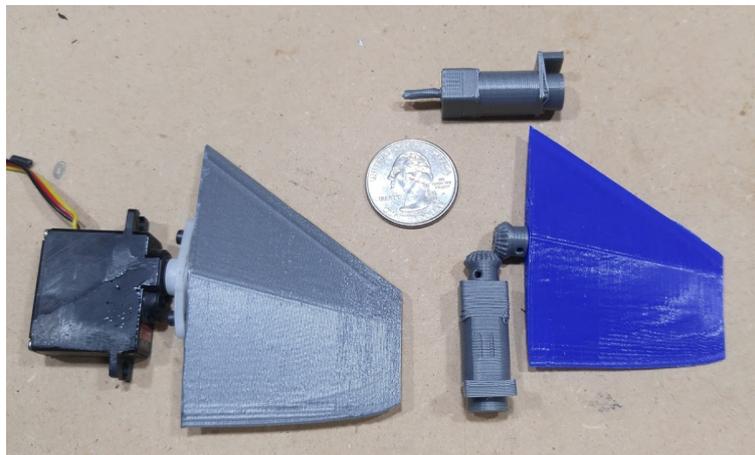
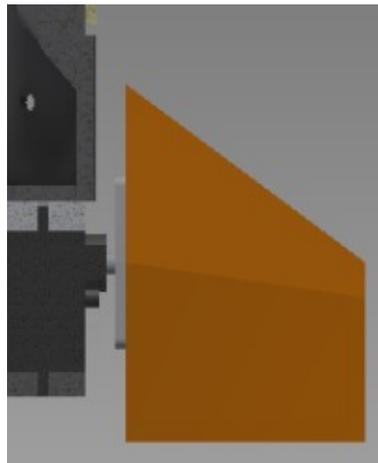
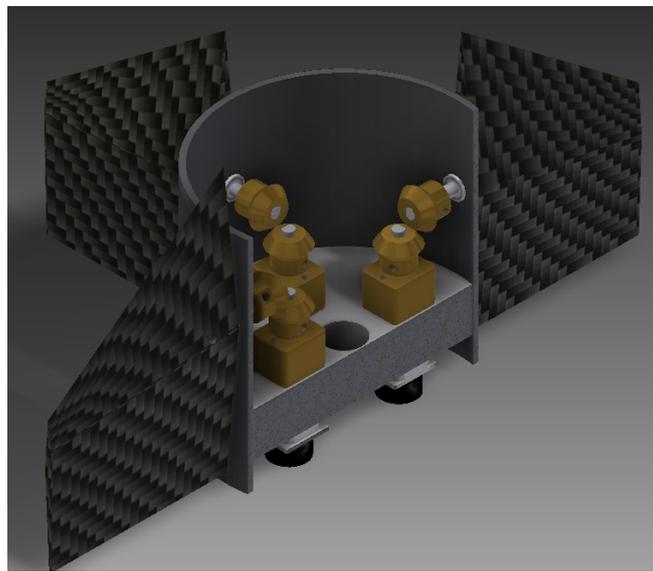
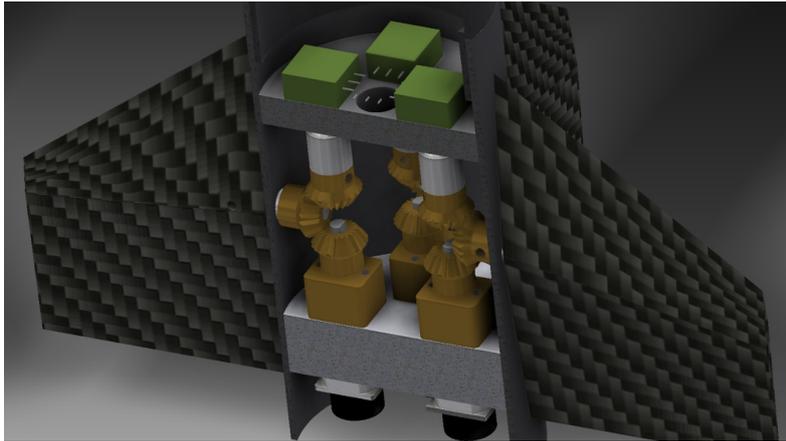


Figure 3.33: Reference : Canard Mechanism





The first design of canard mechanism, is to control the canards using servos. This design contains 2 parts.

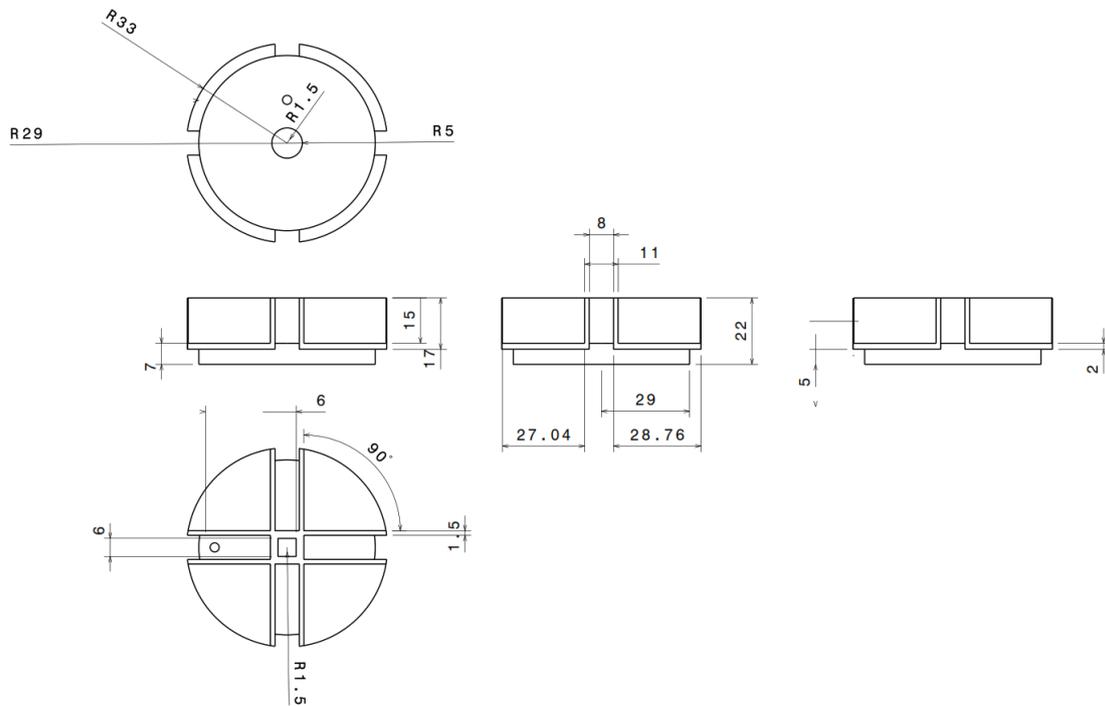


Figure 3.34: Design : Canard Mechanism 1

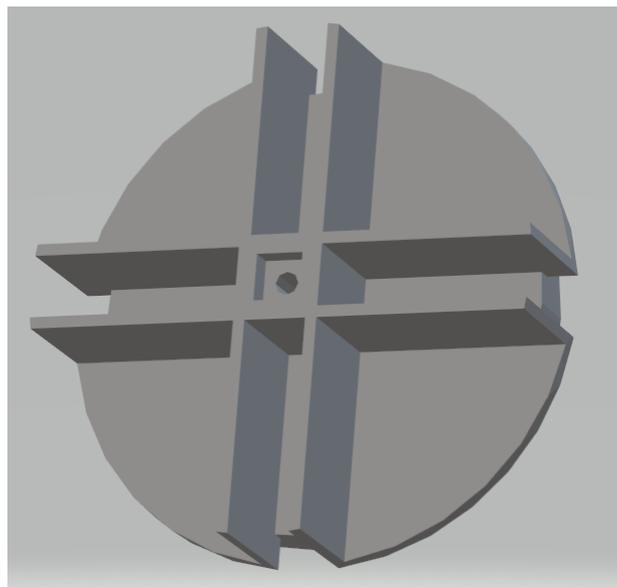
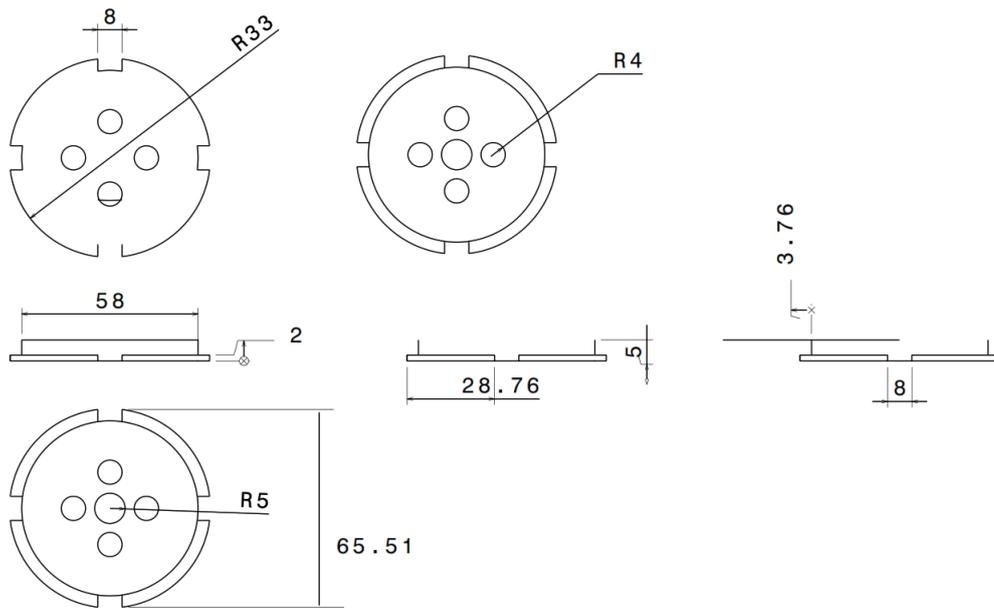
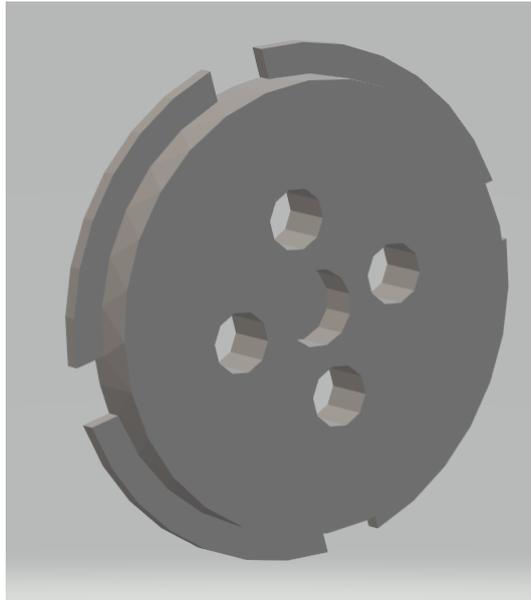


Figure 3.35: Canard Mechanism 1



The second design of canard mechanism, is made to use servos with ( 3.0 - 3.5 kgf.cm Torque, and Rate 0.15 / 0.13 s / 60 degrees at 5 Volts) and to make mechanism design with single part.

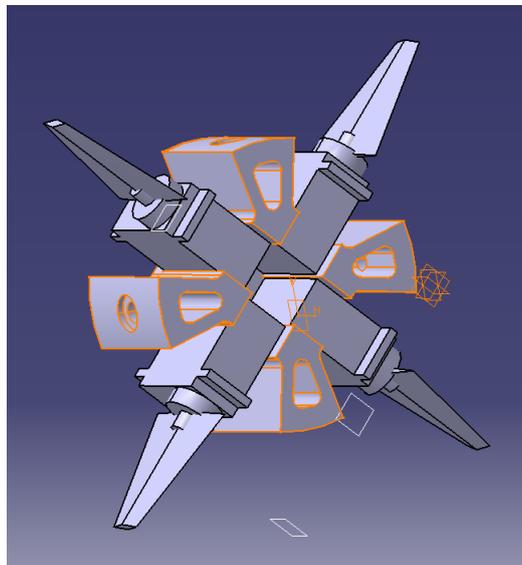


Figure 3.36: Design : Canard Mechanism 2

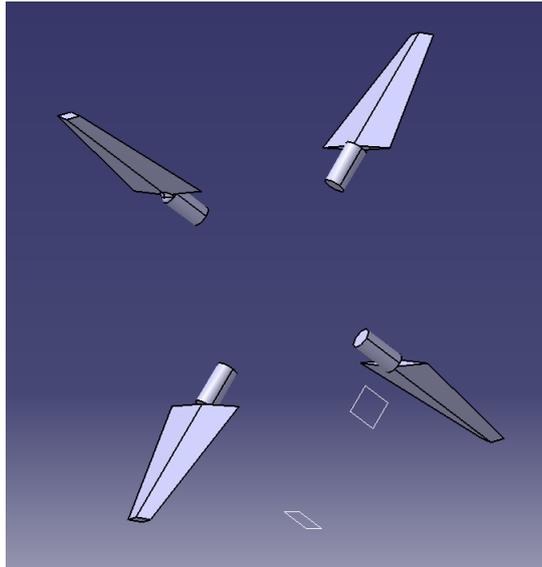


Figure 3.37: Canard Series Assembly A-1

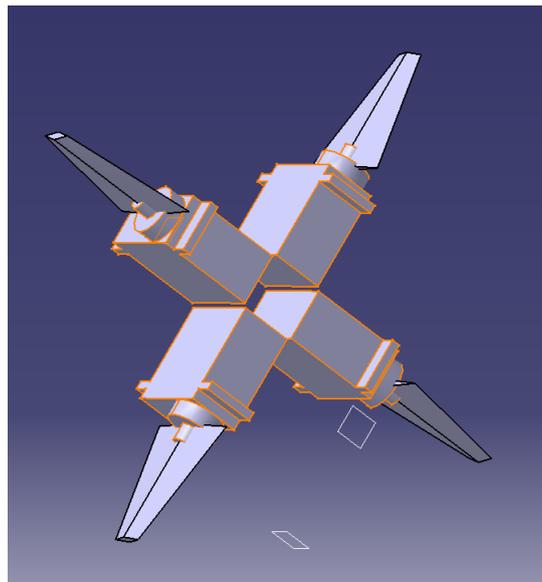


Figure 3.38: Canard Series Assembly A-2

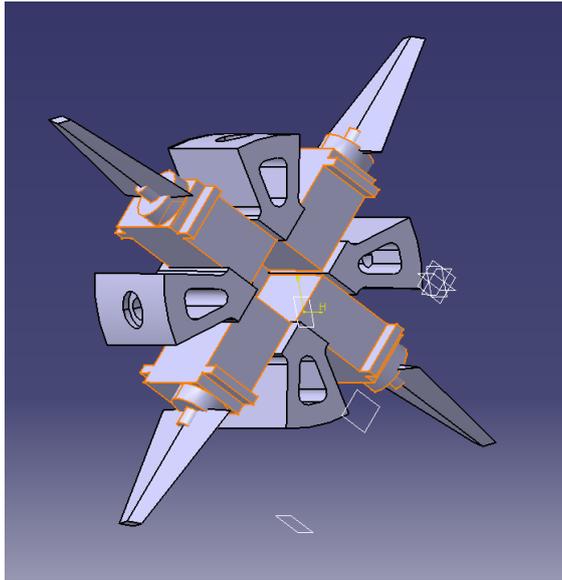


Figure 3.39: Canard Series Assembly A-3

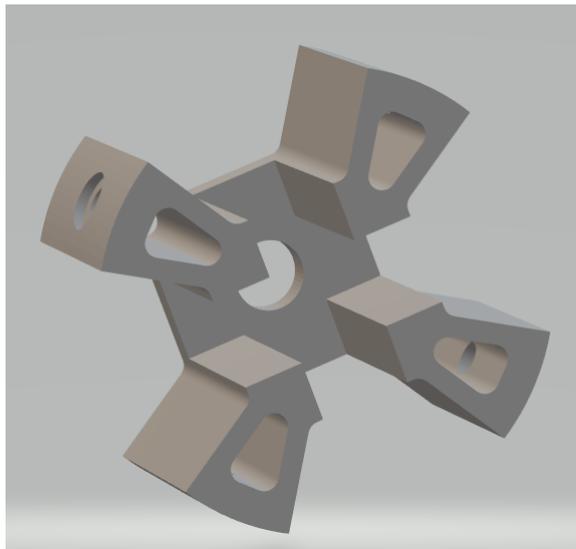
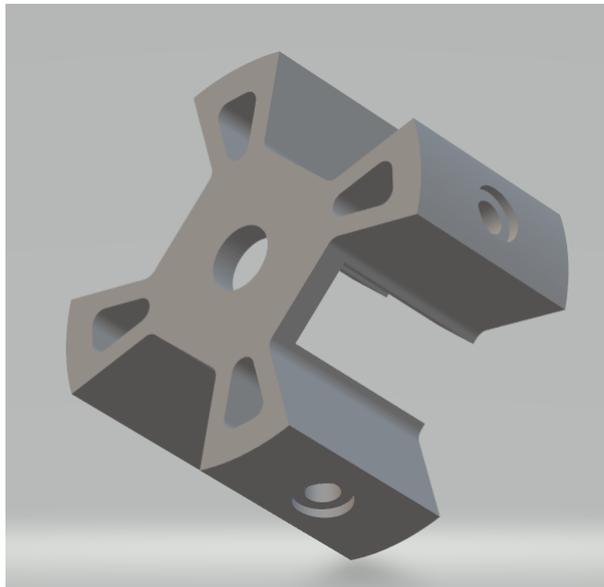
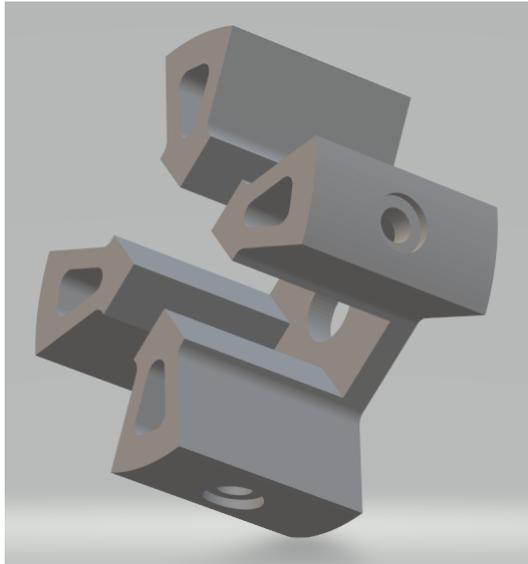


Figure 3.40: Canard Mechanism 2



### **3.2.3 Payload Profile**

Payload is the impact fuse bomb of 2.5 kg for Missile V1, V2, and to be 2.1 kg for Missile V3, V4.

The dimensions of the specification of impact fuse payload bomb, remain same for all 4 versions of missiles, as given in figure 3.41

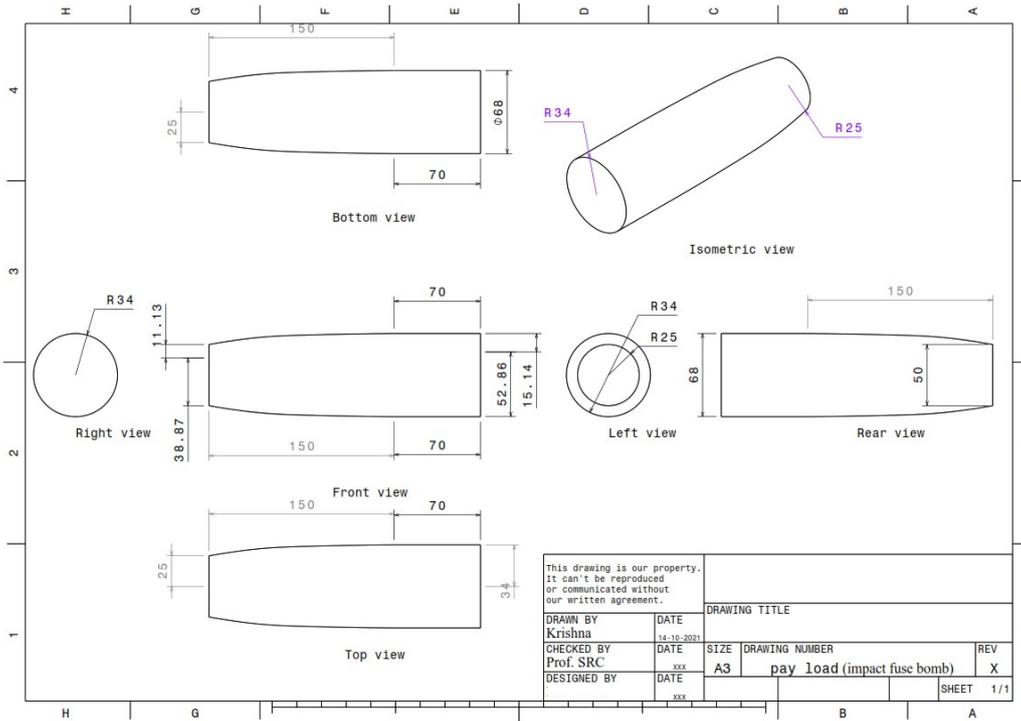


Figure 3.41: Payload Dimensions



Figure 3.42: Payload

### 3.2.4 Gimbal Design

Initial version of gimbal is shown in 3.43

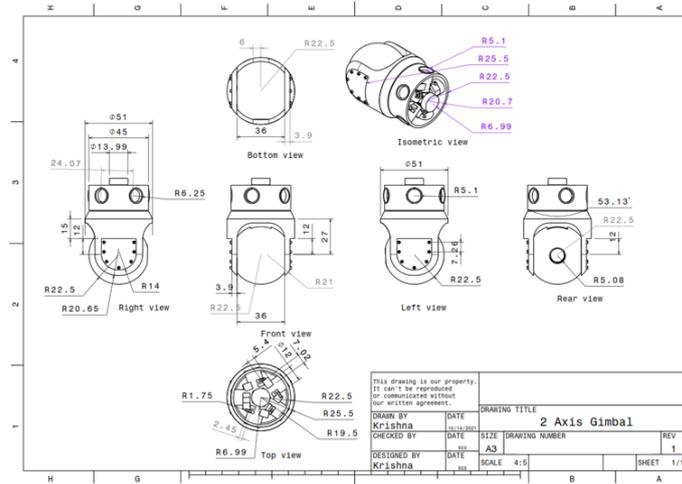


Figure 3.43: Gimbal : Version 0

The 2 Axis gimbal is as follows in figure . This Gimbal is finally designed after so many iterations of design and testing as shown in figures 3.44 , 3.46 , 3.48.

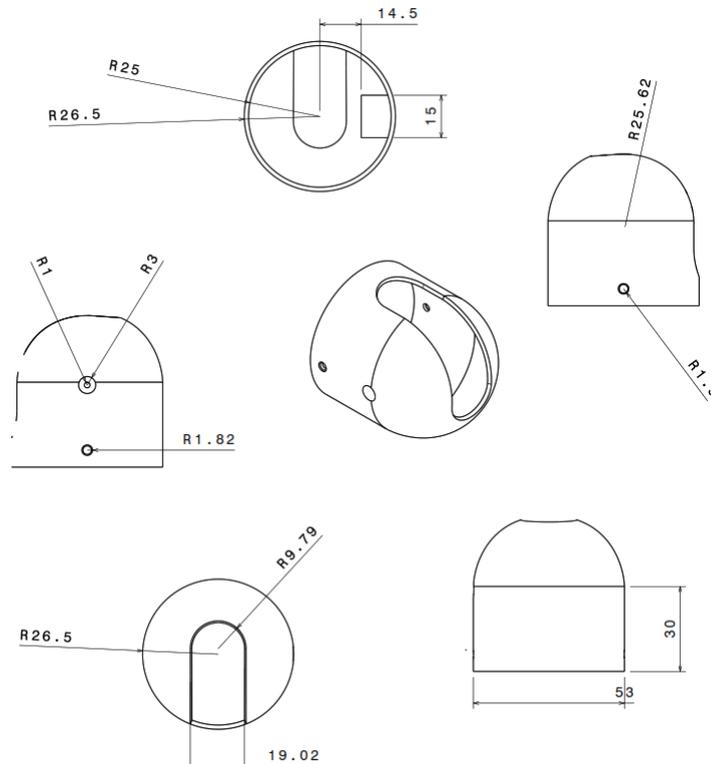


Figure 3.44: Gimbal : Master Frame



Figure 3.45: Fabricated : Gimbal : Master Frame

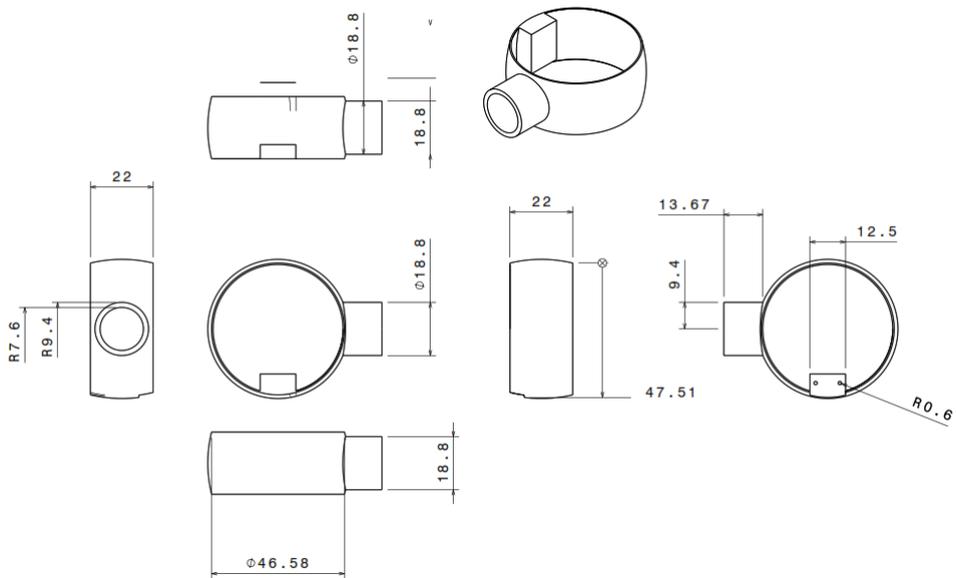


Figure 3.46: Gimbal : Rolling Structure



Figure 3.47: Fabricated : Gimbal : Rolling Structure

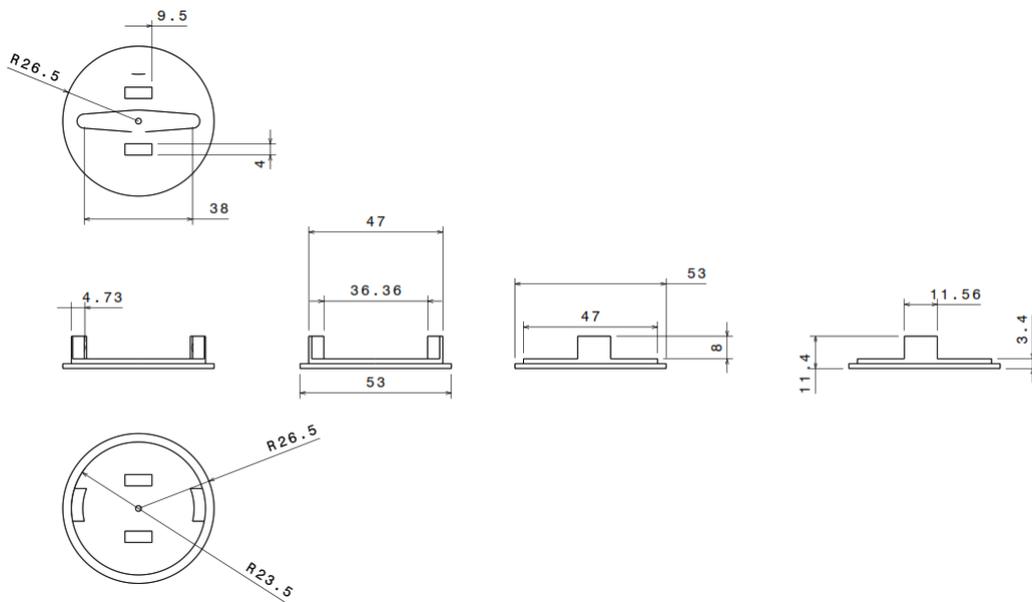


Figure 3.48: Gimbal : Base Plate



Figure 3.49: Fabricated : Gimbal : Base Plate



Figure 3.50: Fabricated : Assembled : Gimbal



### 3.2.5 Object Tracking

The camera will work with RGB color mode, which can be understood by thinking of it as all possible colors that can be made from three colored lights for red, green, and blue. This will be read as [47] Blue, Green, Red by the software designed. To detect the color to track, use code, in appendix C.1. As described with BGR, a pixel is represented by 3 parameters, blue, green, and red. Each parameter usually has a value from 0–255 (or 0 to FF in hexadecimal). For example, a pure blue [48] pixel on your computer screen would have a B value of 255, a G value of 0, and a R value of 0.

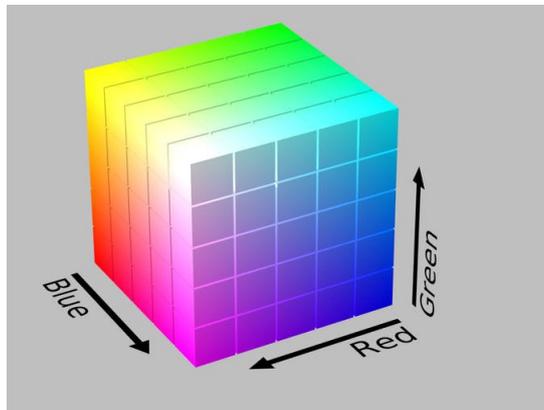


Figure 3.51: BGR Color code

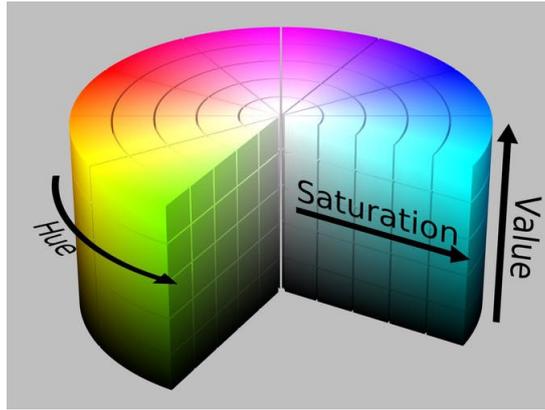


Figure 3.52: HSV Color code

OpenCV works with HSV (Hue, Saturation, Value) color model, that it is an alternative representation of the RGB color model, designed in the 1970s by computer graphics researchers[49] to more closely align with the way human vision perceives color-making attributes. To Track certian color using OpenCV, HSV model must be used. [50]

The code to convert BGR value to HSV value is attached in Appendix C.2. To get the BGR values of the interested pixels, use code in Appendix C.1

Now, The tracking of selected (Region of Interest) ROI in recorded video using the OpenCV csrt algorithm[51], code is given in appendix C.3

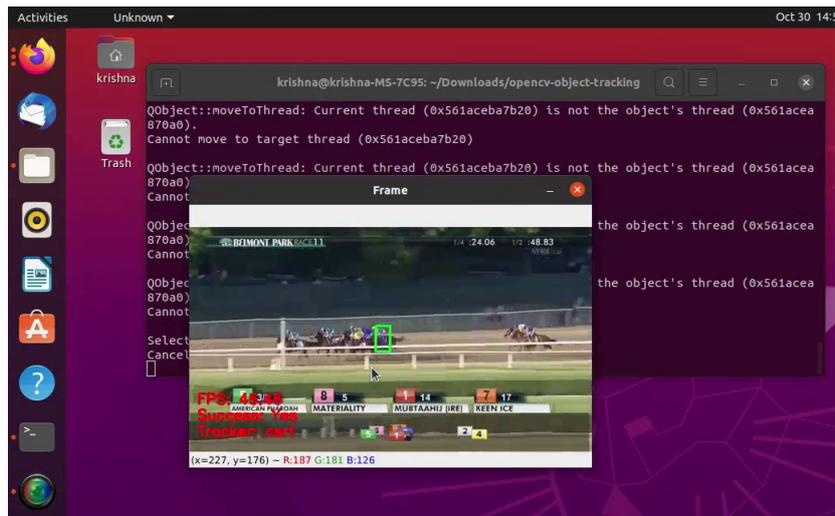
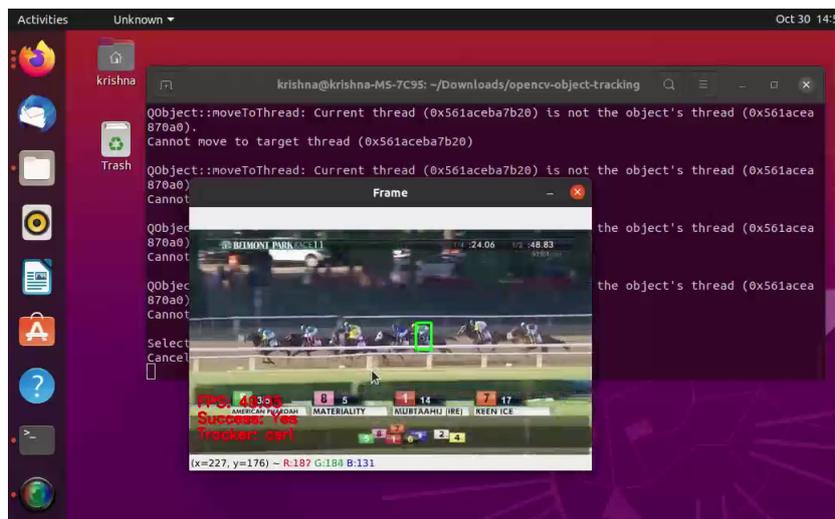


Figure 3.53: ROI Tracking : Recorded Video



The tracking of object in the frame of live video using openCV csrt algorithm, using the code in appendix C.4

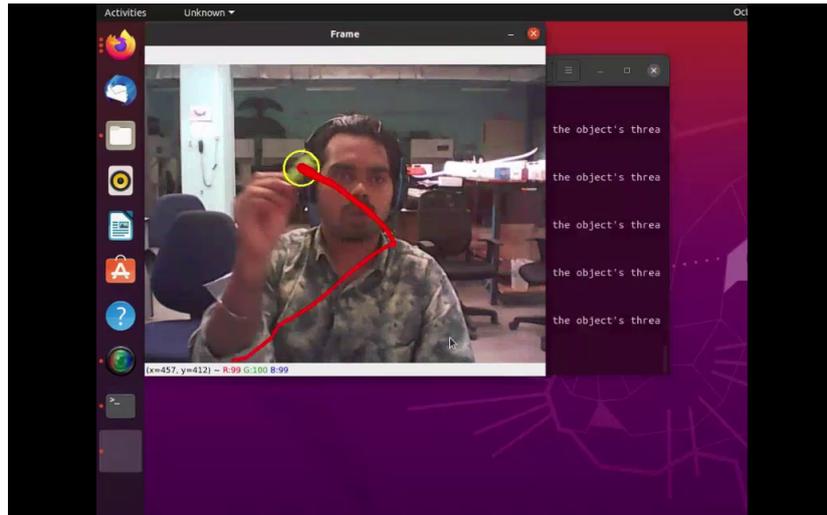
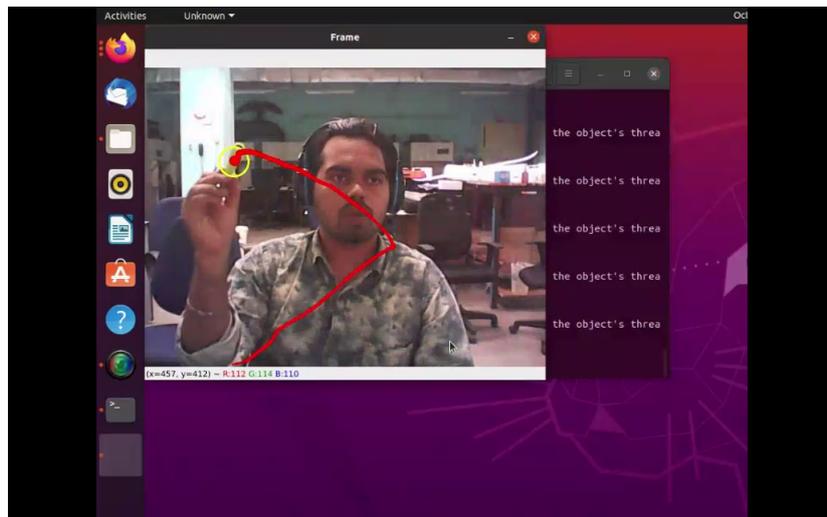


Figure 3.54: ROI Tracking : Live Video



The live position of interested object in the frame can be fetched by the python code, attached in appendix C.5

Using the code in appendix C.6, The live tracking of interested object to the center of frame is possible using the respective control of 2 axis pan tilt servos. The PWM signal to servo is controlled in such a way that the selected ROI object stays at centre of the image frame.



Figure 3.55: Gimbal Tracking





### 3.2.6 Servo Motor Controller

The Canards and Gimbal is controlled by servos, A servo controller is essential to control a servo. A servo controller is a circuit that is used to control the position of a servo motor by the input of PWM signal which is encoded with position or angle parameters.[52]

Micro Maestro 6-Channel USB Servo Controller is best servo controller for the current missile design, since it is has required 6 channels, ( 4 for canard servos, 2 for gimbal servos). It is light weight (4.8 grams), compact, (2.16 × 3.05 cm), upgradable firmware. [53]

<b>Channels:</b>	<b>6</b>
<b>Minimum operating voltage:</b>	5 V
<b>Maximum operating voltage:</b>	16 V
<b>Supply current:</b>	30 mA

Table 3.8: Servo Controller



Figure 3.56: Micro Maestro 6-channel USB servo controller

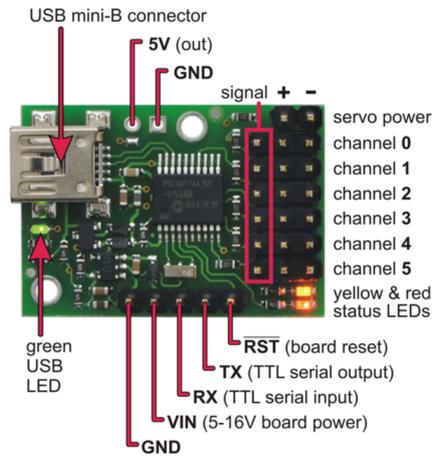


Figure 3.57: Top View : Micro Maestro 6-channel USB servo controller

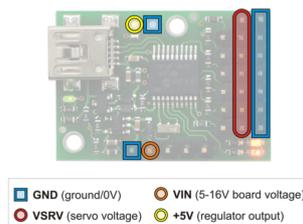


Figure 3.58: Micro Maestro Power Pins

### 3.2.7 Missile Computer

NVIDIA JETSON TX2 exceptionally high compute, accuracy, and power efficiency in a module the size of a credit card. Its small 50 mm x 87 mm size enables real deep

learning applications in small form-factor products.

The purpose of MC is to run high-level mission planning and behavior processes and to exchange messages between processes, other vehicles, and the ground station. Furthermore, a key design goal of the system should be that it is flexible[54] in regard to the architecture and potential expansion. In the future, additional autonomous behaviors, sensors, and communication capabilities may be added. This functionality may even run across multiple processors on separate payload computers. Therefore, it is important that the software components be loosely coupled and communicate using open and flexible architectures.

The Single Board Computer (SBC) chosen for Missile Computer is NVIDIA JETSON TX2 4 GB

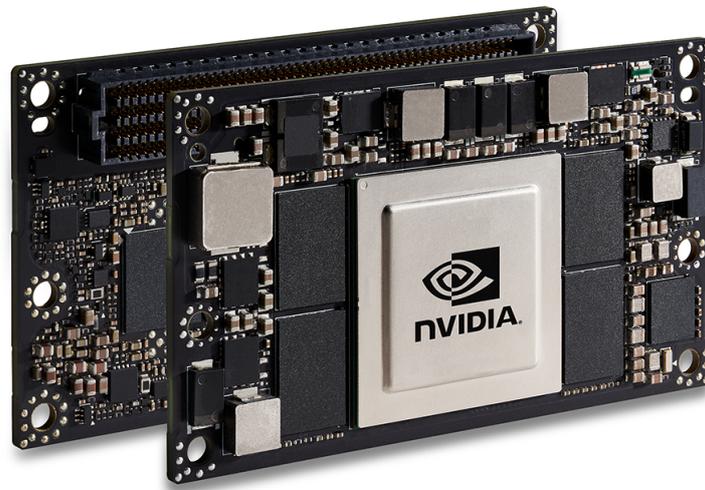


Figure 3.59: NVIDIA Jetson TX2 4 GB

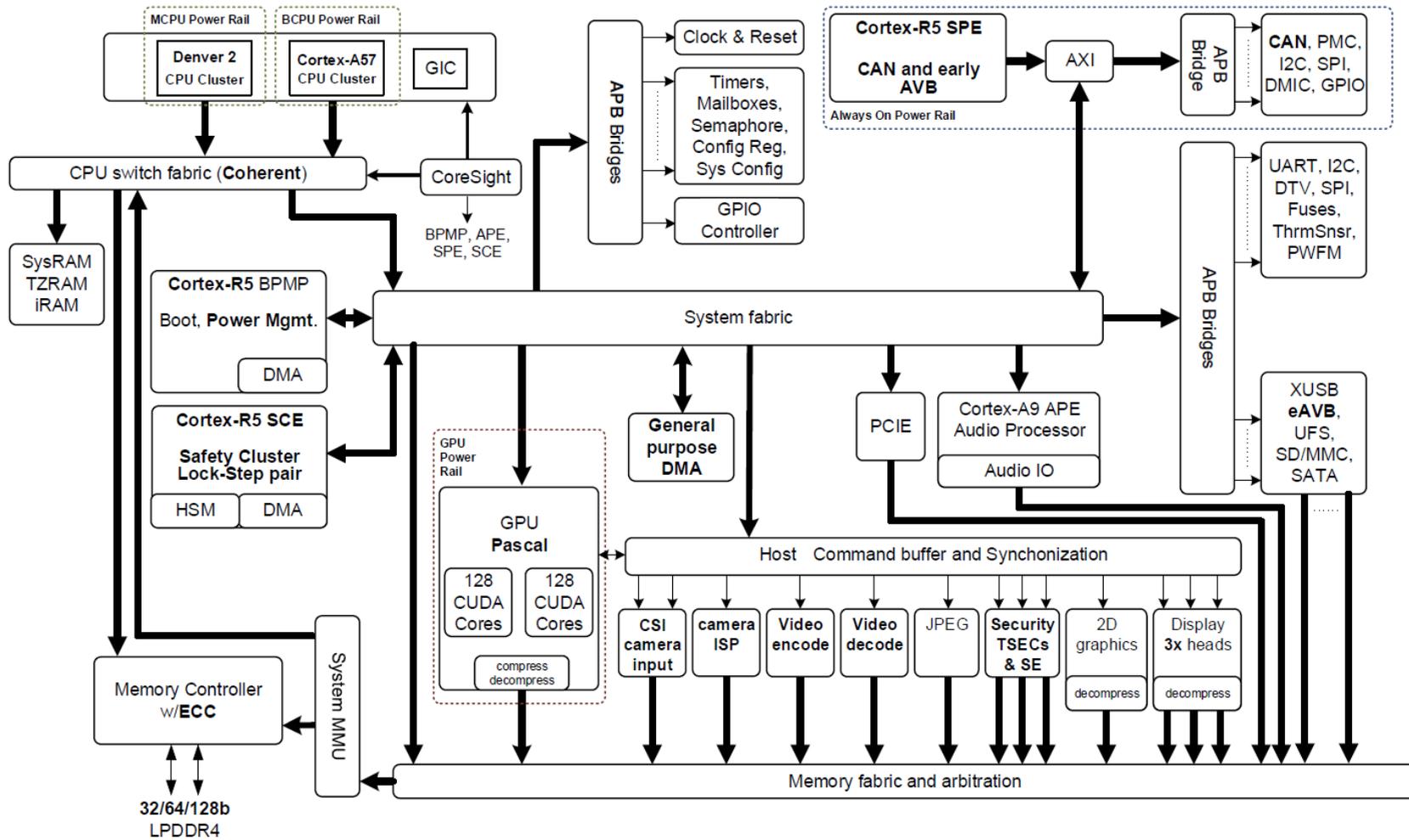


Figure 3.60: NVIDIA Jetson TX2 Architecture

Technical Specifications of Jetson TX2 4 GB	
<b>GPU</b>	NVIDIA Pascal™ architecture with 256 NVIDIA CUDA cores 1.3 TFLOPS (FP16)
<b>CPU</b>	Dual-core Denver 2 64-bit CPU and quad-core ARM A57 complex
<b>Memory</b>	4 GB 128-bit LPDDR4 1600 MHz - 51.2 GBs
<b>Storage</b>	16 GB eMMC 5.1
<b>Video Encode</b>	500 MP/sec 1x 4K @ 60 (HEVC) 3x 4K @ 30 (HEVC) 4x 1080p @ 60 (HEVC) 8x 1080p @ 30 (HEVC)
<b>Video Decode</b>	1000 MP/sec 2x 4K @ 60 (HEVC) 4x 4K @ 30 (HEVC) 7x 1080p @ 60 (HEVC) 14x 1080p @ 30 (HEVC)
<b>Connectivity</b>	Wi-Fi requires external chip 10/100/1000 BASE-T Ethernet
<b>Camera</b>	12 lanes MIPI CSI-2, D-PHY 1.2 (30 Gbps)
<b>Display</b>	HDMI 2.0 / eDP 1.4 / 2x DSI / 2x DP 1.2
<b>UPHY</b>	Gen 2   1x4 + 1x1 OR 2x1 + 1x2, USB 3.0 + USB 2.0
<b>Size</b>	87 mm x 50 mm
<b>Mechanical</b>	400-pin connector with Thermal Transfer Plate (TTP)

Table 3.9: NVIDIA Jetson TX2 Specifications

### 3.2.8 Jetson TX2 Carrier Board : J120

The J120 carrier board turns the Jetson TX2 compute module into a super-mini-computer for desktop usage and for integration into UAVs and drones/missiles. It is very compact. It has the same height as the TX1 (50 mm ) and extends to one side to make space for standard connectors for Gigabit Ethernet, two USB 3 type A and mini HDMI.

It features one M.2 type M slot for ultra fast SSDs (2280 form factor) which is connected via 4 PCIe lanes to achieve a read and write performance up to 2500 Mbyte/s.

The J120 features CAN controllers which are connected via the SPI interface. A bug in the TX1 prohibits the use of spidev0.0. If it is accessed then the spidev0.1 is blocked. Please see the technical reference manual for details. So for CAN to work, the CAN controller 1 chip has to be physically removed. Only one CAN interface is supported (CAN2). So the J120 rev 3 is only equipped with one CAN interface. This is still under investigation and might be fixed in the future[55]



Figure 3.61: J120

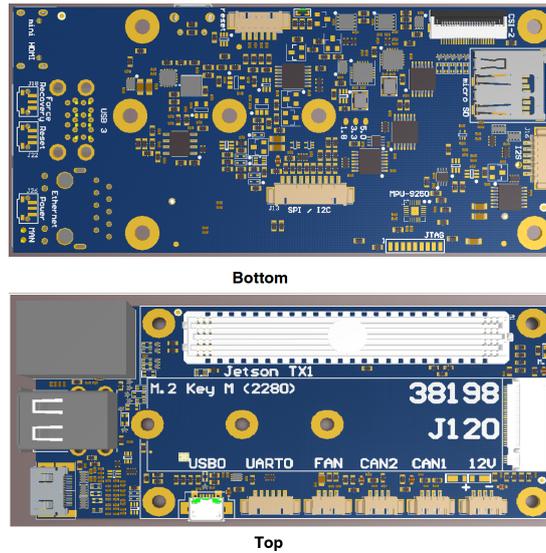


Figure 3.62: J120 Top & Bottom

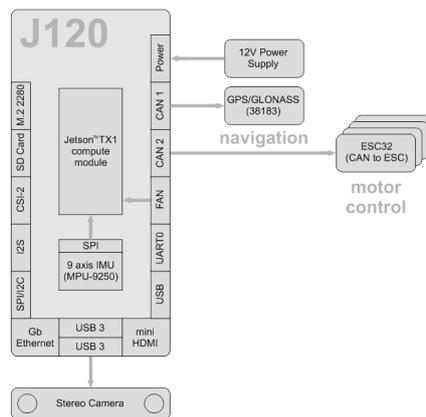


Figure 3.63: CAN centric flight controller

### 3.2.9 IMU

An IMU is a specific type of sensor that measures angular rate, force and sometimes magnetic field. IMUs are composed of a 3-axis accelerometer and a 3-axis gyroscope, which would be considered a 6-axis IMU. They can also include an additional 3-axis magnetometer, which would be considered a 9-axis IMU.

Sensor Name	Measures	Range & Units	Axes	Example Sensor
Accelerometer	Acceleration	$\pm 200$ g	3 axis	ADXL377 - High-G Triple-Axis Accelerometer ( $\pm 200$ g Analog Out)
Gyroscope	Angular velocity	$\pm 2000$ °/sec	3 axis	L3G4200D by STMicroelectronics
Magnetometer	Direction/position	$\pm 1300$ uT	3 axis	BMM150 by DFRobot Fermion

Table 3.10: 9 Axis IMU Sensor

### 3.2.10 Flight Control System (FCS)

Flight Control System (FCS) typically includes an autopilot, Global Positioning System (GPS), gyros, Inertial Measurement Unit (IMU), and a dedicated link to a ground station computer which can be used to send waypoint and control commands to the autopilot. The FCS also directly generates the control signals for aircrafts control surfaces and throttle. Note that the FCS should be able to operate independently and isolated from the mission computer by having one or more dedicated datalinks and power sources. This provides for a level of fault tolerance in the system, as well as enabling it to be easily extensible. In principle, the flight control system can operate as a "black box" and it does not matter where the commands originate, while the mission processor also operates as a separate entity and has little knowledge of the internal details of the flight control system. The Single Board Computer used to implement FCS is also called Flight Control Computer (FCC).

The Single Board Computer (SBC) chosen for implementing FCC is the PIXHAWK MODULE [56]

### 3.2.11 Dual Redundant Stores Management Processor

Stores Management Processor or SMP is a Single Board Computer implemented to control and execute weapon store related functionalities. The aim is to use a powerful, lightweight and a small form factor based computing device to implement stores management logic.[57] The SBC should support Real-Time task execution and should also have support for analog and discrete communication for interfacing with other SBCs. Various COTS SBC are available in open source market such as NVIDIA Boards, ESP32, Raspberry, Beaglebone Boards, etc. However after comparing all the above mentioned factors on each of the SBCs, we narrowed down to a Beaglebone Pocketbeagle SBC, which is extremely small and lightweight, cost effective and powerful.

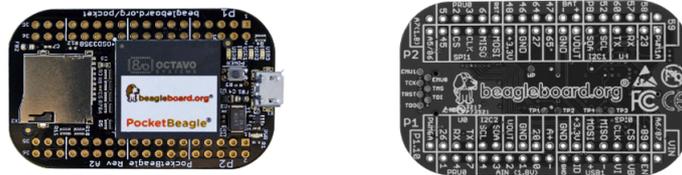


Figure 3.64: Pocketbeagle SBC from Beaglebone

#### PocketBeagle Technical Specifications:

- \* Based on new Octavo Systems OSD3358-SM 21 mm × 21 mm system-in-package that includes 512MB DDR3 RAM, 1-GHz ARM Cortex-A8 CPU, 2x 200-MHz PRUs, ARM Cortex-M3, 3D accelerator, power/battery management and EEPROM
- \* 72 expansion pin headers with power and battery I/Os, high-speed USB, 8 analog inputs, 44 digital I/O s and numerous digital interface peripherals
- \* microUSB host/client and microSD connectors

**Processor:** Octavo Systems OSD3358 1GHz ARM Cortex-A8

- \* 512MB DDR3 RAM integrated
- \* Integrated power management

\* 2 × 32– bit 200 – MHz programmable real-time units (PRUs)

\* ARM Cortex-M3

### 3.2.12 e-CAM132\_TX2 Camera : for 2 Axis Gimbal

e-CAM132\_TX2 - 13MP Autofocus Jetson™ TX2 camera board is a 4-lane MIPI CSI-2 camera for NVIDIA Jetson™ TX2. This camera is based on 1/3.2ÄR1335 CMOS image sensor with advanced 1.1µm pixel BSI technology from onsemi and an integrated high-performance image signal processor (ISP) that performs all the Auto functions (Auto White Balance, Auto Exposure control). e-CAM132\_TX2 is a two board consists of a base board and a 13MP autofocus camera board. This camera board is connected to the base board using 30 cm micro-coaxial cable.

Camera module with Adaptor board - 3.5 Grams

Base board - 13.5 Grams

Coaxial cable - 4 Grams

<b>Resolutions</b>	<b>Uncompressed YUV422</b>
VGA	120 fps
HD (720p)	80 fps
Full HD (1080p)	80 fps
4K Ultra HD (3840x2160)	30 fps
13MP (4192 x 3120)	19 fps

Table 3.11: Maximum Image Transfer Rate

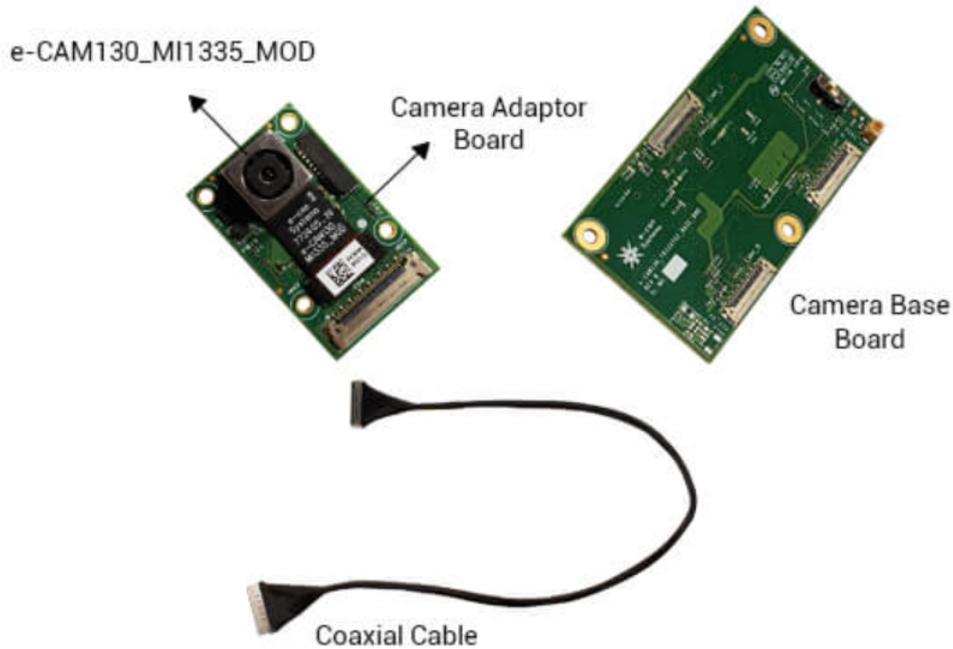


Figure 3.65: e-CAM132\_TX2 Camera Module

### 3.2.13 FPGA Architecture

A field-programmable gate array (FPGA) is an integrated circuit designed to be configured by a customer or a designer after manufacturing – hence the term field-programmable.[64] The FPGA configuration is generally specified using a hardware description language (HDL), similar to that used for an application-specific integrated circuit (ASIC).[60] Circuit diagrams were previously used to specify the configuration, but this is increasingly rare due to the advent of electronic design automation tools. [65]

FPGA emerged from relatively simpler technologies such as programmable read-only memory (PROM) [63]and programmable logic devices (PLDs) like PAL, PLA, or Complex PLD (CPLD).

The general FPGA architecture consists of three types of modules. They are I/O blocks or Pads, Switch Matrix/ Interconnection Wires and Configurable logic blocks (CLB). The basic FPGA architecture has two dimensional arrays of logic blocks with a means

for a user to arrange the interconnection between the logic blocks. [59]

1. Configurable Logic Blocks :: which implement logic functions, includes digital logic, inputs, outputs. It implements the user logic.
2. Programmable Interconnects :: which implement routing. Interconnects provide direction between the logic blocks to implement the user logic. Depending on the logic, switch matrix provides switching between interconnects.[61]
3. Programmable I/O Blocks :: which connect with external components. These are used for the outside world to communicate with different applications.[62]

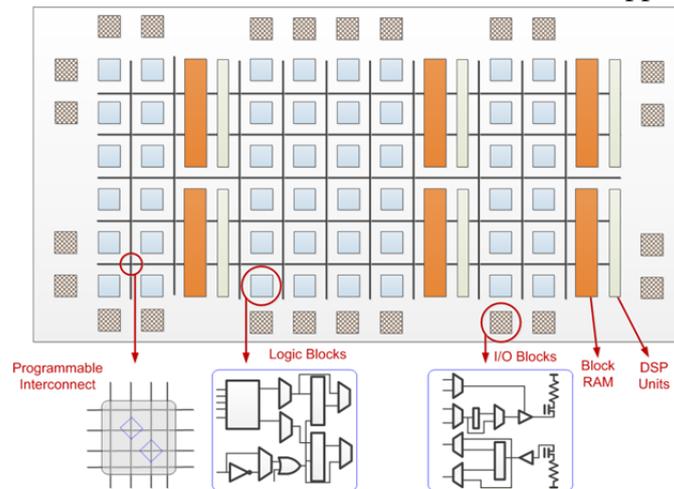


Figure 3.66: FPGA Architecture



Figure 3.67: Example FPGA Circuit board

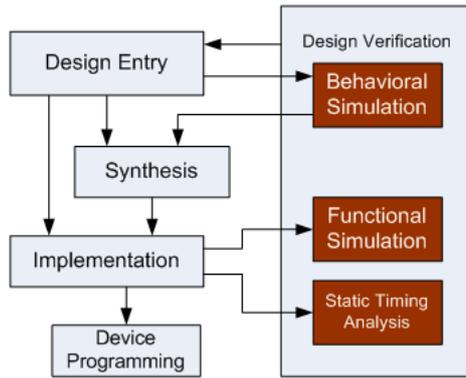


Figure 3.68: Our initial FPGA Architecture

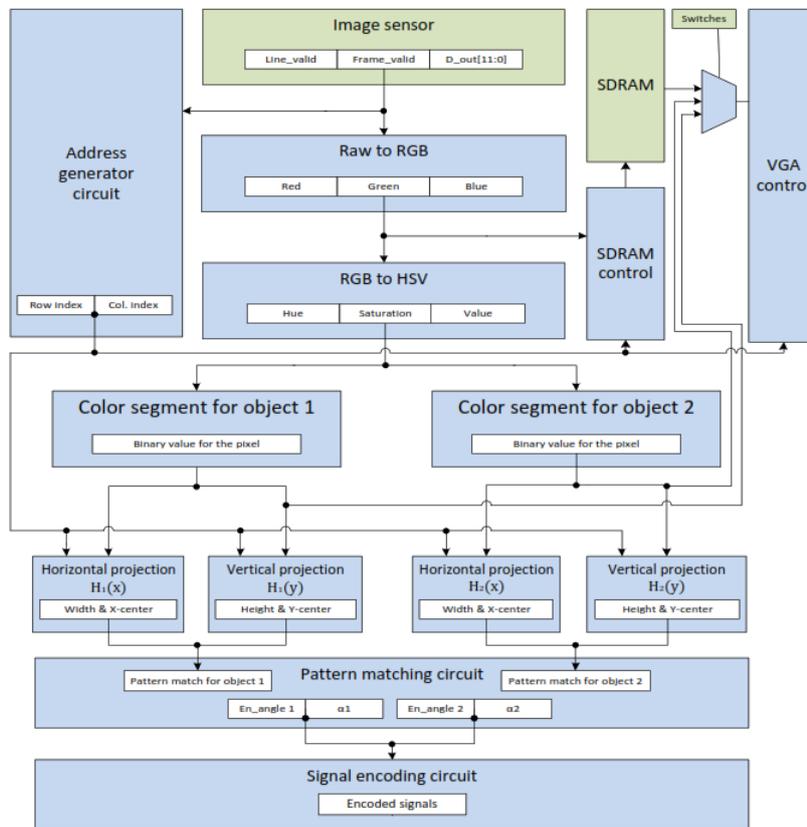


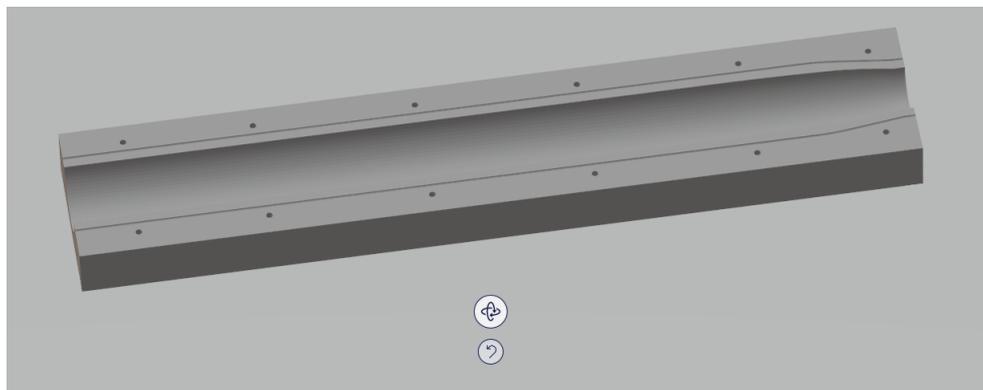
Figure 3.69: FPGA Design Workflow

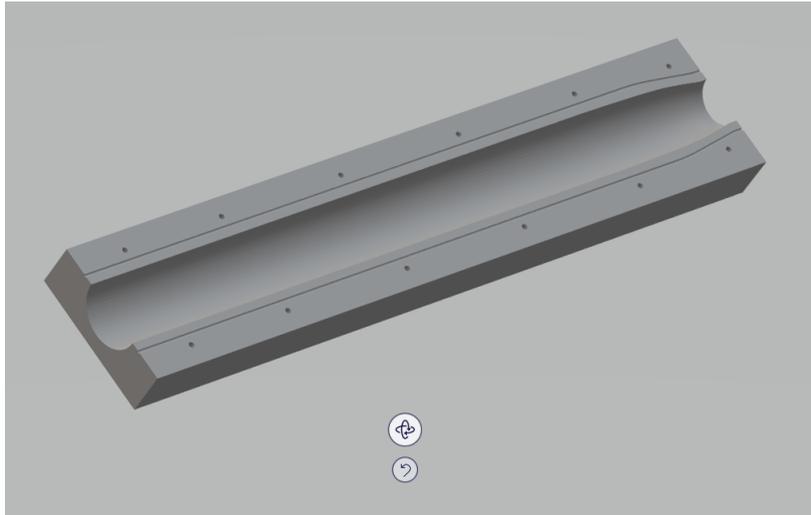
### 3.3 DESIGN OF ACCESSORIES OF MISSILE

#### 3.3.1 Missile Mould



Figure 3.70: Missile Frame Mould





### 3.3.2 Ground Launcher

The Design of ground launcher is as follows,

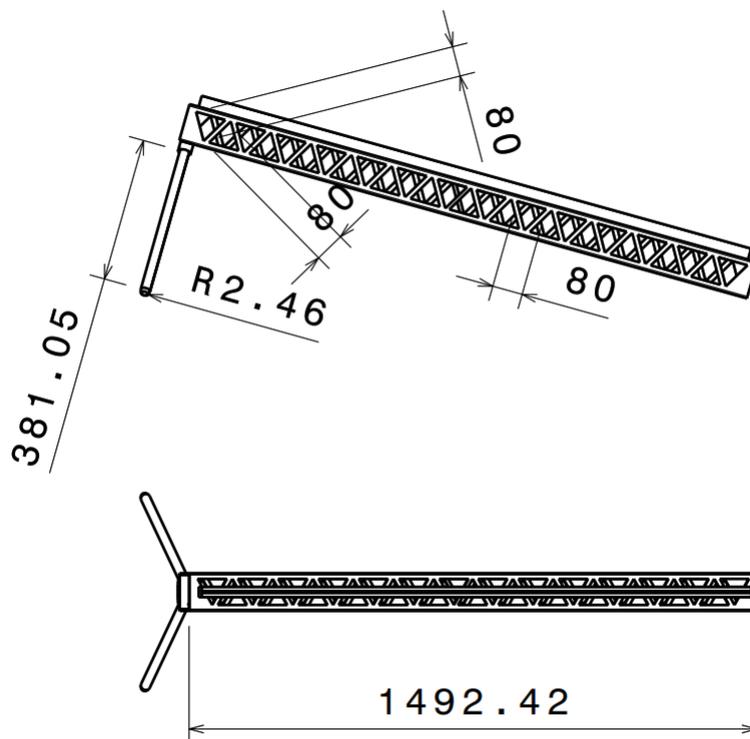
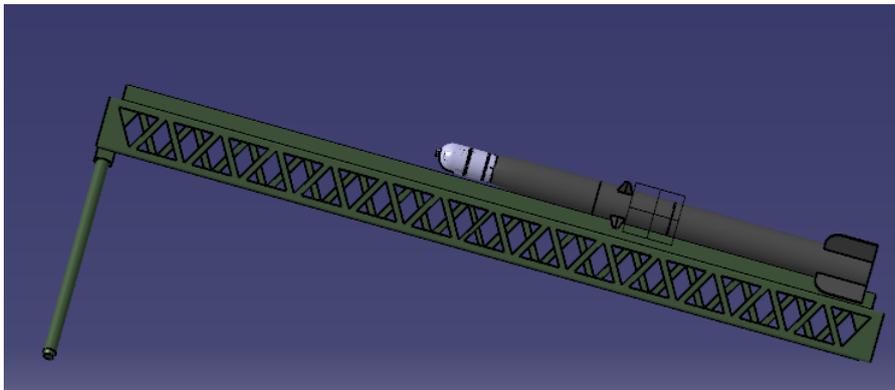
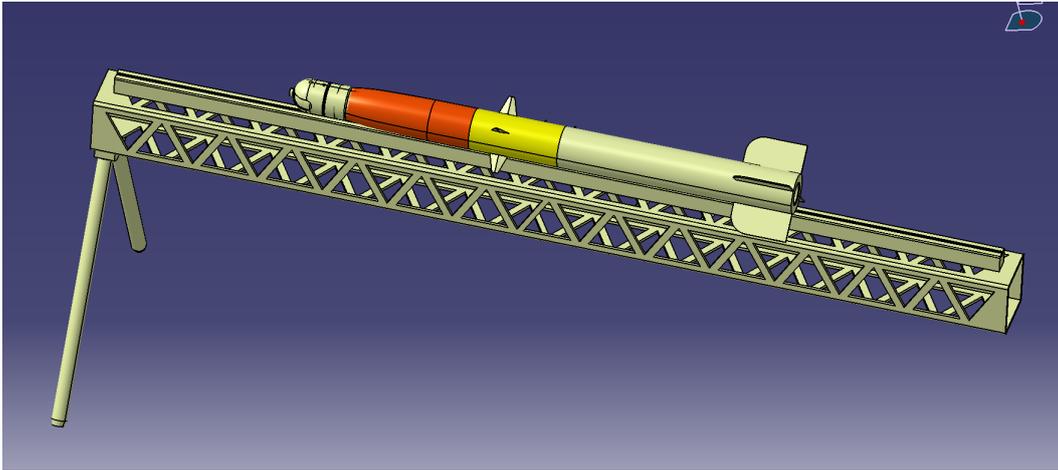
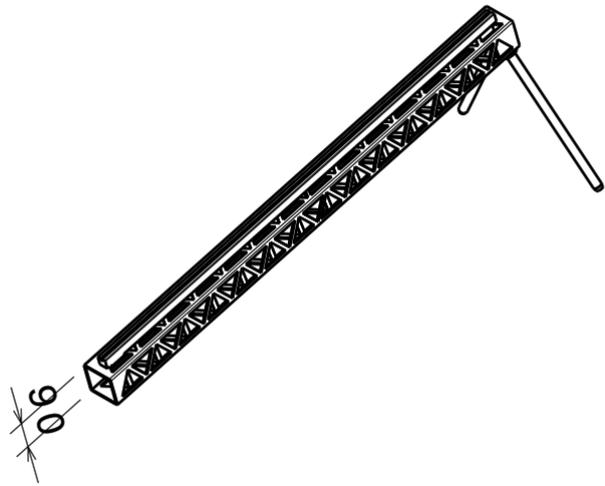
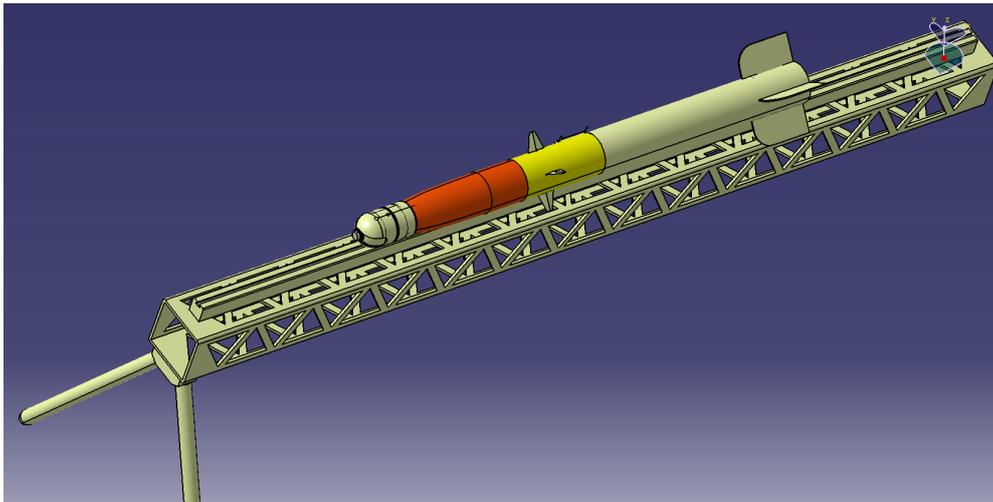
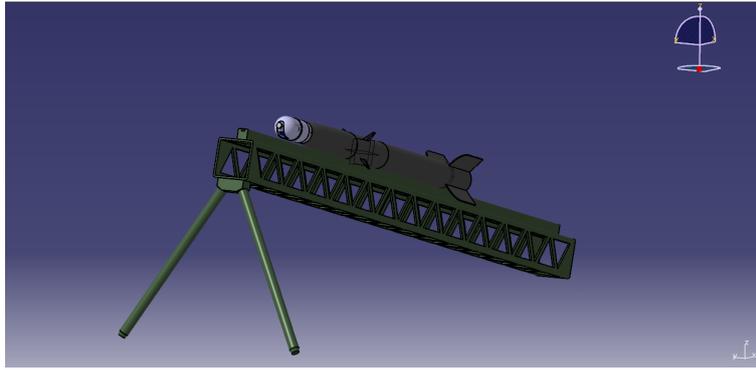


Figure 3.71: Design : Ground Launcher



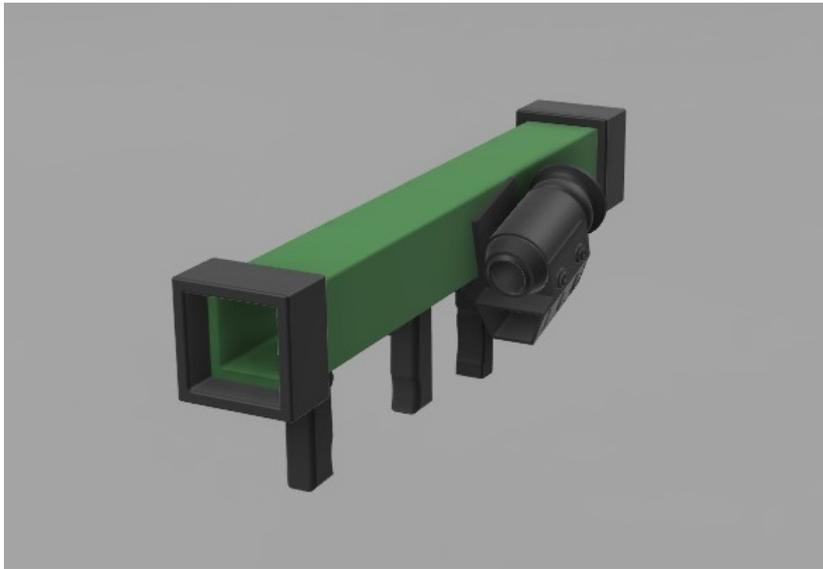


### 3.3.3 Hand Launcher

The same missile designed can also be hand launched, and thus a hand launcher has been designed.



Figure 3.72: Design of Hand Launcher





### 3.3.4 Design of Weapon Release System A

Weapon Release system A is servo control, has a camera attached to the release system for target lock. This system can be used for Missile Version 1 , 2 , 3. This version launches the missile with the known, calculated guide angle.

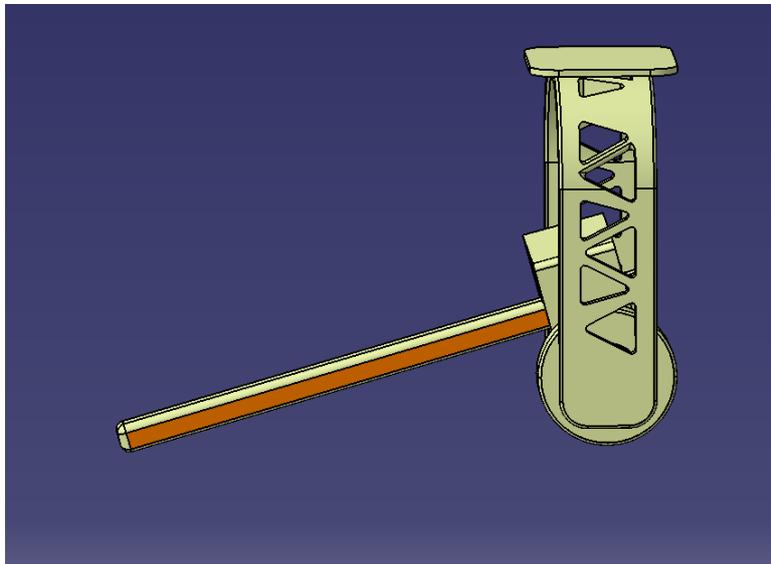
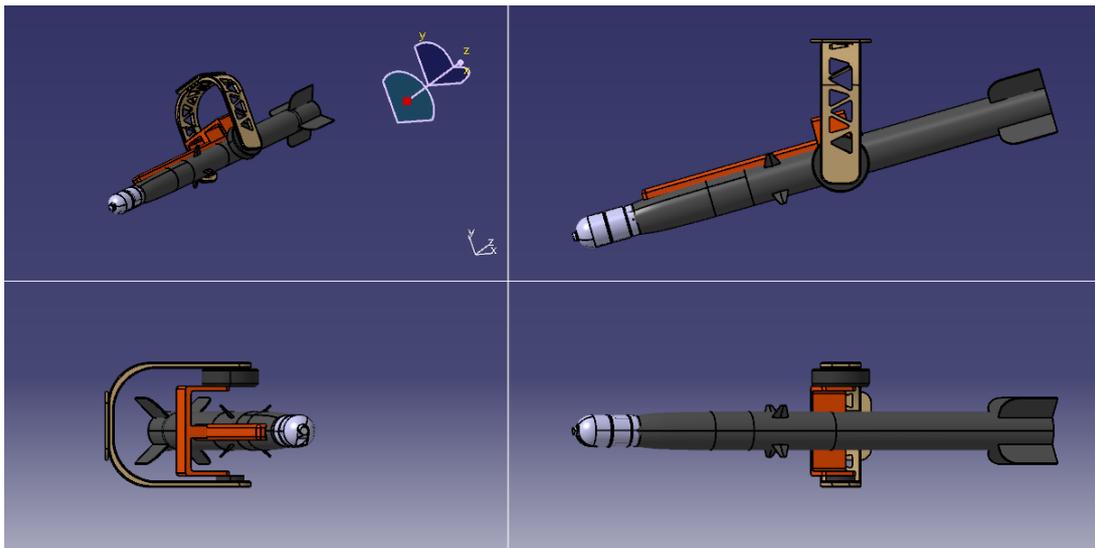
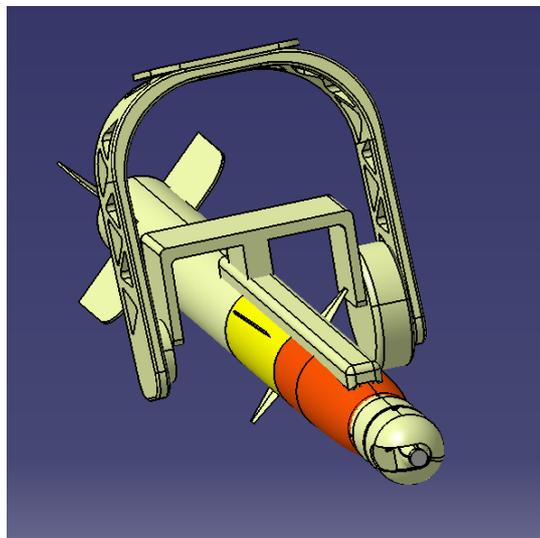
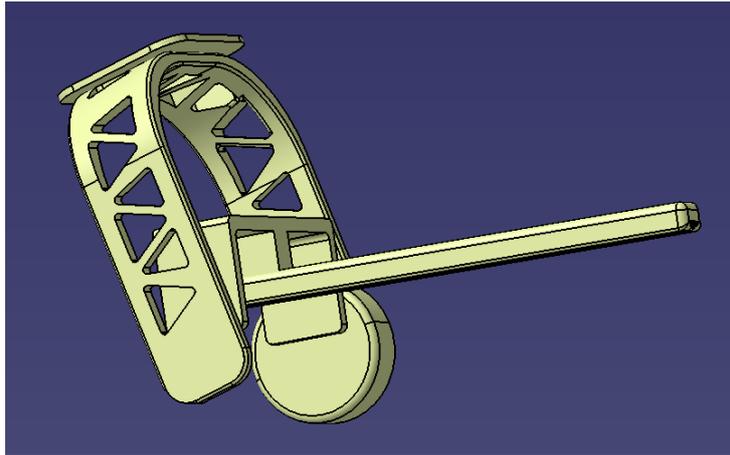
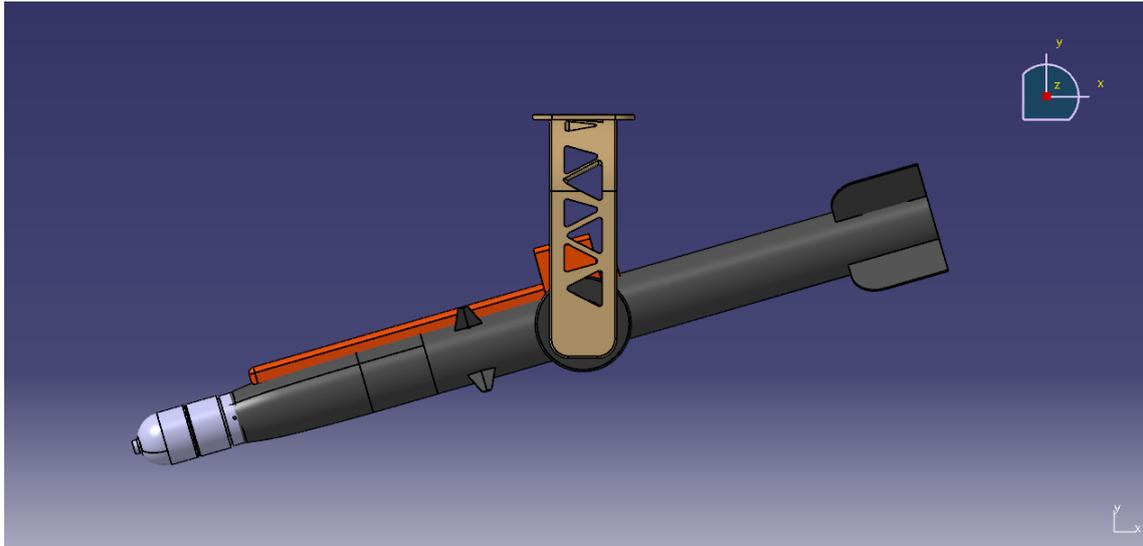


Figure 3.73: Weapon Release System A





### 3.3.5 Design of Weapon Release System B

Weapon Release system B drops the missile. This system can be used for Missile Version 4 where launch with initial guide angle is not required.

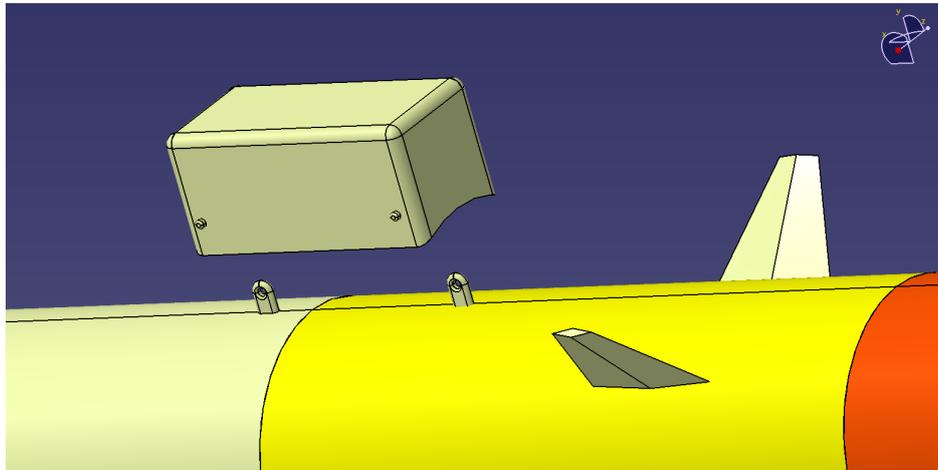
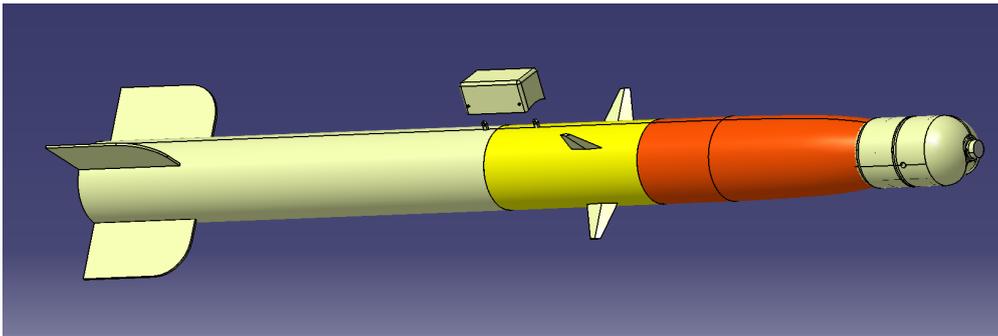
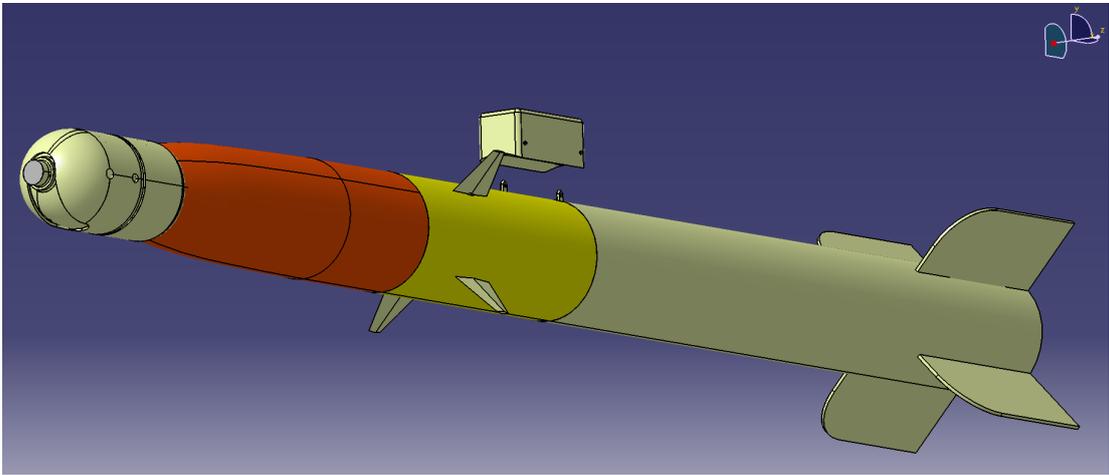
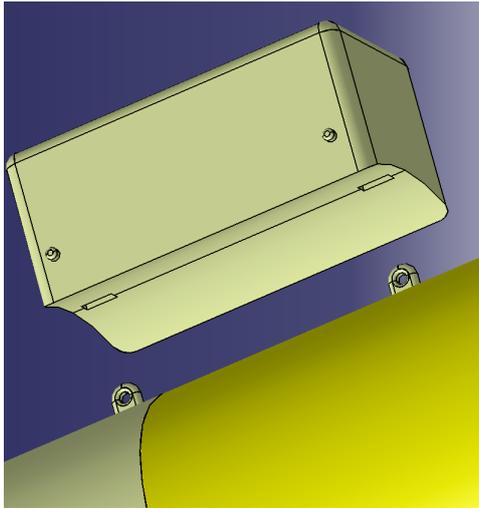


Figure 3.74: Weapon Release System B



## CHAPTER 4

# TRAJECTORY SIMULATION & PREDICTION METHODOLOGY

### 4.1 STABILITY ANALYSIS

The stability is the tendency of the rocket to return to its equilibrium position after it has been disturbed. The disturbance may be generated by the thrust action or atmospheric phenomena. The atmospheric disturbance can be wind gusts, wind gradients, or turbulent air.

The stability analysis begins with the defining the equilibrium. If a rocket is to remain in steady uniform flight, the resultant force as well as the resultant moment about the centre of gravity (CG) must be equal to zero. A rocket satisfying this requirement is said to be in equilibrium. On the other hand, if the forces and moment do not sum to zero, the rocket will be subjected to translational and rotational acceleration.

The subject of stability is divided into static and dynamic stability. Static stability is the initial tendency of the vehicle to return to its equilibrium state after a disturbance. In dynamic stability we are concerned with the time history of the motion of the vehicle after it is disturbed from its equilibrium point.

### 4.2 STATIC STABILITY

Static stability is the initial tendency of the vehicle to return to its equilibrium state after a disturbance. The pitching, yawing and rolling moment coefficients are denoted as  $C_m$ ,  $C_n$ ,  $C_l$ . For this to happen, three conditions have to be satisfied :

1. Longitudinal static stability condition  $C_m\alpha < 0$ , this condition has to be satisfied by the horizontal tail.

2. Directional static Stability Condition  $C_n\beta > 0$ , this condition has to be satisfied by the vertical tail
3. Lateral static stability condition  $C_l\beta < 0$ , this condition has to be satisfied by vertical tail.

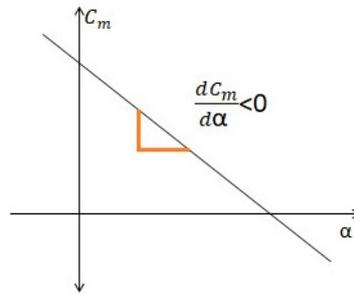


Figure 4.1: Longitudinal static Stability Condition

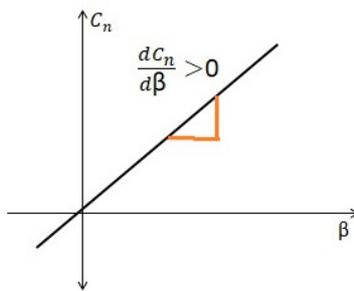


Figure 4.2: Directional static Stability Condition

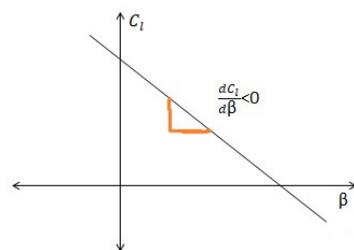


Figure 4.3: Lateral static stability condition

### 4.3 DYNAMIC STABILITY

If the rocket were disturbed from its equilibrium conditions. Note that the vehicle can be statically stable but dynamically unstable. Static stability, therefore does not guarantee dynamic stability. However, for the vehicle to be dynamically stable it must be statically stable.

- **Conservation of Linear Momentum Equations**

$$F_x - mg \sin \theta = m [\dot{u} + qw - rv] \quad (4.1)$$

$$F_y + mg \cos \theta \sin \phi = m [\dot{v} + ru - pw] \quad (4.2)$$

$$F_z + mg \cos \theta \cos \phi = m [\dot{w} + pv - qu] \quad (4.3)$$

Where  $F_x, F_y, F_z$  and  $u, v, w$  are the components of the force and velocity along the  $x, y$  and  $z$  axes respectively. The force components are composed of contributions due to the aerodynamic, propulsive and gravitational forces acting on the rocket.  $L, M, N$  are the components of the moment along the  $x, y$  and  $z$  axis respectively.  $m$  is mass of the rocket and  $g$  is the gravitational force.  $I_{xx}, I_{yy}$  and  $I_{zz}$  are the mass moment of inertia of the rocket about the  $x, y, z$  axis respectively. The term with the mixed indexes are called the product of inertial.

- **Conservation of Angular Momentum equations**

$$L = I_{xx}\dot{p} - I_{xz}\dot{r} + qr [I_{zz} - I_{yy}] - I_{xz}pq \quad (4.4)$$

$$M = I_{yy}\dot{q} + rq [I_{xx} - I_{zz}] + I_{xz} [p^2 - r^2] \quad (4.5)$$

$$N = -I_{xz}\dot{p} + I_{zz}\dot{r} + pq [I_{yy} - I_{xx}] + I_{xz}qr \quad (4.6)$$

- **Body Angular Velocities in terms of Euler Angles and Euler Rates (Navigation Equation)** The relationship between the angular velocities in the body frame  $p, q$  and  $r$  are roll, pitch and yaw rates. The Euler rates ( $\dot{\phi}, \dot{\psi}, \dot{\theta}$ ) are

$$p = \dot{\phi} - \dot{\psi} \sin \theta \quad (4.7)$$

$$q = \dot{\theta} \cos \phi + \dot{\psi} \cos \theta \sin \phi \quad (4.8)$$

$$r = \dot{\psi} \cos \theta \cos \phi - \dot{\theta} \sin \phi \quad (4.9)$$

Small disturbance theory is used in linearising the above equations. In applying the small disturbance theory we assume that the motion of rocket consists of small deviation about a steady flight condition. The term with the indexes '0' represents the reference value i.e steady state values. The linearised small-disturbance longitudinal and lateral rigid body

equation of motions are as follows [66]

• **Longitudinal Equations**

$$F_x - mg \sin \theta = m [\dot{u} + qw - rv] \quad (4.10)$$

$$F_z + mg \cos \theta \cos \phi = m [\dot{w} + pv - qu] \quad (4.11)$$

$$M = I_{yy}\dot{q} + rq [I_{xx} - I_{zz}] + I_{xz} [p^2 - r^2] \quad (4.12)$$

• **Lateral Equations**

$$F_y + mg \cos \theta \sin \phi = m [\dot{v} + ru - pw] \quad (4.13)$$

$$L = I_{xx}\dot{p} - I_{xz}\dot{r} + qr [I_{zz} - I_{yy}] - I_{xz}pq \quad (4.14)$$

$$N = -I_{xz}\dot{p} + I_{zz}\dot{r} + pq [I_{yy} - I_{xx}] + I_{xz}qr \quad (4.15)$$

**4.3.1 Stability Derivatives**

Stability Derivatives	
Lateral Directional	Longitudinal Stability
$Y_p = \frac{C_{y\beta t} \bar{q} S r_d}{mu_0}$	$X_u = \frac{[C_{Du} + 2C_{Do}] \bar{Q}_0 S}{mu_0}$
$Y_r = \frac{\bar{q} S C_{y\beta l_v}}{mu_0}$	$X_\alpha = \frac{\bar{Q}_0 S [-C_{D\alpha} + C_{Lss}]}{m}$
$Y_\beta = \frac{\bar{Q}_0 S C_{y\beta}}{m}$	$X_q = 0$
$L_p = -\frac{C_{L\alpha} \bar{Q}_0 C b^2}{12U_0 I_{xx}}$	$Z_u = -\frac{\bar{Q}_0 S [C_{Lu} + 2C_{Lss}]}{mu_0}$
$L_r = -\frac{\bar{Q}_0 S r_d C_{y\beta l_v}}{U_0 I_{xx}}$	$Z_q = -\frac{\bar{Q}_0 S l_t C_{L\alpha}}{mu_0}$
$L_\beta = \frac{\bar{Q}_0 S r_d C_{y\beta}}{I_{xx}}$	$Z_\alpha = -\frac{\bar{Q}_0 S [C_{L\alpha} + C_{Dss}]}{m}$
$N_p = \frac{\bar{Q}_0 S C_{y\beta} r_d l_v}{U_0 I_{zz}}$	$Z_q = -\frac{\bar{Q}_0 S \bar{c} C_{mu}}{I_{yy} u_0}$
$N_r = \frac{\bar{Q}_0 S l_v^2 C_{y\beta}}{U_0 I_{zz}}$	$M_\alpha = \frac{\bar{Q}_0 S \bar{c} C_{m\alpha}}{I_{yy}}$
$N_\beta = -\frac{\bar{Q}_0 S l_v C_{y\beta}}{I_{zz}}$	$M_q = -\frac{C_{L\alpha t} l_t^2 \bar{Q}_0 S}{u_0 I_{yy}}$

Table 4.1: Stability Derivatives

### 4.3.2 Aerodynamic Characteristics of Missile

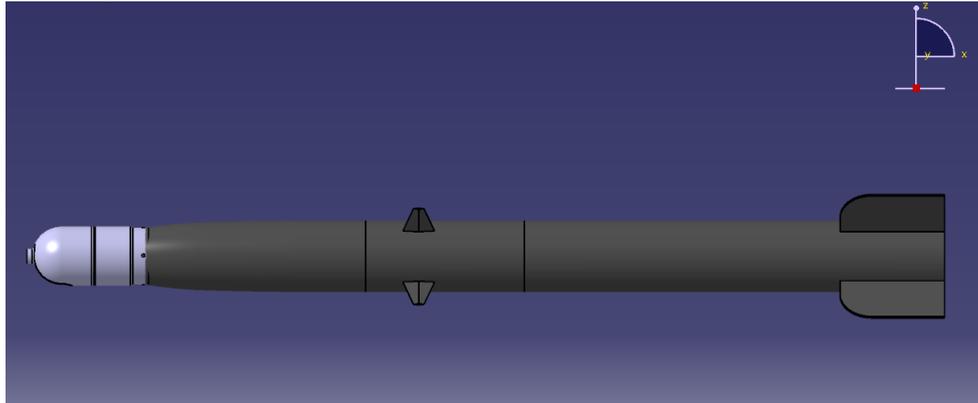
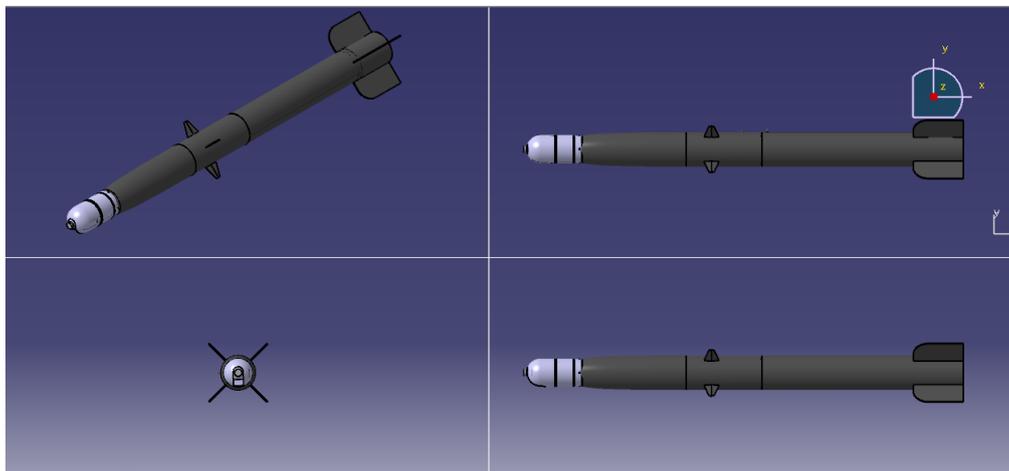


Figure 4.4: Missile Design



### Computational Simulation

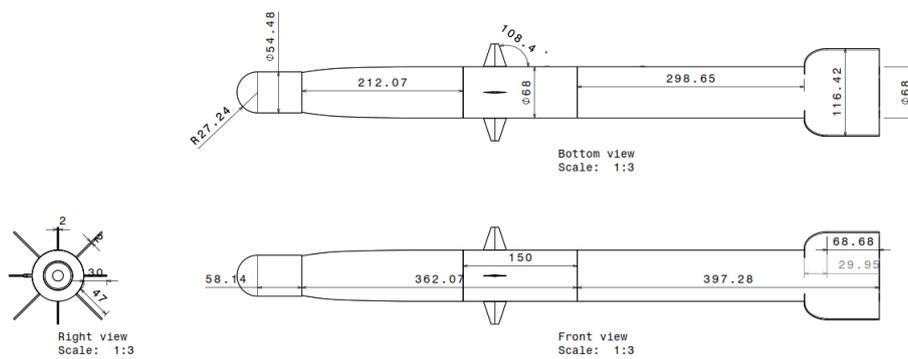
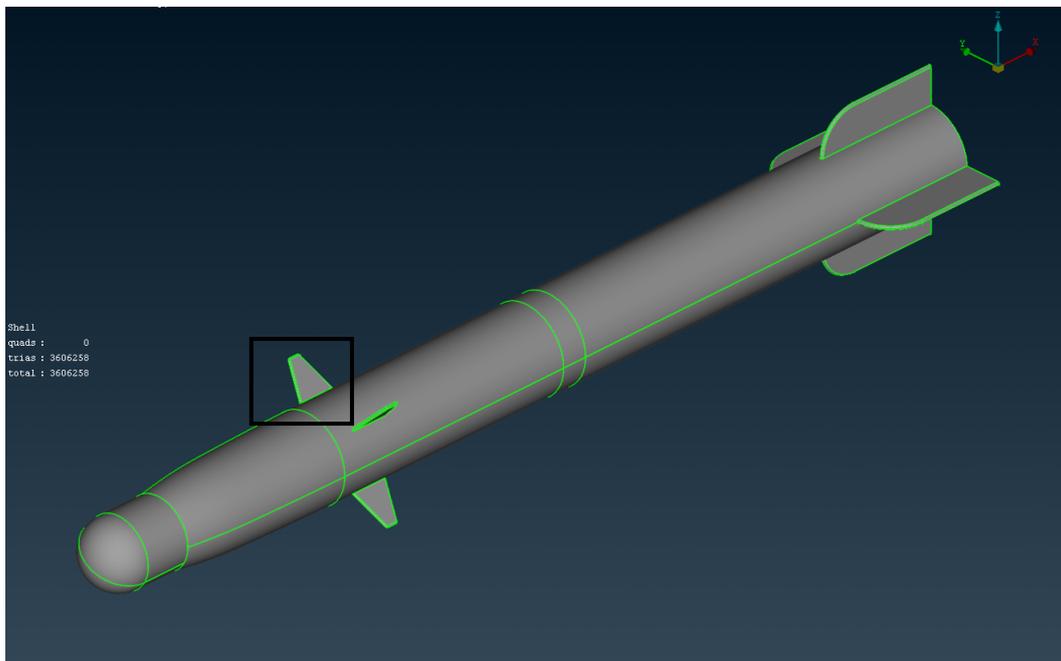
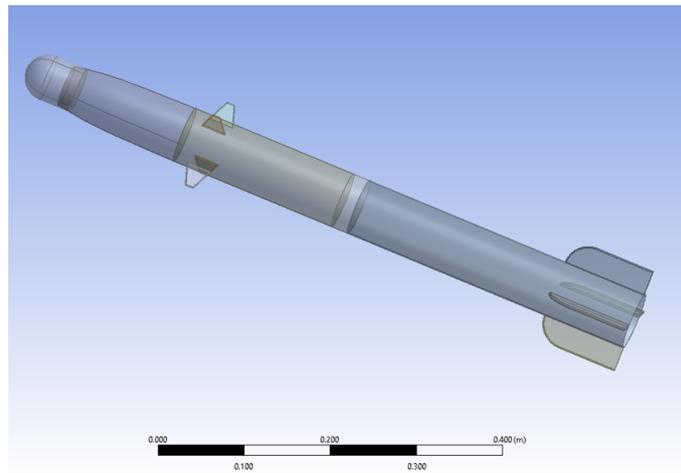
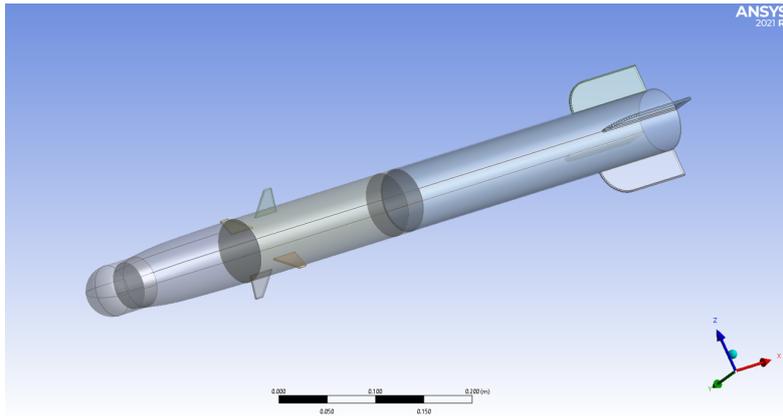
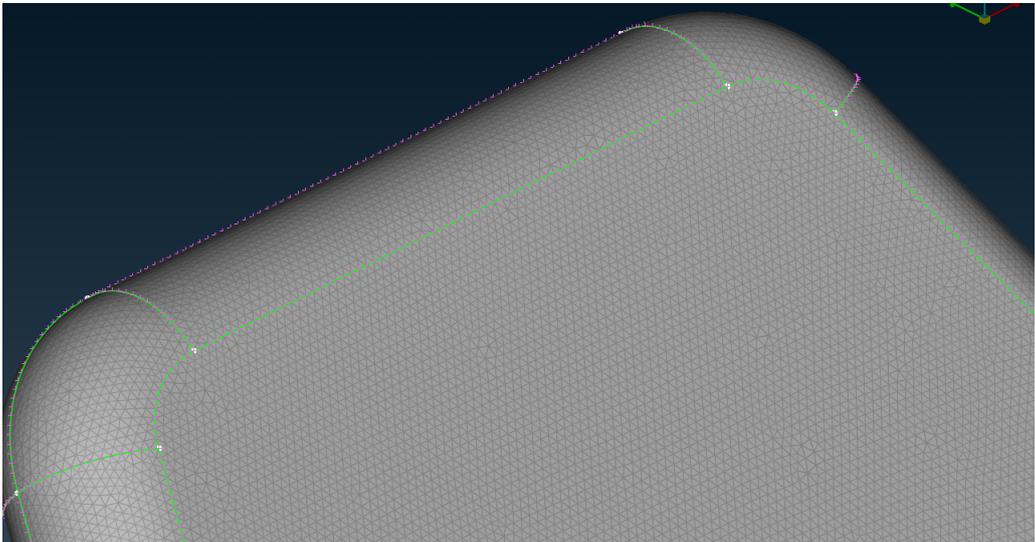
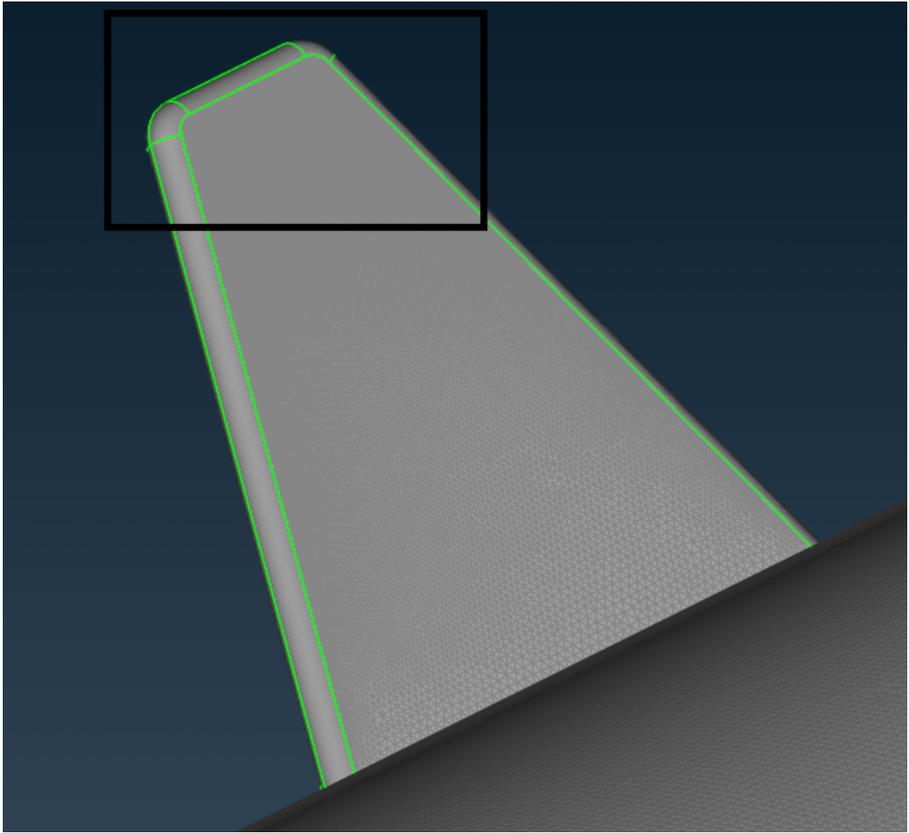
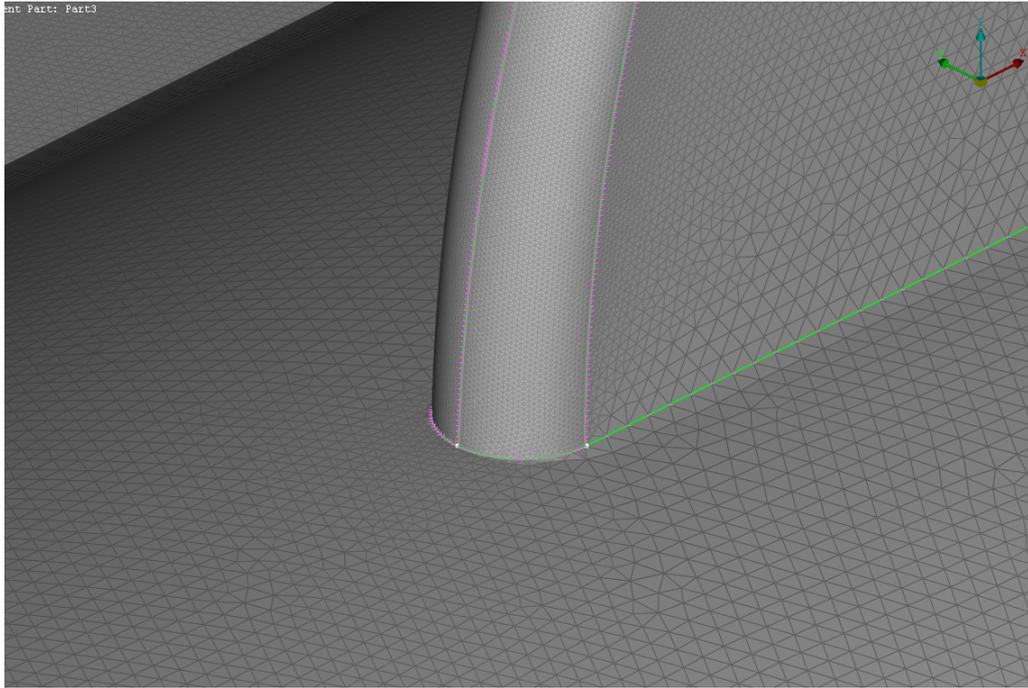


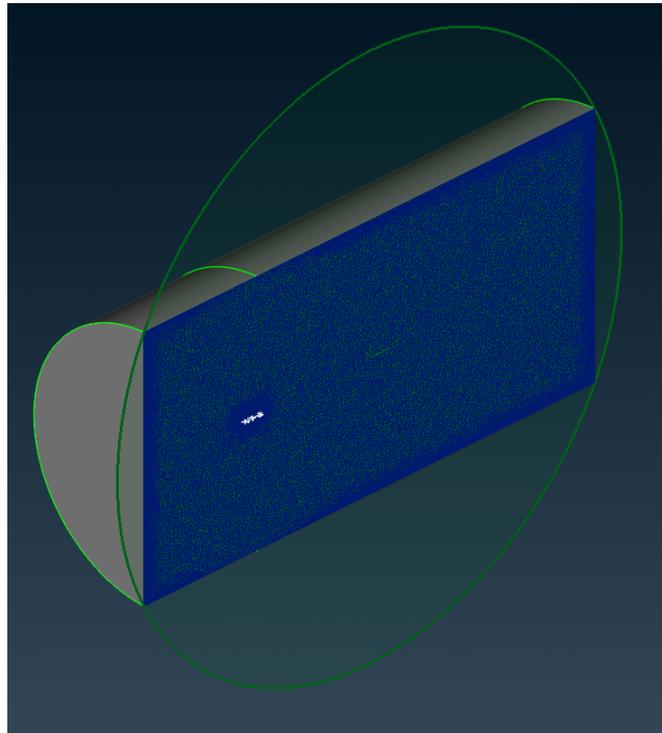
Figure 4.5: Missile CAD

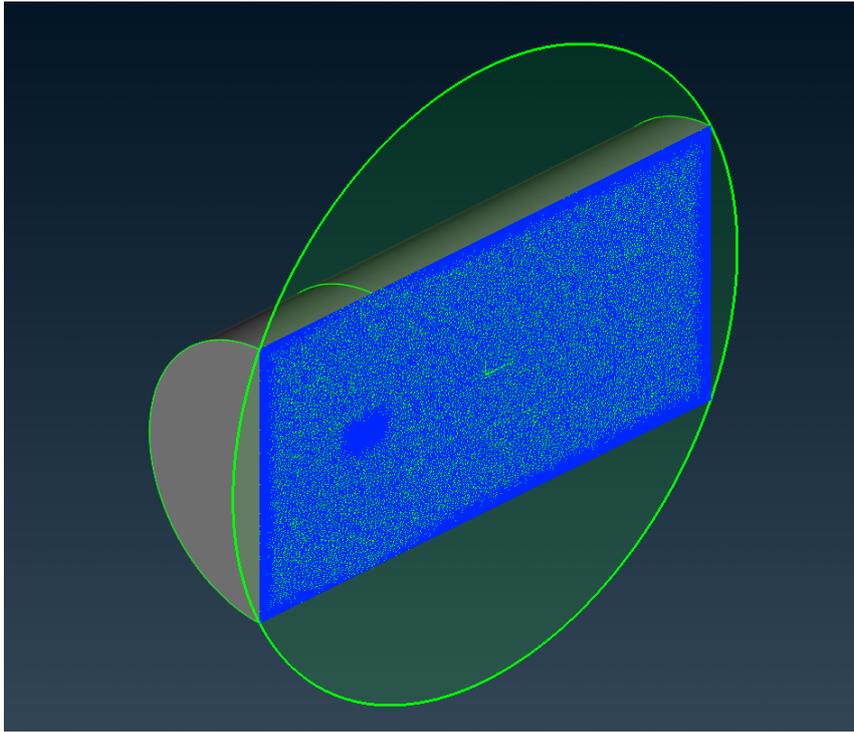


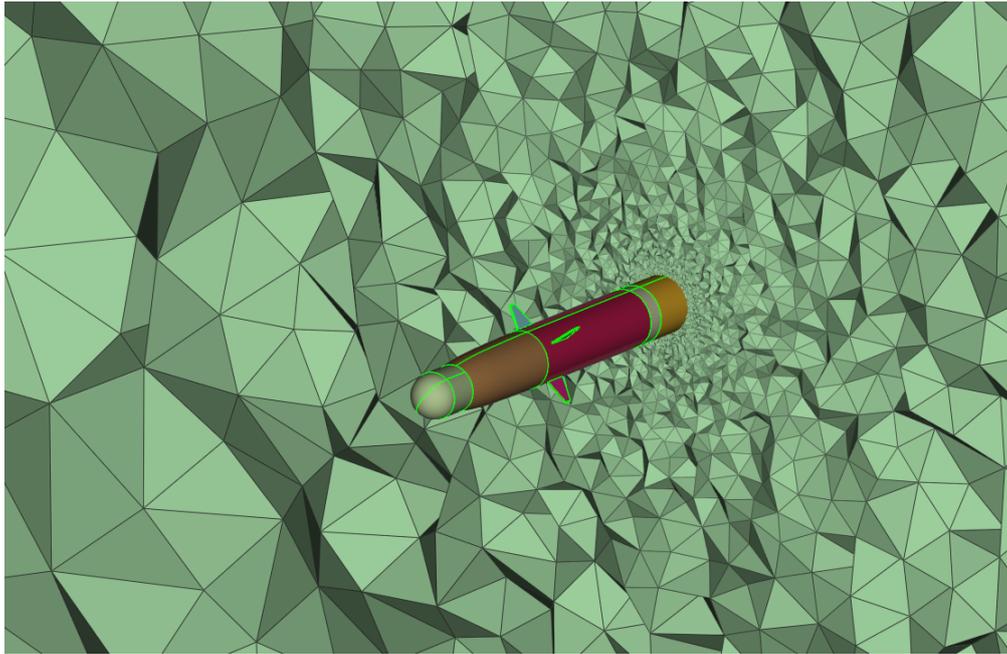




Surface mesh on missile body with 3606258 trias elements, 1034611 nodes.







Volume mesh on missile body with 65862454 tetras elements, 19079505 nodes.

The commercial CFD software Fluent 2021R1 by ANSYS Inc. was used for the simulations. In order to obtain the flow solution, Fluent is used to numerically solve the 3-D, viscous compressible, steady-state RANS equations. And the two equations SST  $K - \omega$  turbulence model is chosen to closure the RANS equations. For Solving these equations, pressure-based solver provided by FLUENT is selected. The coupled pressure-velocity coupling approach is employed to solve for all variables, and as a result it has higher accuracy. Simulation has been run for Mach number ranging from 0.3 to 1.6, for angle of attacks 0 to 20 degrees.

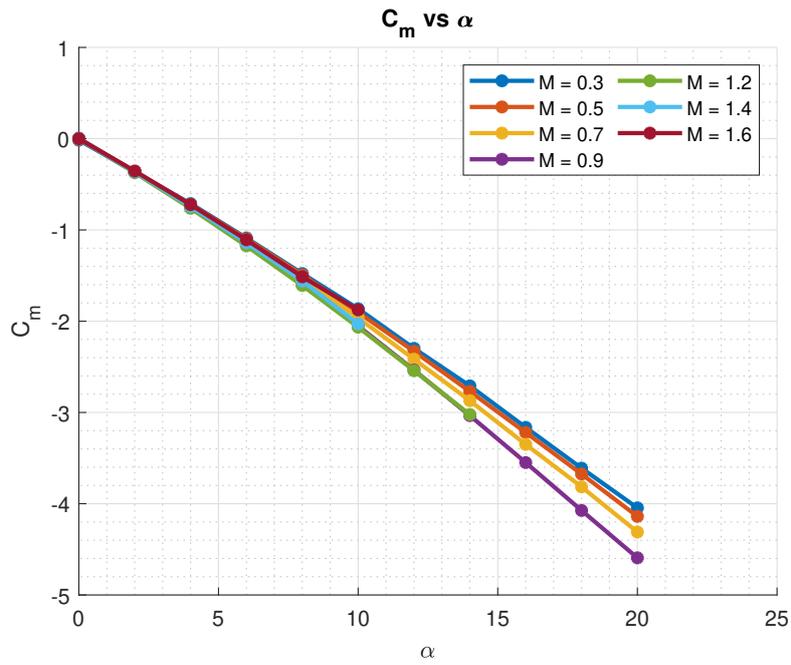


Figure 4.6:  $C_m$  vs  $\alpha$

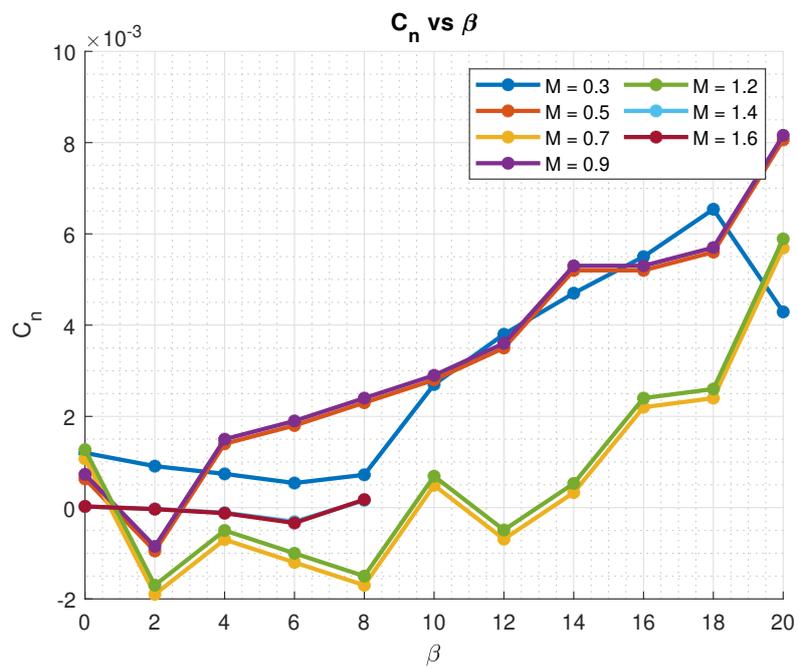


Figure 4.7:  $C_n$  vs  $\beta$

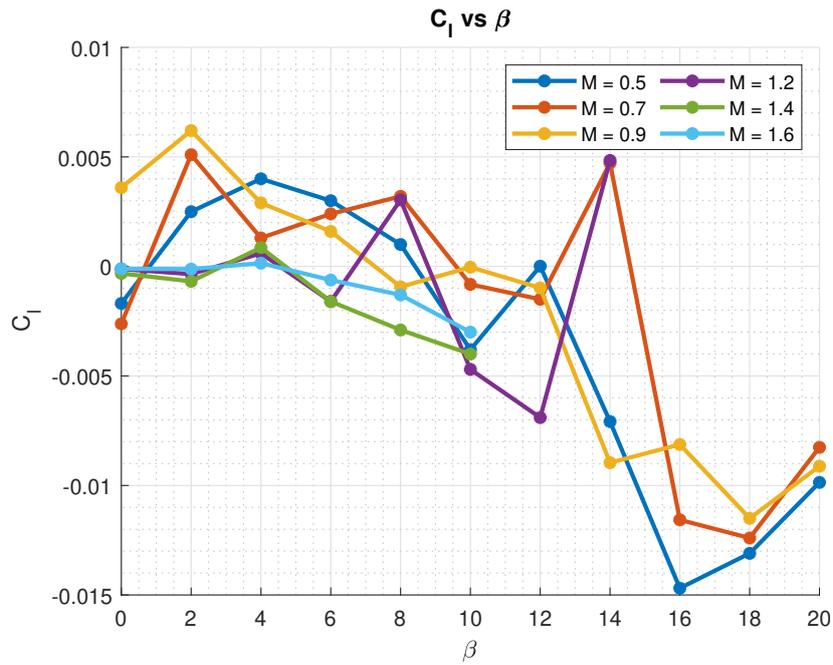


Figure 4.8:  $C_l$  vs  $\beta$

- \* Longitudinal static stability condition  $C_m\alpha < 0$  is satisfied in figure 4.6
- \* Directional static Stability Condition  $C_n\beta > 0$ , this condition is satisfied by the vertical tail, visually from figure 4.7
- \* Lateral static stability condition  $C_l\beta < 0$ , this condition is satisfied by vertical tail, from figure 4.8

#### 4.4 TRAJECTORY SIMULATION IN MATLAB

The equations of motions that describe the 6-DOF model is mentioned below which is used to do derive the trajectory 2 D simulation for Version 1, Version 2.

$$\begin{aligned}
F_x - mg \sin \theta &= m[\dot{u} + qw - rv] \\
F_y + mg \cos \theta \sin \phi &= m[\dot{v} + ru - pw] \\
F_z + mg \cos \theta \cos \phi &= m[\dot{w} + pv - qu] \\
L &= I_{xx}\dot{p} - I_{xz}\dot{r} + qr [I_{zz} - I_{yy}] - I_{xz}pq \\
M &= I_{yy}\dot{q} + rq [I_{xx} - I_{zz}] + I_{xz} [p^2 - r^2] \\
N &= -I_{xz}\dot{p} + I_{zz}\dot{r} + pq [I_{yy} - I_{xx}] + I_{xz}qr
\end{aligned} \tag{4.16}$$

$$m \frac{dV}{dt} = T - D - mg \sin \gamma \tag{4.17}$$

$$\frac{dV}{dt} = \frac{(T - D - mg \sin \gamma)}{m} \tag{4.18}$$

$$m \frac{dV_t}{dt} = L - mg \cos \gamma \tag{4.19}$$

$$m \frac{d}{dt}(\gamma\omega) = L - mg \cos \gamma \tag{4.20}$$

$$\frac{d(\gamma\omega)}{dt} = \frac{d\gamma}{dt}\omega + \frac{d\omega}{dt}\gamma \tag{4.21}$$

$\frac{d\omega}{dt}$  tends to zero

$$mV \frac{d\gamma}{dt} = L - mg \cos \gamma \tag{4.22}$$

$$\frac{d\gamma}{dt} = \frac{L - mg \cos \gamma}{mv} \tag{4.23}$$

$$\frac{dx}{dt} = V \cos \gamma \quad (4.24)$$

$$\frac{dy}{dt} = V \sin \gamma \quad (4.25)$$

## ODE 45

MATLAB's standard solver for ordinary differential equations (ODEs) is the function `ode45`. This function implements a Runge-Kutta method with a variable time step for efficient computation. `ode45` is designed to handle the following general problem

$$\frac{d\mathbf{x}}{dt} = \mathbf{f}(t, \mathbf{x}), \quad \mathbf{x}(t_0) = \mathbf{x}_0 \quad (4.26)$$

where  $t$  is the independent variable,  $\mathbf{x}$  is a vector of dependent variables to be found and  $\mathbf{f}(t, \mathbf{x})$  is a function of  $t$  and  $\mathbf{x}$ . The mathematical problem is specified when the vector of functions on the right-hand side of Eq. (4.26),  $\mathbf{f}(t, \mathbf{x})$ , is set and the initial conditions,  $\mathbf{x} = \mathbf{x}_0$  at time  $t_0$  are given.

### 4.4.1 Version 1

Using, ODE45 for equations (4.18), (4.23), (4.24), (4.25), given the initial conditions, It is possible to find all the possible  $x, y, u, v, \gamma$  datasets in a matrix., Now for a possible range of  $\gamma$  from  $-\pi/2$  to  $+\pi/2$ , we can find optimum value of  $\gamma_{required}$  inserting the required final position  $(x_f, y_f)$  in ODE45 run. This  $\gamma_{required}$  is the value that is needed depression angle, to launch missile to reach the required range, and to hit the target.

The code is given in Appendix B.3

To the given Matlab code, when given range value, it returns the angle of depression required for the desired trajectory. Also returns the trajectory graphs.

The figure 4.9 is a trajectory obtained when the input given to matlab code is,, that we launch from 800 meter altitude, for the target range of 1400 meter. Then, Matlab returns the output as " Therefore gamma required for the given range of 1400 is -14.8969 "

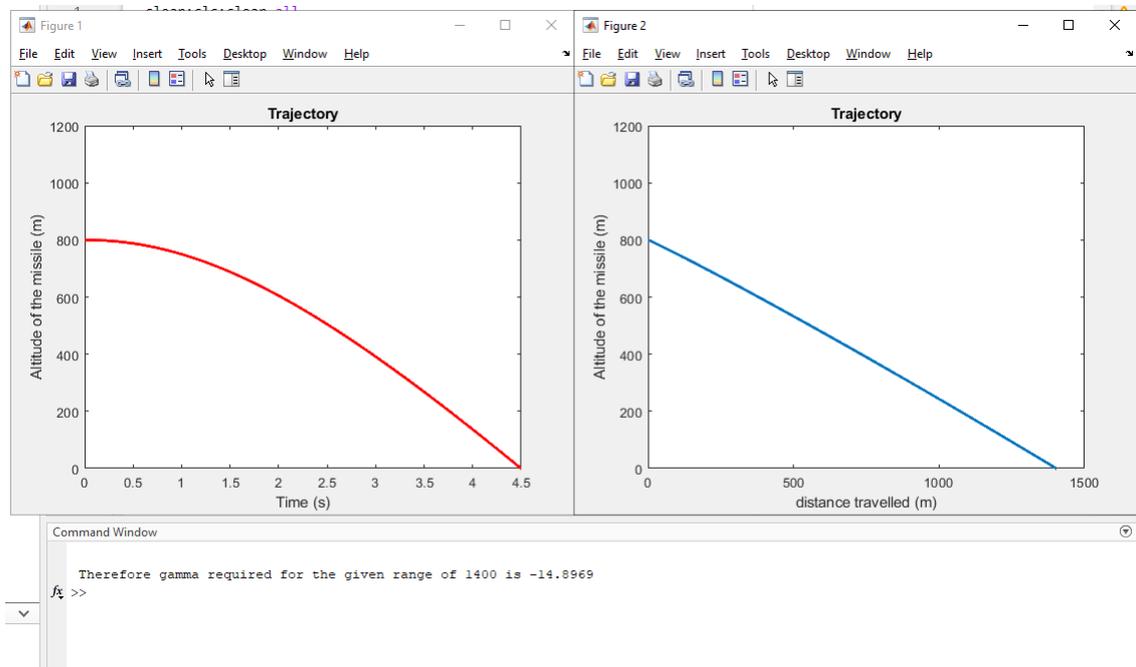


Figure 4.9: Version 1.0 : Trajectory

#### 4.4.2 Version 2

Expected Trajectory is shown in figure 4.10

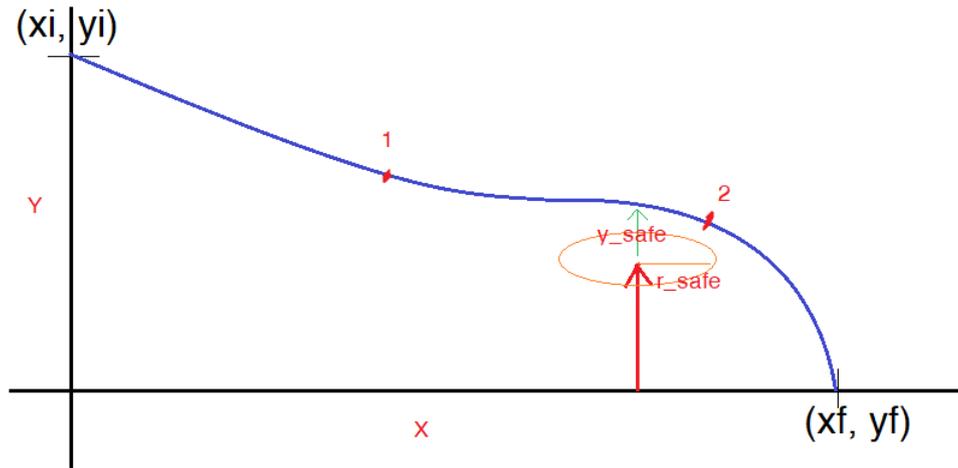


Figure 4.10: Caption

1. Find the optimal gamma to reach the safe point 1
2. Find the  $C_l$  of canards required to apply for 0.5 seconds to turn the missile, such that the gamma at end of turn equals zero is found, and applied
3. Find the  $C_l$  of canards required to apply for 0.5 seconds to change the gamma to a value, at the end of 0.5 seconds, which will lead the rest un-powered projectile path to intersect at target location

The Matlab code for the respective logic is attached in appendix B.4.

Checking matlab code

Input

1. Obstacle (650,350)
2. Radius of Obstacle = 100 meter
3.  $X_0, Y_0 = (950,0)$
4. Target  $(X,Y) = (830,0)$

Output from code

1. Initial gamma = -16 degree
2. Intermediate gamma = 0 degree
3. Final gamma = -32 degree
4. 0.5 seconds, we had Cl of 0.025 for 1st Turn. For First turn 1,3 canard deflection, = 14 degree
5. 0.5 seconds, we had Cl of 0.035 for 2nd turn. For Second turn 1,3 canard deflection, = -23 degree
6. The figure 4.11 is a trajectory obtained

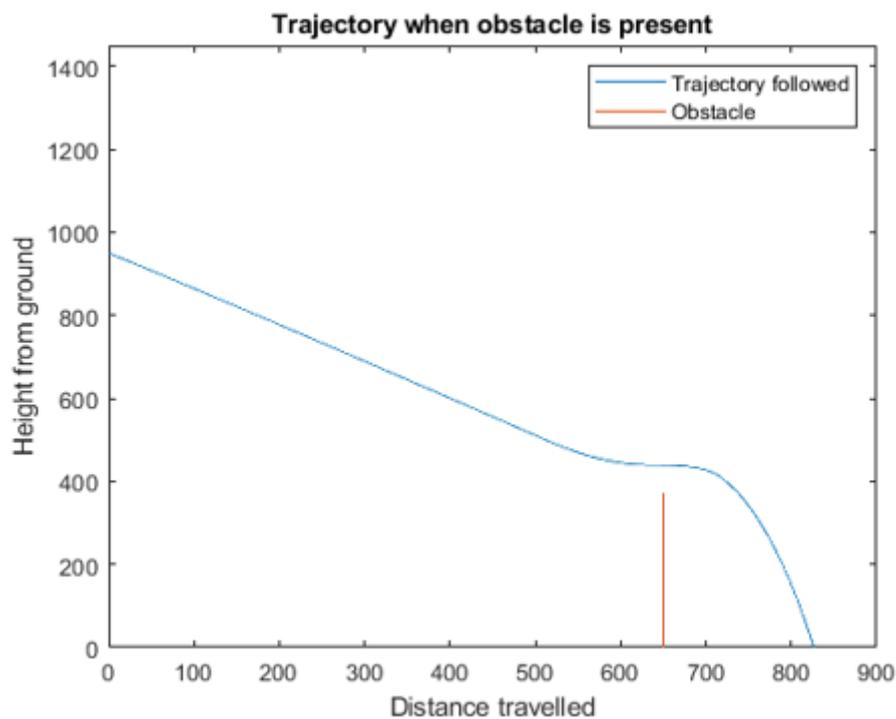


Figure 4.11: Version 2.0 : Trajectory

#### 4.5 TRAJECTORY PREDICTION USING ARTIFICIAL INTELLIGENCE

The traditional method used for trajectory predictions use models and numerical integration, which requires a lot of computing resources. Even though missile guidance [68] is a well-studied focus, conventional algorithms [69] underperform when the target is rapidly changing direction simultaneously exerting tremendous acceleration. [67]

### 4.5.1 Artificial Intelligence

Artificial Intelligence (AI) is the science and engineering of making intelligent machines, especially intelligent computer programs. It is related to the similar task of using computers to understand human intelligence. It combines computer science and robust datasets, to enable problem-solving.[70]

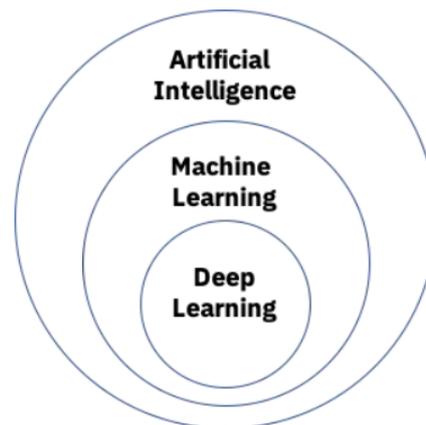


Figure 4.12: Design of Conventional Deep Neural Networks

It also encompasses sub-fields of machine learning and deep learning, which are frequently mentioned in conjunction with artificial intelligence. These disciplines are comprised of AI algorithms which seek to create expert systems which make predictions or classifications based on input data.

### 4.5.2 Machine Learning

Machine Learning (ML) is the field of AI that gives computers the capability to learn from past experiences without being explicitly programmed. ML is one of the most exciting technologies that one would have ever come across. As it is evident from the name, it gives the [71]computer that makes it more similar to humans. Various ML algorithms are utilized in this work to compare and contrast the trajectory predictions with DL algorithms.[72]

### **4.5.3 Deep Learning**

DL is a subset of AI and ML that drives many AI applications and services that improve automation, performing analytical and physical tasks without human intervention. DL distinguishes itself from classical ML by the type of data that it works with and the methods in which it learns.

DL is an important element of data science, which includes statistics and predictive modeling. It is extremely beneficial for tasks that includes collecting, analyzing and interpreting large amounts of data as DL makes this process faster [73]and easier. At its simplest, DL can be thought of as a way to automate predictive analytics. While traditional ML algorithms are linear, DL algorithms are stacked in a hierarchy of increasing complexity and abstraction.

It eliminates some of data pre-processing that is typically involved with ML. Then, through the processes of gradient descent and forward propogation or backpropagation, the DL algorithm adjusts [74]and fits itself for accuracy, allowing it to make predictions about a trejectory with increased precision.

### **4.5.4 Deep Neural Network**

Deep Neural Networks (DNN) consist of multiple layers of interconnected nodes, each building upon the[75] previous layer to refine and optimize the prediction or categorization. This progression of computations through the network is called forward propagation. The input and output layers of a deep neural network are called visible[77] layers. The input layer is where the deep learning model ingests the data for processing, and the output layer is where the final prediction or classification is made.[76]

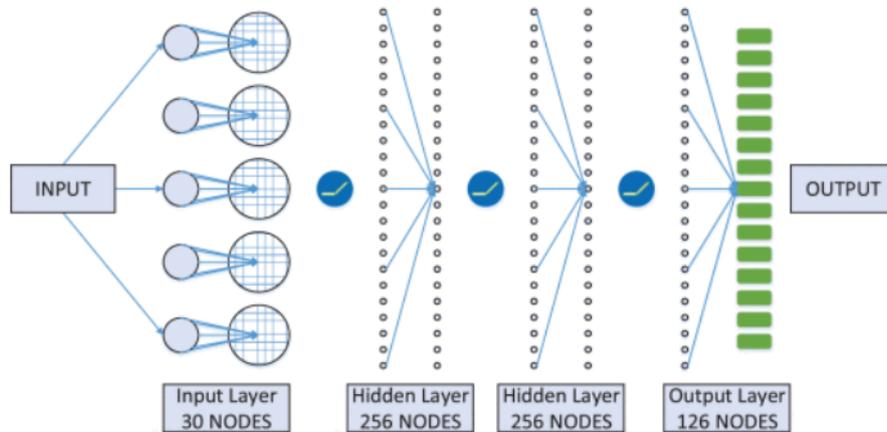


Figure 4.13: Design of Conventional Deep Neural Networks

Another process called backpropagation uses algorithms, like gradient descent, to calculate errors in predictions and then adjusts the weights and biases of the function by moving backwards through the layers in an effort to train the model. Together, forward[78] propagation and backpropagation allow a neural network to make predictions and correct for any errors accordingly. Over time, the algorithm becomes gradually more accurate.[79]

#### 4.5.5 Model Input & Output

Since the missile's flight trajectory is continuous, the network's input should include the present[80] point as well as numerous points prior to it, allowing the DNN to learn the changing law of the flight trajectory. To make continuous fitting of the DNN easier, the output of the DNN should likewise be a collection of continuous points derived backward from the current point. The network's input is set to the position[81] and velocity of the current time point and the four points preceding it. The network's output is the position and speed of the next time point, as well as the next 25 points.

#### 4.5.6 Dataset Description

To work with ML or DL, we need a huge amount of data, because, without the data, one cannot train AI models. Collecting and preparing the dataset is one of the most crucial parts while creating an ML/AI prediction. A dataset is a collection of data in which data is arranged in some order. A tabular dataset can be understood as a database table or matrix, where each column corresponds to a particular variable, and each row corresponds to the fields of the dataset. The most supported file type for a tabular dataset is "Comma Separated File," or CSV. The dataset comprises various fields related to missile trajectories and aerodynamics. The features considered are time  $t$ , altitude  $h$ , propulsive thrust  $T$ , time step  $t$ , flight path angle  $\gamma$ , time derivative  $T$ , velocity  $V$  in  $u$ ,  $v$ , and  $w$ , acceleration  $A$  in  $x$ ,  $y$ , and  $z$  direction. pitch, roll, yaw, roll rate, pitch rate and yaw rate respectively.

#### 4.5.7 Other Algorithms Adopted for Comparison

##### Random Forest Regressor

The random forest model[84] is a type of added substance model that makes forecasts by combining choices from many base models. Each base classifier in this case is a decision tree. Model ensembling refers to the broad process of combining many models to improve [82]predictive performance. All of the basic models in arbitrary sequence are produced independently using a different sub-test of the information. We used the sklearn package to import Rando nForest Regressor and computed the provided scores for comparison.[83]

##### XGB Regressor

XGB regression is an abbreviation for Extreme Gradient Boosting, also known as XGBoost. XGboost is an ensemble model approach to tackle problems with classification or regression forecasting. Ensembles are built using decision tree models. Each trees are added in the ensemble model to rectify misclassification rate produced[85] by previous models. To fit models, any arbitrarily discrete error rate and the optimization approach

are utilised. XGBoost dominates structural datasets when it comes to regression and classification predictive modelling.[86]

### **Linear regression**

The most elementary regression process is linear regression, which demands us to determine the predictive  $y$  [87] coordinate from the input  $x$ . A linear regression model assumes a straight-line between both the average value of the output and the [88] value of the input variable. Parameters are almost always undetermined and should be deduced from data.[89]

### **Lasso Regression**

The abbreviation Least Absolute Shrinkage and Selection Operator (LASSO) stands for Least Absolute Shrinkage and Selection Operator. Regularisation is a form of Lasso regression.[90] It is favoured over regression techniques for more accurate forecasting.[91] This model capitalises on shrinking. This type of regression is suitable for models with a significant level of multivariate regression or when you want to automate certain portions of model evaluation, such as parameter elimination.[92] Lasso Regression employs the L1 regularisation approach. It is used when there are a huge number of features since it automatically selects features.[93]

### **Logistic Regression**

Logistic regression (LR) is a statistical technique that, like linear regression, [94] finds an expression which forecasts an occurrence for a categorical variable depending across one or even more output responses. To forecast group [95] membership, LR uses the logarithmic odds ratio instead of probabilities, and the resultant model is built using an incremental expectation - maximization approach.[96] It has always been the case that the application of the approach (and how well it works, for example, the classification error) takes precedence above statistical assumptions.[97]

## 4.6 PERFORMANCE METRICS

The performance was analysed on the basis of various factors such as:

### **Mean Absolute Error**

Mean Absolute Error is the amount of error in your measurements. It is the difference between the measured value and “true” value. The Goal is to minimize the MAE.

### **Mean Squared Error**

Mean Squared Error (MSE) measures the average of the squares of the errors that is, the average of the squared difference between the estimated values and the actual value. MSE is a risk function, pointing to the value of expectation of the squared error loss. The Goal is to minimize the MSE.

### **R2-Score**

It is (total variance explained by model) / total variance. So if it is 100, the two variables are perfectly, i.e., with no variance at all. A low value would show a minimum correlation, meaning a regression model that is not valid, but not in all cases. Lower the R2 score the more accurate the model will be and that is not valid in all cases.

#### 4.6.1 Result Analysis

<b>Methods</b>	<b>MAE</b>	<b>MSE</b>	<b>R2 Score</b>
<b>Random Forest</b>	0.64986	0.6160	0.7355
<b>SVM</b>	0.7648	0.6558	0.3771
<b>XGB</b>	0.2162	0.5148	0.1096
<b>DNN</b>	0.9974	0.1450	0.3912
<b>Linear Regression</b>	0.4952	0.3586	0.3942
<b>Lasso Regression</b>	0.6416	0.4458	0.2021
<b>Logistic Regression</b>	0.5002	0.9874	0.3771

Table 4.2: Performance analysis of intelligent models

From the above table, it is evident that DNN outperforms all the state-of-art algorithms by achieving lowest error rate. Thus the predicted trajectory will be the best one for the missile to reach the target.

# CHAPTER 5

## CONCLUSION

1. Solid Rocket motor V2.0 for the range of 2000 m with  $\Delta\theta < 45$  deg with thrust of 1000 N for 2.5 s burnout is designed.
2. Warhead payload profile is designed, for 2500 gram and 2100 gram, and named WP V 2.0, and WP V 3.0 respectively
3. Implemented : Optimising structural weight without compromising on performance : Carbon composite material selected for Missile frame, to provide same strength as that of aluminum alloy, with 50 percent less weight than aluminum alloy
4. Successfully passed hydrotest for the material selected to validate the maximum pressure Rocket Motor case can handle, and it is found the material withstands 50 bar
5. Nozzle throat Rocket motor igniter is selected
6. Matlab code developed for, Trust calculation using the Pressure data obtained in firing of propellant using BEM
7. 2 Canard mechanism designed and fabricated
8. Custom 2 axis gimbal for missile has been designed with lot of iterations, for the missile.
9. Stability analysis of Missile is calculated and found missile is statically stable.
10. Design of Ground Launcher, Hand Launcher, Weapon Release System A and Weapon Release System B is complete
11. FPGA Architecture achitecture is studied and found that FPGA methodology is the best for tracking development of missile version 4.0
12. Studied and finalised Sensors, Single Board Computers (SBC), Carrier circuit, and python code for csrt tracking with pan-tilt servo configuration is implemented
13. Trajectory Simulation is done using matlab for version 1, version 2
14. Trajectory Prediction using Machine Learning and Deep Learning is implemented.

## **5.1 FUTURE SCOPE**

1. Fabrication, Assembling and Testing can be conducted for the designed models. Key variables at each stage can be validated in real field
2. Further development can be based on real field validation, The data obtained can be used for further simulations
3. Coding can be developed using FPGA architecture for Tracking

# APPENDIX A

## CEA ANALYSIS

### A.1 SRP V 2.0 CEA ANALYSIS REPORT

```
1
2 *****
3
4 NASA-GLENN CHEMICAL EQUILIBRIUM PROGRAM CEA2, MAY 21, 2004
5 BY BONNIE MCBRIDE AND SANFORD GORDON
6 REFS: NASA RP-1311, PART I, 1994 AND NASA RP-1311, PART II, 1996
7
8 *****
9
10
11
12 problem o/f=2.125,
13 rocket equilibrium frozen nfz=1 tcest,k=3800
14 p,bar=40,
15 sup,ae/at=4.23,
16 react
17 oxid=NH4CLO4(I) wt=68 t,k=300
18 fuel=AL(cr) wt=18 t,k=300
19 fuel=HTPB wt=14 t,k=300
20 h,kj/mol=-51.8 C 4 H 6
21 end
22
23 OPTIONS: TP=F HP=F SP=F TV=F UV=F SV=F DETN=F SHOCK=F REFL=F INCD=F
24 RKT=T FROZ=T EQL=T IONS=F SIUNIT=T DEBUGF=F SHKDBG=F DETDBG=F TRNSPT=F
25
26 TRACE= 0.00E+00 S/R= 0.000000E+00 H/R= 0.000000E+00 U/R= 0.000000E+00
27
28 Pc, BAR = 40.000000
29
30 Pc/P =
31
32 SUBSONIC AREA RATIOS =
33
34 SUPERSONIC AREA RATIOS = 4.2300
35
36 NFZ= 1 Mdot/Ac= 0.000000E+00 Ac/At= 0.000000E+00
37
38 REACTANT WT.FRAC (ENERGY/R),K TEMP,K DENSITY
39 EXPLODED FORMULA
40 O: NH4CLO4(I) 1.000000 -0.355439E+05 300.00 0.0000
41 N 1.00000 H 4.00000 CL 1.00000 O 4.00000
42 F: AL(cr) 0.562500 0.538838E+01 300.00 0.0000
43 AL 1.00000
44 F: HTPB 0.437500 -0.623007E+04 300.00 0.0000
45 C 4.00000 H 6.00000
46
47 SPECIES BEING CONSIDERED IN THIS SYSTEM
48 (CONDENSED PHASE MAY HAVE NAME LISTED SEVERAL TIMES)
```

49 LAST thermo.inp UPDATE: 9/09/04

50

51 g12/97 \*AL tpis96 ALC tpis96 ALC2

52 tpis96 ALCL tpis96 ALCL2 tpis96 ALCL3

53 tpis96 ALH tpis96 ALHCL tpis96 ALHCL2

54 tpis96 ALH2 tpis96 ALH2CL tpis96 ALH3

55 tpis96 ALN tpis96 \*ALO tpis96 ALOCL

56 tpis96 ALOCL2 tpis96 ALOH tpis96 ALOHCL

57 tpis96 ALOHCL2 tpis96 ALO2 tpis96 AL(OH)2

58 tpis96 AL(OH)2CL tpis96 AL(OH)3 tpis96 AL2

59 tpis96 AL2C2 tpis96 AL2CL6 tpis96 AL2O

60 tpis96 AL2O2 tpis96 AL2O3 g 7/97 \*C

61 g 8/99 CCL g 8/99 CCL2 n12/93 CCL3

62 tpis91 CCL4 tpis79 \*CH g 9/99 CHCL

63 n12/93 CHCL2 g 7/99 CHCL3 g 4/02 CH2

64 g12/99 CH2CL tpis91 CH2CL2 g 4/02 CH3

65 tpis91 CH3CL g11/00 CH2OH g 7/00 CH3O

66 g 8/99 CH4 g 7/00 CH3OH srd 01 CH3OOH

67 g 8/99 \*CN g12/99 CNN tpis79 \*CO

68 tpis91 COCL tpis91 COCL2 tpis91 COHCL

69 g 9/99 \*CO2 tpis91 COOH tpis91 \*C2

70 tpis91 C2CL g 5/02 C2CL2 tpis91 C2CL3

71 g 5/02 C2CL4 g 5/02 C2CL6 g 6/01 C2H

72 g 5/02 C2HCL g 5/02 C2HCL3 g 1/91 C2H2, acetylene

73 g 5/01 C2H2, vinylidene tpis91 C2H2CL2 g 4/02 CH2CO, ketene

74 g 3/02 O(CH)2O srd 01 HO(CO)2OH g 7/01 C2H3, vinyl

75 g 5/02 C2H3CL srd 01 CH2CL-COOH g 9/00 CH3CN

76 g 6/96 CH3CO, acetyl g 1/00 C2H4 g 8/88 C2H4O, ethylen-o

77 g 8/88 CH3CHO, ethanal g 6/00 CH3COOH srd 01 OHCH2COOH

78 g 7/00 C2H5 g 7/00 C2H6 g 8/88 CH3N2CH3

79 g 8/88 C2H5OH g 7/00 CH3OCH3 srd 01 CH3O2CH3

80 g 7/00 CCN tpis91 CNC srd 01 OCCN

81 tpis79 C2N2 g 8/00 C2O tpis79 \*C3

82 n 4/98 C3H3, 1-propynl n 4/98 C3H3, 2-propynl g 2/00 C3H4, allene

83 g 1/00 C3H4, propyne g 5/90 C3H4, cyclo- g 3/01 C3H5, allyl

84 g 2/00 C3H6, propylene g 1/00 C3H6, cyclo- g 6/01 C3H6O, propylox

85 g 6/97 C3H6O, acetone g 1/02 C3H6O, propanal g 7/01 C3H7, n-propyl

86 g 9/85 C3H7, i-propyl g 2/00 C3H8 g 2/00 C3H8O, 1propanol

87 g 2/00 C3H8O, 2propanol srd 01 CNCOCN g 7/88 C3O2

88 g tpis \*C4 g 7/01 C4H2, butadiyne g 8/00 C4H4, 1,3-cyclo-

89 n10/92 C4H6, butadiene n10/93 C4H6, 1butyne n10/93 C4H6, 2butyne

90 g 8/00 C4H6, cyclo- n 4/88 C4H8, 1-butene n 4/88 C4H8, cis2-buten

91 n 4/88 C4H8, tr2-butene n 4/88 C4H8, isobutene g 8/00 C4H8, cyclo-

92 g10/00 (CH3COOH)2 n10/84 C4H9, n-butyl n10/84 C4H9, i-butyl

93 g 1/93 C4H9, s-butyl g 1/93 C4H9, t-butyl g12/00 C4H10, n-butane

94 g 8/00 C4H10, isobutane g 6/01 C4N2 g 8/00 \*C5

95 g 5/90 C5H6, 1,3cyclo- g 1/93 C5H8, cyclo- n 4/87 C5H10, 1-pentene

96 g 2/01 C5H10, cyclo- n10/84 C5H11, pentyl g 1/93 C5H11, t-pentyl

97 n10/85 C5H12, n-pentane n10/85 C5H12, i-pentane n10/85 CH3C(CH3)2CH3

98 g 2/93 C6H2 g11/00 C6H5, phenyl g 8/00 C6H5O, phenoxy

99 g 8/00 C6H6 g 8/00 C6H5OH, phenol g 1/93 C6H10, cyclo-

100 n 4/87 C6H12, 1-hexene g 6/90 C6H12, cyclo- n10/83 C6H13, n-hexyl

101 g 6/01 C6H14, n-hexane g 7/01 C7H7, benzyl g 1/93 C7H8

102 g12/00 C7H8O, cresol-mx n 4/87 C7H14, 1-heptene n10/83 C7H15, n-heptyl

103 n10/85 C7H16, n-heptane n10/85 C7H16, 2-methylh n 4/89 C8H8, styrene

104 n10/86 C8H10, ethylbenz n 4/87 C8H16, 1-octene n10/83 C8H17, n-octyl

105 n 4/85 C8H18, n-octane n 4/85 C8H18, isooctane n10/83 C9H19, n-nonyl

106 g 3/01 C10H8, naphthale n10/83 C10H21, n-decyl g 8/00 C12H9, o-bipheny

107	g 8/00	C12H10, biphenyl	g 7/97	*CL	g 6/95	CLCN
108	tpis89	CLO	g 7/93	CLO2	tpis89	CL2
109	tpis89	CL2O	g 6/97	*H	tpis96	HALO
110	tpis96	HALO2	g 6/01	HCN	g 1/01	HCO
111	tpis89	HCCN	g 6/01	HCCO	tpis89	HCL
112	g 6/01	HNC	g 7/00	HNCO	g10/01	HNO
113	tpis89	HNO2	g 5/99	HNO3	g 1/01	HOCL
114	g 4/02	HO2	tpis78	*H2	g 5/01	HCHO, formaldehy
115	g 6/01	HCOOH	g 8/89	H2O	g 6/99	H2O2
116	g 6/01	(HCOOH)2	g 5/97	*N	g 6/01	NCO
117	g 4/99	*NH	g 3/01	NH2	tpis89	NH3
118	tpis89	NH2OH	tpis89	*NO	g 4/99	NOCL
119	g 4/99	NO2	g 4/99	NO2CL	j12/64	NO3
120	tpis78	*N2	g 6/01	NCN	g 5/99	N2H2
121	tpis89	NH2NO2	g 4/99	N2H4	g 4/99	N2O
122	g 4/99	N2O3	tpis89	N2O4	g 4/99	N2O5
123	tpis89	N3	g 4/99	N3H	g 5/97	*O
124	g 4/02	*OH	tpis89	*O2	g 8/01	O3
125	coda89	AL (cr)	coda89	AL (L)	tpis96	ALCL3 (cr)
126	tpis96	ALCL3 (L)	tpis96	ALH3 (a)	tpis96	ALN (cr)
127	tpis96	ALN (cr)	tpis96	ALN (L)	tpis96	ALN (L)
128	tpis96	AL (OH)3 (a)	tpis96	AL2O3 (a)	tpis96	AL2O3 (a)
129	tpis96	AL2O3 (a)	tpis96	AL2O3 (L)	tpis96	AL4C3 (cr)
130	tpis96	AL4C3 (cr)	n 4/83	C (gr)	n 4/83	C (gr)
131	n 4/83	C (gr)	g11/99	H2O (cr)	g 8/01	H2O (L)
132	g 8/01	H2O (L)	j 9/65	NH4CL (II)	j 9/65	NH4CL (III)
133	j 9/65	NH4CL (III)				

134  
135 O/F = 2.125000

137			EFFECTIVE FUEL	EFFECTIVE OXIDANT	MIXTURE		
138	ENTHALPY		h (2) /R	h (1) /R	h0/R		
139	(KG-MOL) (K) /KG		-0.50278394E+02	-0.30252904E+03	-0.22180883E+03		
140							
141	KG-FORM.WT./KG		bi (2)	bi (1)	b0i		
142	*N		0.00000000E+00	0.85114308E-02	0.57877729E-02		
143	*H		0.48529833E-01	0.34045723E-01	0.38680638E-01		
144	*CL		0.00000000E+00	0.85114308E-02	0.57877729E-02		
145	*O		0.00000000E+00	0.34045723E-01	0.23151092E-01		
146	*AL		0.20847588E-01	0.00000000E+00	0.66712283E-02		
147	*C		0.32353222E-01	0.00000000E+00	0.10353031E-01		
148							
149	POINT	ITN	T	N	H	CL	O
150			AL	C			
151	1	22	2568.230	-13.324	-8.923	-22.064	-20.511
152			-13.398	-10.874			
153	ADD	AL2O3 (L)					
154	1	6	3284.231	-13.785	-9.257	-20.497	-19.009
155			-16.449	-12.142			
156	Pinf/Pt =	1.731179					
157	2	4	3098.873	-13.947	-9.413	-20.825	-19.529
158			-16.947	-12.184			
159	Pinf/Pt =	1.733822					
160	2	2	3098.362	-13.947	-9.413	-20.826	-19.530
161			-16.948	-12.184			
162	3	5	2228.111	-14.644	-10.115	-22.834	-22.915
163			-21.423	-11.864			
164	PHASE CHANGE, REPLACE	AL2O3 (L)		WITH	AL2O3 (a)		

165	3	3	2397.704	-14.774	-10.242	-22.622	-22.069
166			-20.106	-12.549			
167	ADD	AL2O3 (L)					
168	3	3	2327.000	-14.721	-10.189	-22.704	-22.407
169			-20.676	-12.272			
170	3	3	2327.000	-14.684	-10.152	-22.666	-22.407
171			-20.676	-12.197			
172	3	2	2327.000	-14.683	-10.152	-22.666	-22.407
173			-20.676	-12.197			

174  
175  
176  
177  
178

THEORETICAL ROCKET PERFORMANCE ASSUMING EQUILIBRIUM

COMPOSITION DURING EXPANSION FROM INFINITE AREA COMBUSTOR

183 Pin = 580.2 PSIA  
184 CASE =

	REACTANT	WT FRACTION (SEE NOTE)	ENERGY KJ/KG-MOL	TEMP K
188	OXIDANT	NH4CLO4 (I)	1.0000000	-295529.716
189	FUEL	AL (cr)	0.5625000	44.802
190	FUEL	HTPB	0.4375000	-51800.000

191  
192 O/F= 2.12500 %FUEL= 32.000000 R, EQ. RATIO= 1.921799 PHI, EQ. RATIO= 2.659239  
193

	CHAMBER	THROAT	EXIT
195	Pinf/P	1.0000	1.7338
196	P, BAR	40.000	23.070
197	T, K	3284.23	3098.36
198	RHO, KG/CU M	4.0063 0	2.4678 0
199	H, KJ/KG	-1844.23	-2376.08
200	U, KJ/KG	-2842.66	-3310.95
201	G, KJ/KG	-33642.5	-32374.7
202	S, KJ/(KG) (K)	9.6821	9.6821
203			
204	M, (1/n)	27.350	27.556
205	MW, MOL WT	25.268	25.365
206	(dLV/dLP)t	-1.01518	-1.01146
207	(dLV/dLT)p	1.2853	1.2247
208	Cp, KJ/(KG) (K)	3.7669	3.4131
209	GAMMAS	1.1340	1.1378
210	SON VEL, M/SEC	1064.0	1031.4
211	MACH NUMBER	0.000	1.000

212  
213

PERFORMANCE PARAMETERS

215	Ae/At	1.0000	4.2300
216	CSTAR, M/SEC	1571.6	1571.6
217	CF	0.6562	1.4381
218	Ivac, M/SEC	1937.8	2565.0
219	Isp, M/SEC	1031.4	2260.2

220  
221  
222

MOLE FRACTIONS

223					
224	*AL	0.00016	0.00007	0.00000	
225	ALCL	0.00823	0.00545	0.00016	
226	ALCL2	0.00061	0.00039	0.00001	
227	ALCL3	0.00022	0.00019	0.00003	
228	ALH	0.00004	0.00002	0.00000	
229	ALHCL	0.00003	0.00001	0.00000	
230	ALHCL2	0.00006	0.00004	0.00000	
231	*ALO	0.00014	0.00006	0.00000	
232	ALOCL	0.00035	0.00021	0.00000	
233	ALOH	0.00456	0.00259	0.00005	
234	ALOHCL	0.00059	0.00032	0.00001	
235	ALOHCL2	0.00076	0.00055	0.00006	
236	AL(OH)2	0.00012	0.00005	0.00000	
237	AL(OH)2CL	0.00017	0.00010	0.00001	
238	AL(OH)3	0.00003	0.00002	0.00000	
239	AL2O	0.00009	0.00003	0.00000	
240	AL2O2	0.00002	0.00001	0.00000	
241	*CO	0.25407	0.25535	0.25781	
242	*CO2	0.00748	0.00722	0.00810	
243	*CL	0.00778	0.00646	0.00138	
244	CL2	0.00001	0.00001	0.00000	
245	*H	0.03062	0.02457	0.00470	
246	HALO2	0.00001	0.00000	0.00000	
247	HCN	0.00001	0.00001	0.00000	
248	HCO	0.00002	0.00001	0.00000	
249	HCL	0.12553	0.13172	0.14685	
250	*H2	0.32881	0.33699	0.35704	
251	H2O	0.07681	0.07243	0.06379	
252	NH2	0.00001	0.00000	0.00000	
253	NH3	0.00001	0.00001	0.00000	
254	*NO	0.00017	0.00009	0.00000	
255	*N2	0.07302	0.07334	0.07433	
256	*O	0.00016	0.00008	0.00000	
257	*OH	0.00312	0.00204	0.00016	
258	*O2	0.00001	0.00001	0.00000	
259	AL2O3(a)	0.00000	0.00000	0.03739	
260	AL2O3(L)	0.07613	0.07953	0.04812	
261					
262	* THERMODYNAMIC PROPERTIES FITTED TO 20000.K				
263					
264	PRODUCTS WHICH WERE CONSIDERED BUT WHOSE MOLE FRACTIONS				
265	WERE LESS THAN 5.000000E-06 FOR ALL ASSIGNED CONDITIONS				
266					
267	ALC	ALC2	ALH2	ALH2CL	ALH3
268	ALN	ALOCL2	ALO2	AL2	AL2C2
269	AL2CL6	AL2O3	*C	CCL	CCL2
270	CCL3	CCL4	*CH	CHCL	CHCL2
271	CHCL3	CH2	CH2CL	CH2CL2	CH3
272	CH3CL	CH2OH	CH3O	CH4	CH3OH
273	CH3OOH	*CN	CNN	COCL	COCL2
274	COHCL	COOH	*C2	C2CL	C2CL2
275	C2CL3	C2CL4	C2CL6	C2H	C2HCL
276	C2HCL3	C2H2, acetylene	C2H2, vinylidene	C2H2CL2	CH2CO, ketene
277	O(CH)2O	HO(CO)2OH	C2H3, vinyl	C2H3CL	CH2CL-COOH
278	CH3CN	CH3CO, acetyl	C2H4	C2H4O, ethylen-o	CH3CHO, ethanal
279	CH3COOH	OHCH2COOH	C2H5	C2H6	CH3N2CH3
280	C2H5OH	CH3OCH3	CH3O2CH3	CCN	CNC

281	OCCN	C2N2	C2O	*C3	C3H3,1-propynl
282	C3H3,2-propynl	C3H4,allene	C3H4,propyne	C3H4,cyclo-	C3H5,allyl
283	C3H6,propylene	C3H6,cyclo-	C3H6O,propylox	C3H6O,acetone	C3H6O,propanal
284	C3H7,n-propyl	C3H7,i-propyl	C3H8	C3H8O,1propanol	C3H8O,2propanol
285	CNCOCN	C3O2	*C4	C4H2,butadiyne	C4H4,1,3-cyclo-
286	C4H6,butadiene	C4H6,1butyne	C4H6,2butyne	C4H6,cyclo-	C4H8,1-butene
287	C4H8,cis2-buten	C4H8,tr2-butene	C4H8,isobutene	C4H8,cyclo-	(CH3COOH)2
288	C4H9,n-butyl	C4H9,i-butyl	C4H9,s-butyl	C4H9,t-butyl	C4H10,n-butane
289	C4H10,isobutane	C4N2	*C5	C5H6,1,3cyclo-	C5H8,cyclo-
290	C5H10,1-pentene	C5H10,cyclo-	C5H11,pentyl	C5H11,t-pentyl	C5H12,n-pentane
291	C5H12,i-pentane	CH3C(CH3)2CH3	C6H2	C6H5,phenyl	C6H5O,phenoxy
292	C6H6	C6H5OH,phenol	C6H10,cyclo-	C6H12,1-hexene	C6H12,cyclo-
293	C6H13,n-hexyl	C6H14,n-hexane	C7H7,benzyl	C7H8	C7H8O,cresol-mx
294	C7H14,1-heptene	C7H15,n-heptyl	C7H16,n-heptane	C7H16,2-methylh	C8H8,styrene
295	C8H10,ethylbenz	C8H16,1-octene	C8H17,n-octyl	C8H18,n-octane	C8H18,isoctane
296	C9H19,n-nonyl	C10H8,naphthale	C10H21,n-decyl	C12H9,o-biphenyl	C12H10,biphenyl
297	CLCN	CLO	CLO2	CL2O	HALO
298	HCCN	HCCO	HNC	HNCO	HNO
299	HNO2	HNO3	HOCL	HO2	HCHO,formaldehy
300	HCOOH	H2O2	(HCOOH)2	*N	NCO
301	*NH	NH2OH	NOCL	NO2	NO2CL
302	NO3	NCN	N2H2	NH2NO2	N2H4
303	N2O	N2O3	N2O4	N2O5	N3
304	N3H	O3	AL(cr)	AL(L)	ALCL3(cr)
305	ALCL3(L)	ALH3(a)	ALN(cr)	ALN(L)	AL(OH)3(a)
306	AL4C3(cr)	C(gr)	H2O(cr)	H2O(L)	NH4CL(II)
307	NH4CL(III)				

NOTE. WEIGHT FRACTION OF FUEL IN TOTAL FUELS AND OF OXIDANT IN TOTAL OXIDANTS

THEORETICAL ROCKET PERFORMANCE ASSUMING FROZEN COMPOSITION

P<sub>in</sub> = 580.2 PSIA

CASE =

	REACTANT	WT FRACTION (SEE NOTE)	ENERGY KJ/KG-MOL	TEMP K
322	OXIDANT NH4CLO4 (I)	1.0000000	-295529.716	300.000
323	FUEL AL(cr)	0.5625000	44.802	300.000
324	FUEL HTPB	0.4375000	-51800.000	300.000

O/F= 2.12500 %FUEL= 32.000000 R,EQ.RATIO= 1.921799 PHI,EQ.RATIO= 2.659239

	CHAMBER	THROAT
329	P <sub>inf</sub> /P	1.0000 1.7656
330	P, BAR	40.000 22.655
331	T, K	3284.23 3000.20
332	RHO, KG/CU M	4.0063 0 2.4839 0
333	H, KJ/KG	-1844.23 -2386.97
334	U, KJ/KG	-2842.66 -3299.05
335	G, KJ/KG	-33642.5 -31435.2
336	S, KJ/(KG)(K)	9.6821 9.6821
338	M, (1/n)	27.350 27.350

339 MW, MOL WT 25.268 25.268  
 340 Cp, KJ/(KG)(K) 1.9182 1.9032  
 341 GAMMAS 1.1883 1.1901  
 342 SON VEL, M/SEC 1089.3 1041.9  
 343 MACH NUMBER 0.000 1.000

344  
 345 PERFORMANCE PARAMETERS

346  
 347 Ae/At 1.00000  
 348 CSTAR, M/SEC 1545.7  
 349 CF 0.6740  
 350 Ivac, M/SEC 1917.3  
 351 Isp, M/SEC 1041.9

352  
 353 MOLE FRACTIONS

354  
 355 \*AL 0.00016 ALCL 0.00823 ALCL2 0.00061  
 356 ALCL3 0.00022 ALH 0.00004 ALHCL 0.00003  
 357 ALHCL2 0.00006 \*ALO 0.00014 ALOCL 0.00035  
 358 ALOH 0.00456 ALOHCL 0.00059 ALOHCL2 0.00076  
 359 AL(OH)2 0.00012 AL(OH)2CL 0.00017 AL(OH)3 0.00003  
 360 AL2O 0.00009 AL2O2 0.00002 \*CO 0.25407  
 361 \*CO2 0.00748 \*CL 0.00778 CL2 0.00001  
 362 \*H 0.03062 HALO2 0.00001 HCN 0.00001  
 363 HCO 0.00002 HCL 0.12553 \*H2 0.32881  
 364 H2O 0.07681 NH2 0.00001 NH3 0.00001  
 365 \*NO 0.00017 \*N2 0.07302 \*O 0.00016  
 366 \*OH 0.00312 \*O2 0.00001 AL2O3(L) 0.07613

367  
 368 \* THERMODYNAMIC PROPERTIES FITTED TO 20000.K

369  
 370 PRODUCTS WHICH WERE CONSIDERED BUT WHOSE MOLE FRACTIONS  
 371 WERE LESS THAN 5.000000E-06 FOR ALL ASSIGNED CONDITIONS

372  
 373 ALC ALC2 ALH2 ALH2CL ALH3  
 374 ALN ALOCL2 ALO2 AL2 AL2C2  
 375 AL2CL6 AL2O3 \*C CCL CCL2  
 376 CCL3 CCL4 \*CH CHCL CHCL2  
 377 CHCL3 CH2 CH2CL CH2CL2 CH3  
 378 CH3CL CH2OH CH3O CH4 CH3OH  
 379 CH3OOH \*CN CNN COCL COCL2  
 380 COHCL COOH \*C2 C2CL C2CL2  
 381 C2CL3 C2CL4 C2CL6 C2H C2HCL  
 382 C2HCL3 C2H2, acetylene C2H2, vinylidene C2H2CL2 CH2CO, ketene  
 383 O(CH)2O HO(CO)2OH C2H3, vinyl C2H3CL CH2CL-COOH  
 384 CH3CN CH3CO, acetyl C2H4 C2H4O, ethylen-o CH3CHO, ethanal  
 385 CH3COOH OHCH2COOH C2H5 C2H6 CH3N2CH3  
 386 C2H5OH CH3OCH3 CH3O2CH3 CCN CNC  
 387 OCCN C2N2 C2O \*C3 C3H3, 1-propyn1  
 388 C3H3, 2-propyn1 C3H4, allene C3H4, propyne C3H4, cyclo- C3H5, allyl  
 389 C3H6, propylene C3H6, cyclo- C3H6O, propylox C3H6O, acetone C3H6O, propanal  
 390 C3H7, n-propyl C3H7, i-propyl C3H8 C3H8O, 1propanol C3H8O, 2propanol  
 391 CNCOCN C3O2 \*C4 C4H2, butadiyne C4H4, 1,3-cyclo-  
 392 C4H6, butadiene C4H6, 1butyne C4H6, 2butyne C4H6, cyclo- C4H8, 1-butene  
 393 C4H8, cis2-buten C4H8, tr2-butene C4H8, isobutene C4H8, cyclo- (CH3COOH)2  
 394 C4H9, n-butyl C4H9, i-butyl C4H9, s-butyl C4H9, t-butyl C4H10, n-butane  
 395 C4H10, isobutane C4N2 \*C5 C5H6, 1,3cyclo- C5H8, cyclo-  
 396 C5H10, 1-pentene C5H10, cyclo- C5H11, pentyl C5H11, t-pentyl C5H12, n-pentane

397	C5H12, i-pentane	CH3C(CH3)2CH3	C6H2	C6H5, phenyl	C6H5O, phenoxy
398	C6H6	C6H5OH, phenol	C6H10, cyclo-	C6H12, 1-hexene	C6H12, cyclo-
399	C6H13, n-hexyl	C6H14, n-hexane	C7H7, benzyl	C7H8	C7H8O, cresol-mx
400	C7H14, 1-heptene	C7H15, n-heptyl	C7H16, n-heptane	C7H16, 2-methylh	C8H8, styrene
401	C8H10, ethylbenz	C8H16, 1-octene	C8H17, n-octyl	C8H18, n-octane	C8H18, isooctane
402	C9H19, n-nonyl	C10H8, naphthale	C10H21, n-decyl	C12H9, o-bipheny	C12H10, biphenyl
403	CLCN	CLO	CLO2	CL2O	HALO
404	HCCN	HCCO	HNC	HNCO	HNO
405	HNO2	HNO3	HOCL	HO2	HCHO, formaldehy
406	HCOOH	H2O2	(HCOOH)2	*N	NCO
407	*NH	NH2OH	NOCL	NO2	NO2CL
408	NO3	NCN	N2H2	NH2NO2	N2H4
409	N2O	N2O3	N2O4	N2O5	N3
410	N3H	O3	AL (cr)	AL (L)	ALCL3 (cr)
411	ALCL3 (L)	ALH3 (a)	ALN (cr)	ALN (L)	AL (OH)3 (a)
412	AL4C3 (cr)	C (gr)	H2O (cr)	H2O (L)	NH4CL (II)
413	NH4CL (III)				

414  
415 NOTE. WEIGHT FRACTION OF FUEL IN TOTAL FUELS AND OF OXIDANT IN TOTAL OXIDANTS

416  
417 WARNING!! CALCULATIONS WERE STOPPED BECAUSE NEXT POINT IS MORE  
418 THAN 50 K BELOW THE TEMPERATURE RANGE OF A CONDENSED SPECIES (ROCKET)

# APPENDIX B

## MATLAB CODE

### B.1 METHOD OF CHARACTERISTICS

```
1  clc; close all; clear all;
2
3  p_1 = 4000000 ;
4  T_1 = 3284;
5  FT = 0;
6  m_dot = 0.4914;
7  ALT = 1000;
8  g = 1.2;
9  R = 329;
10
11 T = 15.04 - 0.00649*ALT;
12 p_o = 1000*(101.29*((T+273.1)/288.08)^5.256);
13
14 PR = p_o/p_1;
15 PR2 = (p_o/p_1)^((g-1)/g);
16 TT = (2*g*R*T_1)/(g-1);
17 p_t = ((2/(g+1))^(g/(g-1)))*2.068;
18 v_t = sqrt((2*g*R*T_1)/(g+1));
19 v_e = sqrt(TT*(1-PR2));
20
21 if m_dot==0
22     m_dot=FT/v_e;
23 elseif FT==0
24     FT = m_dot/v_e;
25 else
26     fprintf('You can either set desired thrust
```

```

                OR mass flow rate')
27  end
28
29  T_e = T_1*(p_o/p_1)^((g-1)/g);
30  a_e = sqrt(g*R*T_e);
31
32  Me = v_e/a_e;
33
34
35  TR = 7.8; %throat radius (mm)
36  RTOD = 180/pi;
37  DTOR = pi/180;
38  P = [];
39
40  A = sqrt((g+1)/(g-1));
41  B = (g-1)/(g+1);
42  v_PM = @(x) A*atan(sqrt(B*(x^2-1))) - atan(
        sqrt(x^2-1));
43
44  T_max = 0.5*v_PM(Me)*RTOD;
45  DT = (90-T_max) - fix(90-T_max);
46  T(1) = DT*DTOR;
47  n = T_max*2;
48
49  for m = 2:n+1
50      T(m) = (DT + (m-1))*DTOR;
51      %Mach from T(i) using T(i) = v_PM (FALSE
        POSITION)
52      x_int = [1 1.01*Me];
53      func = @(x) T(m) - v_PM(x);
54      M(m) = fzero(func, x_int);
55      P(m) = 0 + TR*tan(T(m)); %X-AXIS POINTS
56      %RRSLOPES

```

```

57     RR(m) = -TR/P(m);
58     %LR slopes
59     LR(m) = tan(T(m)+asin(1/M(m)));
60     SL(m) = -RR(m);
61 end
62
63 P(1) = [];
64 l = length(P);
65
66 for j = 1:l
67     P1 = [0 TR];
68     P2 = [P(j) 0];
69     plot(P2,P1,'k')
70     hold on
71     xlabel('CENTERLINE (mm)')
72     ylabel('RADIUS (mm)')
73 end
74 hold on;
75 LR(1) = []; RR(1) = [];
76 SL(1) = [];
77 F = RR(m-1);
78
79 for c = 1:length(P)-1
80     x(c) = (TR+SL(c)*P(c))/(SL(c)-F);
81     y(c) = F*x(c)+TR;
82     X_P = [P(c) x(c)];
83     Y_P = [0 y(c)];
84     plot(X_P,Y_P,'b');
85 end
86 hold on
87
88
89 TM = T_max*DTOR;

```

```

90  xw(1) = (TR+SL(1)*P(1))/(SL(1)-tan(TM));
91  yw(1) = tan(TM)*xw(1)+TR;
92  X_P2 = [P(1) xw];
93  Y_P2 = [P(2) yw];
94  plot(X_P2, Y_P2, 'g');
95
96  DTW = tan(TM)/(length(P)-1);
97  s(1) = tan(TM);
98  b(1) = TR;
99
100  for k = 2:length(P)-1
101      s(k) = tan(TM)-(k-1)*DTW; %slope
102      b(k) = yw(k-1)-s(k)*xw(k-1); %y-int
103      xw(k) = (b(k)+SL(k)*P(k))/(SL(k)-s(k))
104          ;
105      yw(k) = s(k)*xw(k)+b(k);
106      X_P3 = [x(k) xw(k)];
107      Y_P3 = [y(k) yw(k)];
108      plot(X_P3, Y_P3, 'r');
109  end
110  hold on
111
112  LAST POINT
113  xf = (b(length(b))+SL(length(SL))*P(length
114      (P)))/SL(length(SL));
115  yf = b(length(b));
116  X_F = [P(length(P)) xf];
117  Y_F = [0 yf];
118  plot(X_F, Y_F, 'r');
119
120  xw = [0 xw];
121  yw = [TR yw];
122  RTHROAT = TR;

```

```

121     REXIT = yw(length(yw));
122
123     AR = (RTHROAT/REXIT)^2
124
125     xlswrite('PARAMS.xlsx', transpose(xw), 'PTS'
126             , 'A1:A62');
127
128     xlswrite('PARAMS.xlsx', transpose(yw), 'PTS'
129             , 'B1:B62');

```

## B.2 THRUST CALCULATION AT EACH TIME-STEP

```

1  A = 0.001168999;
2  Astar = 0.000261586;
3  pb = 101325;
4  Te = 1445;
5  gamma = 1.2;
6  R = 330.9;
7
8  t = load('Time.mat', 'VarName1');
9  t = struct2cell(t);
10 t = t{1};
11 t = transpose(t);
12 P = load('Pressure.mat', 'Pb');
13 P = struct2cell(P);
14 P = P{1};
15 P = transpose(P);
16 n = length(P);
17 %P = P.*100000;
18
19 T = findthrust(P, n, pb, Te, gamma, A, Astar, R);
20

```

```

21 figure(1)
22 plot(t,P)
23 xlabel('Time')
24 ylabel('Pressure')
25 title('Pressure vs time')
26
27 figure(2)
28 plot(t,T)
29 xlabel('Time')
30 ylabel('Thrust')
31 title('Thrust vs time')
32
33 function Thrust = findthrust(P,n,pb,Te,gamma,A
    ,Astar,R)
34 % Calculations
35 a = A/Astar;
36 fprintf('\nThe value of A/Astar is %g\n',a)
37 g = gamma;
38 c1 = (g+1)/(2*(g-1));
39 c2 = (g-1)/2;
40 c3 = (g+1)/2;
41 m = 0.01:0.0000001:1;
42 val1 = ((1./m).*((1 + c2.*m.*m)./c3).^c1) -
    a;
43 [~,ind] = min(abs(val1));
44 M1 = m(1,ind); % subsonic mach
45 fprintf('\n The value of Subsonic Mach number
    for given A/Astar value is %g\n',M1)
46 m = 1:0.0000001:4;
47 val2 = ((1./m).*((1 + c2.*m.*m)./c3).^c1) -
    a;
48 [~,ind] = min(abs(val2));
49 M2 = m(1,ind); %super sonic mach

```

```

50     fprintf('\n The value of Supersonic Mach
        number for given A/Astar value is %g\n',M2)
51
52     prat1 = (1 + c2*M1*M1)^(g/(1-g));
53     p01 = pb/prat1;
54     fprintf('\nP01 value is %g\n',p01)
55
56     prat2 = (1 + c2*M2*M2)^(g/(1-g));
57     p02 = pb/prat2;
58     fprintf('\nP02 value is %g\n',p02);
59
60     Md = (((g-1)*M2^2 + 2)/(2*g*M2^2 - (g-1)))
        ^0.5;
61     pratd = (1 + c2*Md*Md)^(g/(1-g));
62
63     p21 = (((g+1)*M2^2)/(((g-1)*M2^2)+2))^(g/(g
        -1))*(((g+1)/((2*g*M2^2)-(g-1)))^(1/(g-1))
        );
64
65     pbi = pratd*p21;
66
67     p0i = pb/pbi;
68     fprintf('\nP0i value is %g\n',p0i);
69
70     Mi = ((1-((pb/p0i)^((1-g)/g)))*(2/(1-g)))
        ^00.5;
71     fprintf('\n Value of Mi is %g\n',Mi)
72     M = zeros(1,n); % Exit Mach number
73     mdot = zeros(1,n); % Mass flow rate
74     PE = zeros(1,n); % Exit Pressure
75
76     for i = 1:1:n
77         pc = P(1,i);

```

```

78     if pc <= p01
79         M(1,i) = ((1-((pb/pc) ^ ((1-g)/g)))
80             *(2/(1-g))) ^ 0.5;
81         mdot(1,i) = A*pc*(g/R) ^ 0.5 * M(1,i) * (1
82             + c2 * M(1,i) * M(1,i)) ^ (-c1);
83         PE(1,i) = pb;
84     end
85     if pc > p01 && pc <= p0i
86         pbc = pb/pc;
87         Asrat = findAs(pbc, a, g);
88         As = Asrat * Astar;
89         m = 1:0.0000001:4;
90         val2 = ((1./m) .* ((1 + c2.*m.*m) ./ c3)
91             .^c1) - Asrat;
92         [~, ind] = min(abs(val2));
93         Mup = m(1, ind); %super sonic mach
94         Mdo = ((1 + c2*Mup*Mup) / (g*Mup*Mup -
95             c2)) ^ 0.5;
96         A2star = Mdo.*As.*(1./((1./Mdo) .* ((1
97             + c2.*Mdo.*Mdo) ./ c3) .^c1)));
98         m = 0.01:0.0000001:1;
99         val1 = ((1./m) .* ((1 + c2.*m.*m) ./ c3)
100             .^c1) - (A./A2star);
101         [~, ind] = min(abs(val1));
102         M(1,i) = m(1, ind); % subsonic mach
103         mdot(1,i) = A*pc*(g/R) ^ 0.5 * M(1,i) * (1
104             + c2 * M(1,i) * M(1,i)) ^ (-c1);
105         Pt1t0 = (((g+1)*Mup^2) / (((g-1)*Mup^2
106             + 2)) ^ (g/(g-1))) * (((g+1) / (2*g*Mup^2
107             - (g-1))) ^ (1/(g-1)));
108         Pt1 = Pt1t0*pc;
109         PE(1,i) = Pt1 * (1 + c2*M(1,i)^2) ^ (-g/(
110             g-1));

```

```

101     end
102     if pc > p0i
103         M(1,i) = M2;
104         mdot(1,i) = A*pc*(g/R)^0.5 * M(1,i)*(1
            + c2*M(1,i)*M(1,i))^(-c1);
105         PE(1,i) = pc*(1 + c2*M(1,i)^2)^(-g/(g
            -1));
106     end
107 end
108
109 Thrust = -mdot.*M.*((g*R*Te)^0.5).*0.1 - (PE -
        pb).*A;
110 end

```

### B.2.1 Normal Shock Area function

```

1  #save this file in same directory as findAs.m
2
3  function Asrat = findAs(pbc,a,g)
4
5      Ae_At      = a;
6
7      % Ratio of specific heats []
8      setPbP0_NSN = pbc;
9
10     gm1      = g-1;
11     gp1      = g+1;
12     gogm1    = g/gm1;
13     gm1o2    = gm1/2;
14     gogp1    = g/gp1;
15
16     Me_Sub   = ISENTROPIC_FLOW(Ae_At,'Asub',g,'M');
17     Pe_P0_Sub = (1 + gm1o2*Me_Sub^2)^(-gogm1);
18
19     Me_Sup   = ISENTROPIC_FLOW(Ae_At,'Asup',g,'M');
20     Pb_P0_Sup = (1 + gm1o2*Me_Sup^2)^(-gogm1);
21

```

```

22
23     P2_P1      = 1 + ((2*gogp1)*(Me_Sup^2-1));
24     Pe_P0_NSE = (P2_P1)*(Pb_P0_Sup);
25     Me_NSE    = NORMAL_SHOCK(Me_Sup, 'M1', g, 'M2');
26
27
28     if (setPbP0_NSN > Pe_P0_NSE && setPbP0_NSN < Pe_P0_Sub)
29
30
31         errTol = 1e-6;
32         Arat_Lo = 1.00001;
33         Arat_Hi = Ae_At;
34         err     = inf;
35
36
37         while (err > errTol)
38
39
40             Arat_Mid = 0.5*(Arat_Hi + Arat_Lo);
41
42
43             Pb_P0_Lo  = NS_NOZZLE(Arat_Lo, Ae_At, g);
44             Pb_P0_Mid = NS_NOZZLE(Arat_Mid, Ae_At, g);
45             Pb_P0_Hi  = NS_NOZZLE(Arat_Hi, Ae_At, g);
46
47
48             errLo = setPbP0_NSN - Pb_P0_Lo;
49             errMid = setPbP0_NSN - Pb_P0_Mid;
50             errHi  = setPbP0_NSN - Pb_P0_Hi;
51
52
53             if (errLo*errMid < 0)
54                 Arat_Hi = Arat_Mid;
55             elseif (errHi*errMid < 0)
56                 Arat_Lo = Arat_Mid;
57             end
58
59
60             err = abs(errMid-errLo);
61         end
62
63
64         ANS_Als_Iter = Arat_Mid;
65
66         term1 = -(1/gm1);

```

```

67     term2 = 1/(gm1^2);
68     term3 = 2/gm1;
69     term4 = (2/gp1)^(gp1/gm1);
70     term5 = (setPbP0_NSN*Ae_At)^-2;
71     Me     = sqrt(term1 + sqrt(term2 + term3*term4*term5));
72
73
74     P0e_Pe = (1 + (gm1o2*Me^2))^(g/gm1);
75     P02_P01 = P0e_Pe*setPbP0_NSN;
76
77
78     problem.objective = @(M) exp(-gogm1*log(((2 + gm1*M^2)/(
79         gp1*M^2))*...
80         (1+(2*g/gp1)*(M^2-1))) +
81         ...
82         log((1+(2*g/gp1)*(M^2-1)
83         )))) - P02_P01;
84
85     problem.x0         = [1+1e-5 50];
86     problem.solver     = 'fzero';
87     problem.options   = optimset(@fzero);
88     M1                 = fzero(problem);
89
90
91
92     ANS_Als_Dir = ISENTROPIC_FLOW(M1,'M',g,'AAs');
93     else
94         fprintf('Set pressure ratio does not give NS in nozzle!\n
95             \n');
96         ANS_Als_Iter = 1;
97         ANS_Als_Dir  = 1;
98     end
99     Asrat = ANS_Als_Iter;
end

```

### B.3 TRAJECTORY : VERSION 1

```

1  clear;clc;clear all
2  m = 5;

```

```

3  g = 9.81;
4  cd0 = 0.01; k = 0; cl = 0; rho = 1.225; S =
    0.6;
5
6  T1 = load('Thrusttime.mat');
7  T1 = struct2cell(T1);
8  T1 = T1{1};
9  T1 = transpose(T1);
10
11 t = linspace(0,10,10000);
12
13 v0 = 1; gamma0 = -73.33*pi/180; x0 = 0; y0 =
    2000;
14 [t1,y1] = ode45(@(t,y) flig(t,y,m,g,cd0,cl,k,S,
    rho,T1),t,[V0;gamma0;x0;y0]);
15 z1 =linspace(8,57,10000);
16
17 figure(1)
18 tiledlayout(2,1)
19 nexttile
20 plot(y1(:,3),y1(:,4),'linewidth',2)
21 ylim([0 (y0+400)])
22 xlabel('distance travelled (m)')
23 ylabel('Altitude of the missile (m)')
24 title('Trajectory')
25
26 nexttile
27 plot(t1,y1(:,4),'r','linewidth',2)
28 ylim([0 (y0+400)])
29 xlabel('Time (s)')
30 ylabel('Altitude of the missile (m)')
31 title('Trajectory')
32

```

```

33
34
35
36 gamma = 0:-0.01:-pi/2.1;
37 ran = zeros(1, length(gamma));
38
39
40 for i = 1:length(gamma)
41     gamma0 = gamma(1,i);
42     [t1,y1] = ode45(@(t,y) flig(t,y,m,g,cd0,cl,k
43         ,S,rho,T),t,[V0;gamma0;x0;y0]);
44     ran(1,i) = findrange(y1);
45 end
46
47 reqrange = 1500;
48 [~,b] = min(abs(ran - reqrange));
49 reqqamma = gamma(1,b);
50 fprintf('\n Therefore gamma required for the
51     given range of %g is %g \n',reqrange,
52     reqqamma*180/pi)
53
54 [t1,y1] = ode45(@(t,y) flig(t,y,m,g,cd0,cl,k,S,
55     rho,T),t,[V0;reqgamma;x0;y0]);
56
57 figure(3)
58 plot(y1(:,3),y1(:,4),'linewidth',2)
59 ylim([0 (y0+400)])
60 xlabel('distance travelled (m)')
61 ylabel('Altitude of the missile (m)')
62 title('Trajectory')
63
64 function r = findrange(y)

```

```

62  [~, a] = min(abs(y(:, 4)));
63  r = y(a, 3);
64  end
65
66  function dy = flig(t, y, m, g, cd0, cl, k, S, rho, T1)
67  T = interp1(T1(:, 1), T1(:, 2), t);
68  D = 0.5*rho*S*y(1)*y(1)*(cd0 + k*cl*cl);
69  dy(1, 1) = (T - D - m*g*cos(y(2)))/m;
70  dy(2, 1) = (-m*g*cos(y(2)))/(m*y(1));
71  dy(3, 1) = y(1)*cos(y(2));
72  dy(4, 1) = y(1)*sin(y(2));
73  end

```

#### B.4 TRAJECTORY : VERSION 2

```

1  clear; clear all; clc;
2  m = 5;
3  g = 9.81;
4  cd0 = 0.01; k = 0; cl = 0; rho = 1.225; S =
    0.6;
5
6  T1 = load('Thrusttime.mat');
7  T1 = struct2cell(T1);
8  T1 = T1{1};
9  T1 = transpose(T1);
10
11 t = linspace(0, 10, 10000);
12 V0 = 100; x0 = 0; y0 = 950; xob = 650; yob =
    350; rob = 100;
13 rsafe = 50; ysafe = 20; xdes = xob + 600; d0 =
    3;

```

```

14
15 gamma = 0:-0.01:-pi/2.1;
16 y1val = zeros(1, length(gamma));
17
18 for i = 1:length(gamma)
19     gamma0 = gamma(1, i);
20     [t1, y1] = ode45(@(t, y) flig(t, y, m, g, cd0, cl, k
        , S, rho, T), t, [V0; gamma0; x0; y0]);
21     y1val(1, i) = interp1(y1(:, 3), y1(:, 4), xob-(
        rob+rsafe));
22 end
23
24 [~, ind] = min(abs(y1val - (yob+8*ysafe)));
25 gamma0 = gamma(1, ind);
26
27 [t01, y01] = ode45(@(t, y) flig(t, y, m, g, cd0, cl, k,
        S, rho, T), t, [V0; gamma0; x0; y0]);
28 [~, ind] = min(abs(y01(:, 3) - (xob - (rob+rsafe))))
        ;
29 tp1 = t01(ind, 1); yp1 = y01(ind, 4); xp1 = y01(
        ind, 3); gammal = y01(ind, 2);
30 v1 = y01(ind, 1);
31
32 I = 0.36;
33 t = linspace(tp1, tp1+0.5, 10000);
34
35 clc = 0.00001:10000:1;
36 yval2 = zeros(1, length(clc));
37
38 for i = 1:length(clc)
39     clcan = clc(1, i);
40     t = linspace(0, 10, 10000);
41     [t2, y2] = ode45(@(t, y) turn(t, y, m, g, cd0, cl,

```

```

        k, S, rho, T, clcan, xob, rob, rsafe, d0, I), t, [
        V1; gamma1; xp1; yp1; 0]);
42     A = find(y2(:, 2) > 0);
43     B = A(1, 1);
44     yval2(1, i) = t2(B, 1);
45     end
46
47     [~, k0] = min(abs(yval2 - 0.5));
48     clcan = clc(1, k0);
49
50     t = linspace(tp1, tp1 + 0.5, 10000);
51     [t02, y02] = ode45(@(t, y) turn(t, y, m, g, cd0, cl, k,
        S, rho, T, clcan, xob, rob, rsafe, d0, I), t, [V1;
        gamma1; xp1; yp1; 0]);
52
53     [~, ind1] = min(abs(y02(:, 2)));
54     yp2 = y02(ind1, 4); xp2 = y02(ind1, 3); gamma2 =
        y02(ind1, 2);
55     v2 = y02(ind1, 2);
56     tp2 = t02(ind1, 1);
57
58     t = linspace(tp2, tp2 + 0.15, 10000);
59     [t03, y03] = ode45(@(t, y) turn(t, y, m, g, cd0, cl, k,
        S, rho, T, -clcan*4, xob, rob, rsafe, d0, I), t, [V1;
        gamma2; xp2; yp2; 0]);
60     tp3 = t03(end, 1);
61
62     t = linspace(tp3, tp3 + 10, 10000);
63     [t04, y04] = ode45(@(t, y) flig(t, y, m, g, cd0, cl, k,
        S, rho, 0), t, [y03(end, 1) / 20; y03(end, 2); y03(
        end, 3); y03(end, 4)]);
64
65     figure(1)

```

```

66 P1 = [y01(1:ind,3) y01(1:ind,4)];
67 P2 = [y02(1:ind1,3) y02(1:ind1,4)];
68 P3 = [y03(:,3) y03(:,4)];
69 P4 = [y04(:,3) y04(:,4)];
70 P = [P1;P2;P3;P4];
71
72 Vf1 = [y01(1:ind,1) y01(1:ind,2)];
73 Vf2 = [y02(1:ind1,1) y02(1:ind1,2)];
74 Vf3 = [y03(:,1) y03(:,2)];
75 Vf4 = [y04(:,1) y04(:,2)];
76 Vf = [Vf1;Vf2;Vf3;Vf4];
77
78 time = [t01(1:ind,1);t02(1:ind1,1);t03(:,1);
          t04(:,1)];
79
80 plot(P(:,1),P(:,2),[xob,xob],[0,yob+25])
81 xlabel('Distance travelled')
82 ylabel('Height from ground')
83 title('Trajectory when obstacle is present')
84 legend('Trajectory followed','Obstacle')
85 hold on
86 ylim([0 y0+500])
87
88 figure(2)
89 plot(time(:,1),P(:,2))
90 xlabel('Time')
91 ylabel('Height from ground')
92 title('Height vs time')
93 function dy = flig(t,y,m,g,cd0,cl,k,S,rho,T1)
94 D = 0.5*rho*S*y(1)*y(1)*(cd0 + k*cl*cl);
95 if t > 4
96     T = interp1(T1(:,1),T1(:,2),t);
97 end

```

```

98  dy(1,1) = (T - D - m*g*sin(y(2)))/m;
99  dy(2,1) = (-m*g*cos(y(2)))/(m*y(1));
100 dy(3,1) = y(1)*cos(y(2));
101 dy(4,1) = y(1)*sin(y(2));
102 end
103
104 function dy = turn(t,y,m,g,cd0,cl,k,S,rho,T1,
      clcan,xob,rob,rsafe,d0,I)
105 D = 0.5*rho*S*y(1)*y(1)*(cd0 + k*cl*cl);
106 L = 0.5*rho*S*y(1)*y(1)*clcan;
107 if t > 4
108     T = interp1(T1(:,1),T1(:,2),t);
109 end
110 dy(1,1) = (T - D - m*g*sin(y(2)))/m;
111 dy(2,1) = ((-m*g*cos(y(2)))/(m*y(1)) + y(5));
112 dy(3,1) = y(1)*cos(y(2));
113 dy(4,1) = y(1)*sin(y(2));
114 dy(5,1) = 2*L*d0/I;
115 end

```

# APPENDIX C

## TRACKING CODE

### C.1 COLOR DETECTION

```
1 import cv2
2 import numpy as np
3
4 img = cv2.imread('yellow_object.JPG', 1)
5
6 img = cv2.resize(img, (0,0), fx=0.2, fy=0.2)
7 hsv = cv2.cvtColor(img, cv2.COLOR_BGR2HSV)
8
9 lower_range = np.array([24, 100, 100], dtype=np.uint8)
10 upper_range = np.array([44, 255, 255], dtype=np.uint8)
11 mask = cv2.inRange(hsv, lower_range, upper_range)
12 cv2.imshow('mask', mask)
13 cv2.imshow('image', img)
14
15 while (1):
16     k = cv2.waitKey(0)
17     if (k == 27):
18         break
19
20 cv2.destroyAllWindows()
```

### C.2 BGR TO HSV

```
1 import sys
2 import numpy as np
3 import cv2
4
5 blue = sys.argv[1]
6 green = sys.argv[2]
7 red = sys.argv[3]
8
9 color = np.uint8([[blue, green, red]])
10 hsv_color = cv2.cvtColor(color, cv2.COLOR_BGR2HSV)
```

```

11
12 hue = hsv_color[0][0][0]
13
14 print("Lower bound is :"),
15 print "[" + str(hue-10) + ", 100, 100]\n")
16
17 print("Upper bound is :"),
18 print "[" + str(hue + 10) + ", 255, 255]")

```

### C.3 OBJECT TRACKING IN RECORDED VIDEO

```

1 from imutils.video import VideoStream
2 from imutils.video import FPS
3 import argparse
4 import imutils
5 import time
6 import cv2
7
8 ap = argparse.ArgumentParser()
9 ap.add_argument("-v", "--video", type=str,
10                help="path to input video file")
11 ap.add_argument("-t", "--tracker", type=str, default="kcf",
12                help="OpenCV object tracker type")
13 args = vars(ap.parse_args())
14
15 (major, minor) = cv2.__version__.split(".")[:2]
16 if int(major) == 3 and int(minor) < 3:
17     tracker = cv2.Tracker_create(args["tracker"].
18                                upper())
19 else:
20     OPENCV_OBJECT_TRACKERS = {
21         "csrt": cv2.TrackerCSRT_create,
22         "kcf": cv2.TrackerKCF_create,
23         "boosting": cv2.TrackerBoosting_create,
24         "mil": cv2.TrackerMIL_create,
25         "tld": cv2.TrackerTLD_create,
26         "medianflow": cv2.
27             TrackerMedianFlow_create,
28         "mosse": cv2.TrackerMOSSE_create
29     }

```

```

28         tracker = OPENCV_OBJECT_TRACKERS [args ["tracker
                "]] ()
29     initBB = None
30
31     if not args.get ("video", False):
32         print (" [INFO] starting video stream...")
33         vs = VideoStream (src=0).start ()
34         time.sleep (1.0)
35     else:
36         vs = cv2.VideoCapture (args ["video"])
37     fps = None
38
39     while True:
40         frame = vs.read ()
41         frame = frame [1] if args.get ("video", False) else
                frame
42
43         if frame is None:
44             break
45         frame = imutils.resize (frame, width=500)
46         (H, W) = frame.shape [:2]
47
48
49         if initBB is not None:
50
51             (success, box) = tracker.update (frame)
52
53             if success:
54                 (x, y, w, h) = [int (v) for v in
                        box]
55                 cv2.rectangle (frame, (x, y), (x +
                        w, y + h),
                        (0, 255, 0), 2)
56
57
58                 fps.update ()
59                 fps.stop ()
60
61                 info = [
62                     ("Tracker", args ["tracker"]),
63                     ("Success", "Yes" if success else
                        "No"),

```

```

64         ("FPS", "{:.2f}".format(fps.fps()
65         )),
66     ]
67     for (i, (k, v)) in enumerate(info):
68         text = "{}: {}".format(k, v)
69         cv2.putText(frame, text, (10, H -
70             ((i * 20) + 20)),
71             cv2.FONT_HERSHEY_SIMPLEX,
72             0.6, (0, 0, 255), 2)
73
74     cv2.imshow("Frame", frame)
75     key = cv2.waitKey(1) & 0xFF
76
77     if key == ord("s"):
78         initBB = cv2.selectROI("Frame", frame,
79             fromCenter=False,
80             showCrosshair=True)
81         tracker.init(frame, initBB)
82         fps = FPS().start()
83
84     elif key == ord("q"):
85         break
86
87 if not args.get("video", False):
88     vs.stop()
89
90 else:
91     vs.release()
92
93 cv2.destroyAllWindows()

```

## C.4 OBJECT TRACKING IN LIVE VIDEO

```

1  from collections import deque
2  import numpy as np
3  import argparse
4  import imutils
5  import cv2
6
7  ap = argparse.ArgumentParser()
8  ap.add_argument("-v", "--video",
9      help="path to the (optional) video file")
10 ap.add_argument("-b", "--buffer", type=int, default=64,
11     help="max buffer size")

```

```

12  args = vars(ap.parse_args())
13
14  colorLower = (24, 100, 100)
15  colorUpper = (44, 255, 255)
16  pts = deque(maxlen=args["buffer"])
17
18  if not args.get("video", False):
19      camera = cv2.VideoCapture(0)
20  else:
21      camera = cv2.VideoCapture(args["video"])
22
23  while True:
24      (grabbed, frame) = camera.read()
25
26      if args.get("video") and not grabbed:
27          break
28
29      frame = imutils.resize(frame, width=600)
30      frame = imutils.rotate(frame, angle=180)
31      hsv = cv2.cvtColor(frame, cv2.COLOR_BGR2HSV)
32
33      mask = cv2.inRange(hsv, colorLower, colorUpper)
34      mask = cv2.erode(mask, None, iterations=2)
35      mask = cv2.dilate(mask, None, iterations=2)
36
37      cnts = cv2.findContours(mask.copy(), cv2.
38          RETR_EXTERNAL,
39          cv2.CHAIN_APPROX_SIMPLE)[-2]
40      center = None
41
42      if len(cnts) > 0:
43          c = max(cnts, key=cv2.contourArea)
44          ((x, y), radius) = cv2.minEnclosingCircle(
45              (c)
46              M = cv2.moments(c)
47              center = (int(M["m10"] / M["m00"]), int(M
48                  ["m01"] / M["m00"]))
49
50          if radius > 10:
51              cv2.circle(frame, (int(x), int(y)
52                  ), int(radius),

```

```

49             (0, 255, 255), 2)
50         cv2.circle(frame, center, 5, (0,
51             0, 255), -1)
52
53     pts.appendleft(center)
54
55     for i in range(1, len(pts)):
56         if pts[i - 1] is None or pts[i] is None:
57             continue
58
59         thickness = int(np.sqrt(args["buffer"] /
60             float(i + 1)) * 2.5)
61         cv2.line(frame, pts[i - 1], pts[i], (0,
62             0, 255), thickness)
63
64     cv2.imshow("Frame", frame)
65     key = cv2.waitKey(1) & 0xFF
66     # if the 'q' key is pressed, stop the loop
67     if key == ord("q"):
68         break
69
70 camera.release()
71 cv2.destroyAllWindows()

```

## C.5 GET OBJECT COORDINATE IN LIVE VIDEO

```

1  from __future__ import print_function
2  from imutils.video import VideoStream
3  import imutils
4  import time
5  import cv2
6  import os
7  import RPi.GPIO as GPIO
8  redLed = 21
9  GPIO.setwarnings(False)
10 GPIO.setmode(GPIO.BCM)
11 GPIO.setup(redLed, GPIO.OUT)
12 def mapObjectPosition(x, y):
13     print("[INFO] Object Center coordinates at X0 = {0}
14         and Y0 = {1}".format(x, y))
15 vs = VideoStream(0).start()

```

```

15  time.sleep(2.0)
16  colorLower = (24, 100, 100)
17  colorUpper = (44, 255, 255)
18  GPIO.output(redLed, GPIO.LOW)
19  ledOn = False
20  while True:
21      frame = vs.read()
22      frame = imutils.resize(frame, width=500)
23      frame = imutils.rotate(frame, angle=180)
24      hsv = cv2.cvtColor(frame, cv2.COLOR_BGR2HSV)
25
26      mask = cv2.inRange(hsv, colorLower, colorUpper)
27      mask = cv2.erode(mask, None, iterations=2)
28      mask = cv2.dilate(mask, None, iterations=2)
29
30      cnts = cv2.findContours(mask.copy(), cv2.
        RETR_EXTERNAL,
31          cv2.CHAIN_APPROX_SIMPLE)
32      cnts = cnts[0] if imutils.is_cv2() else cnts[1]
33      center = None
34
35      if len(cnts) > 0:
36          c = max(cnts, key=cv2.contourArea)
37          ((x, y), radius) = cv2.minEnclosingCircle
            (c)
38          M = cv2.moments(c)
39          center = (int(M["m10"] / M["m00"]), int(M
            ["m01"] / M["m00"]))
40
41          if radius > 10:
42              cv2.circle(frame, (int(x), int(y))
43                  , int(radius),
44                      (0, 255, 255), 2)
45              cv2.circle(frame, center, 5, (0,
46                  0, 255), -1)
47
48              mapObjectPosition(int(x), int(y))
49
50          if not ledOn:
51              GPIO.output(redLed, GPIO.
52                  HIGH)

```

```

50             ledOn = True
51     elif ledOn:
52         GPIO.output(redLed, GPIO.LOW)
53         ledOn = False
54     cv2.imshow("Frame", frame)
55
56     key = cv2.waitKey(1) & 0xFF
57     if key == 27:
58         break
59 GPIO.cleanup()
60 cv2.destroyAllWindows()
61 vs.stop()

```

## C.6 LIVE OBJECT TRACK IN 2 AXIS GIMBAL

```

1  from __future__ import print_function
2  from imutils.video import VideoStream
3  import argparse
4  import imutils
5  import time
6  import cv2
7  import os
8  import RPi.GPIO as GPIO
9  panServo = 27
10 tiltServo = 17
11 redLed = 21
12 GPIO.setwarnings(False)
13 GPIO.setmode(GPIO.BCM)
14 GPIO.setup(redLed, GPIO.OUT)
15
16 def positionServo (servo, angle):
17     os.system("python angleServoCtrl.py " + str(servo) +
18             " " + str(angle))
19
20     print("[INFO] Positioning servo at GPIO {0} to {1}
21         degrees\n".format(servo, angle))
22
23 def mapServoPosition (x, y):
24     global panAngle
25     global tiltAngle
26     if (x < 220):
27         panAngle += 10

```

```

25         if panAngle > 140:
26             panAngle = 140
27             positionServo (panServo, panAngle)
28
29     if (x > 280):
30         panAngle -= 10
31         if panAngle < 40:
32             panAngle = 40
33             positionServo (panServo, panAngle)
34
35     if (y < 160):
36         tiltAngle += 10
37         if tiltAngle > 140:
38             tiltAngle = 140
39             positionServo (tiltServo, tiltAngle)
40
41     if (y > 210):
42         tiltAngle -= 10
43         if tiltAngle < 40:
44             tiltAngle = 40
45             positionServo (tiltServo, tiltAngle)
46
47     print ("[INFO] waiting for camera to warmup...")
48     vs = VideoStream(0).start()
49     time.sleep(2.0)
50     colorLower = (24, 100, 100)
51     colorUpper = (44, 255, 255)
52
53     GPIO.output(redLed, GPIO.LOW)
54     ledOn = False
55
56     global panAngle
57     panAngle = 90
58     global tiltAngle
59     tiltAngle =90
60
61     positionServo (panServo, panAngle)
62     positionServo (tiltServo, tiltAngle)
63
64     while True:
65         frame = vs.read()

```

```

66     frame = imutils.resize(frame, width=500)
67     frame = imutils.rotate(frame, angle=180)
68     hsv = cv2.cvtColor(frame, cv2.COLOR_BGR2HSV)
69
70     mask = cv2.inRange(hsv, colorLower, colorUpper)
71     mask = cv2.erode(mask, None, iterations=2)
72     mask = cv2.dilate(mask, None, iterations=2)
73
74     cnts = cv2.findContours(mask.copy(), cv2.
75         RETR_EXTERNAL,
76         cv2.CHAIN_APPROX_SIMPLE)
77     cnts = cnts[0] if imutils.is_cv2() else cnts[1]
78     center = None
79
80     if len(cnts) > 0:
81         c = max(cnts, key=cv2.contourArea)
82         ((x, y), radius) = cv2.minEnclosingCircle
83             (c)
84         M = cv2.moments(c)
85         center = (int(M["m10"] / M["m00"]), int(M
86             ["m01"] / M["m00"]))
87         if radius > 10:
88             cv2.circle(frame, (int(x), int(y))
89                 , int(radius),
90                 (0, 255, 255), 2)
91             cv2.circle(frame, center, 5, (0,
92                 0, 255), -1)
93
94             mapServoPosition(int(x), int(y))
95
96             if not ledOn:
97                 GPIO.output(redLed, GPIO.
98                     HIGH)
99                 ledOn = True
100
101     elif ledOn:
102         GPIO.output(redLed, GPIO.LOW)
103         ledOn = False
104     cv2.imshow("Frame", frame)
105     key = cv2.waitKey(1) & 0xFF
106     if key == 27:

```

```
101             break
102     positionServo (panServo, 90)
103     positionServo (tiltServo, 90)
104     GPIO.cleanup()
105     cv2.destroyAllWindows()
106     vs.stop()
```



## APPENDIX D

### PYTHON CODE FOR ML & DL TRAJECTORY PREDICTION ANALYSIS

#### D.1 IMPORT LIBRARY FILE AND LOAD DATASET

```
1  %matplotlib inline
2  import seaborn as sns
3  from sklearn.model_selection import train_test_split
4  from sklearn.metrics import classification_report,
   plot_confusion_matrix
5  from imblearn.over_sampling import SMOTE
6  from sklearn.tree import DecisionTreeClassifier
7  from sklearn.ensemble import RandomForestClassifier
8  from sklearn.ensemble import
   GradientBoostingClassifier
9  from sklearn.utils import class_weight
10 from keras import models
11 from keras import layers
12 from keras import regularizers
13 from keras import optimizers
14 import tensorflow as tf
15 import random as rn
16
17 os.environ['PYTHONHASHSEED'] = '0'
18 np.random.seed(1)
19 rn.seed(2)
20 tf.random.set_seed(3)
21
22 df = pd.read_csv('/content/drive/MyDrive/dataset.csv
   ')
```

#### D.2 DISPLAY THE FIRST 5 ROWS

```
1  df.head()
```

```
2 df.info()
```

### D.3 SMOTE TECHNIQUE FOR CLASS BALANCING

```
1 X_train_oversampled, y_train_oversampled = SMOTE().
   fit_resample(X_train, y_train)
2
3 print("Oversampled train X: ", X_train_oversampled.
   shape)
4 print("Oversampled train y: ", y_train_oversampled.
   shape)
5
6 pd.DataFrame(y_train_oversampled).value_counts()
7 # Create x, where x the 'scores' column's values as
   floats
8 x = df[['Velocity']].values.astype(float)
9 x
```

### D.4 NORMALIZATION

```
1 # Create a minimum and maximum processor object
2 min_max_scaler = preprocessing.MinMaxScaler()
3
4 # Create an object to transform the data to fit
   minmax processor
5 x_scaled = min_max_scaler.fit_transform(x)
6
7 # Run the normalizer on the dataframe
8 #df_normalized = pd.DataFrame(x_scaled)
9 x_scaled
```

### D.5 FILLING NULL VALUES TEST TRAIN SPLIT

```
1 df['Velocity'] = x_scaled
2 df
3 df.head()
4 df = df.fillna(df.mean())
5 from sklearn.model_selection import train_test_split
```

```

6 y = df['x', 'y']
7 x = df.drop('x', 'y', axis = 1)
8 x_train, x_test, y_train, y_test = train_test_split(
    x, y, test_size = 0.3, random_state = 42)
9
10 print(x_train)
11 print(x_test)
12 print(y_train)
13 print(y_test)
14 from sklearn.preprocessing import StandardScaler
15 sc=StandardScaler()
16 x_train = sc.fit_transform(x_train)
17 x_test = sc.transform(x_test)

```

## D.6 RANDOM FOREST REGRESSOR

```

1 from sklearn.ensemble import RandomForestRegressor
2 regressor = RandomForestRegressor(max_depth=2,
    random_state=0, n_estimators=100)
3 regressor.fit(x_train, y_train)
4 b_pred = regressor.predict(x_test)
5 from sklearn.metrics import mean_squared_error as
    mse
6 from sklearn.metrics import mean_absolute_error as
    mae
7 from sklearn.metrics import r2_score
8 print('MSE␣=', mse(y_pred, y_test))
9 print('MAE␣=', mae(y_pred, y_test))
10 print('R2␣Score␣=', r2_score(y_pred, y_test))

```

## D.7 ARTIFICIAL NEURAL NETWORK

```

1 from keras.callbacks import ModelCheckpoint
2 from keras.models import Sequential
3 from keras.layers import Dense, Activation, Flatten
4 from sklearn.model_selection import train_test_split
5 from sklearn.ensemble import RandomForestRegressor
6 from sklearn.metrics import mean_absolute_error

```

```

7  from matplotlib import pyplot as plt
8  import seaborn as sb
9  import matplotlib.pyplot as plt
10 import pandas as pd
11 import numpy as np
12 import warnings
13 from keras.callbacks import History
14 warnings.filterwarnings('ignore')
15 warnings.filterwarnings('ignore', category=
    DeprecationWarning)
16 NN_model = Sequential()
17
18 # The Input Layer :
19 NN_model.add(Dense(128, kernel_initializer='normal',
    input_dim = a_train.shape[1], activation='relu'))
20
21 # The Hidden Layers :
22 NN_model.add(Dense(256, kernel_initializer='normal',
    activation='relu'))
23 NN_model.add(Dense(256, kernel_initializer='normal',
    activation='relu'))
24 NN_model.add(Dense(256, kernel_initializer='normal',
    activation='relu'))
25
26 # The Output Layer :
27 NN_model.add(Dense(1, kernel_initializer='normal',
    activation='linear'))
28
29 # Compile the network :
30 NN_model.compile(loss='mean_absolute_error',
    optimizer='adam', metrics=['mean_absolute_error'])
31 NN_model.summary()
32 from keras.callbacks import History
33 history = History()
34 History=NN_model.fit(a_train, b_train, epochs=50,
    batch_size=500, validation_split = 0.2, callbacks
    =[history])

```

```

35 print(history.history.keys())
36 plt.plot(History.history['mean_absolute_error'])
37 plt.ylabel('mean_absolute_error')
38 plt.xlabel('epoch')
39
40 plt.plot(History.history['mean_absolute_error'])
41 plt.plot(History.history['val_mean_absolute_error'])
42 plt.title('mean_absolute_error')
43 plt.ylabel('mean_absolute_error')
44 plt.xlabel('epoch')
45 plt.legend(['train', 'test'], loc='upper_left')
46 plt.show()
47 # summarize history for loss
48 plt.plot(History.history['loss'])
49 plt.plot(History.history['val_loss'])
50 plt.title('model_loss')
51 plt.ylabel('loss')
52 plt.xlabel('epoch')
53 plt.legend(['train', 'test'], loc='upper_left')
54 plt.show()

```

## D.8 XGB REGRESSOR

```

1 from xgboost import XGBRegressor
2 from sklearn.metrics import mean_absolute_error
3 XGBModel = XGBRegressor()
4 XGBModel.fit(a_train,b_train , verbose=False)
5 accuracy = XGBModel.score(a_test,b_test)
6 print('accuracy=', accuracy*100)
7
8 # Get the mean absolute error on the validation data
9 :
10 XGBpredictions = XGBModel.predict(a_test)
11 MAE = mean_absolute_error(b_test , XGBpredictions)
12 print('MAE=', MAE)

```

## D.9 LINEAR REGRESSION

```
1 from sklearn.linear_model import LinearRegression
2 linear_regression = LinearRegression()
3 linear_regression.fit(X_train, y_train)
4 accuracy = linear_regression.score(X_test, y_test)
5 print (accuracy*100, '%')
```

#### **D.10 LASSO REGRESSION**

```
1 from sklearn.linear_model import Lasso
2 lasso = Lasso(alpha=0.3, max_iter=1)
3 lasso.fit(X_train, y_train)
4 accuracy = lasso.score(X_test, y_test)
5 print (accuracy*100, '%')
```

#### **D.11 CORRELATION HEATMAP**

```
1 import matplotlib.pyplot as plt
2 import seaborn as sb
3
4 C_mat = dataset.corr()
5 fig = plt.figure(figsize = (15,15))
6
7 sb.heatmap(C_mat, vmax = .8, square = True)
8 plt.show()
```

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